Series solution of differential equations Legendre polynomials

- In this lecture we will:
 - Use the power series method to solve general differential equations.
 - Use the power series technique to solve Legendre's equation using Legendre polynomials.
 - Look at some properties and applications of Legendre polynomials.
- A comprehension question for this lecture:
 - Write $x^3 + 2x$ in terms of Legendre polynomials by using their orthonormality.

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- These can be found using the initial conditions.
- For example, if y(0) = 0, we see $a_0 = 0$.
- Using this, and differentiating the polynomial solution, we see $y' = a_1 + ...$
- So if y'(0) = 1, this implies $a_1 = 1$.

Further coefficients can be found

• What are the values of the

using the recurrence relationship.

coefficients multiplying x4 and x5?









