

NuSTEC Neutrino Generator School



Lecture T7

Neutrino production of resonances

Luis Alvarez Ruso

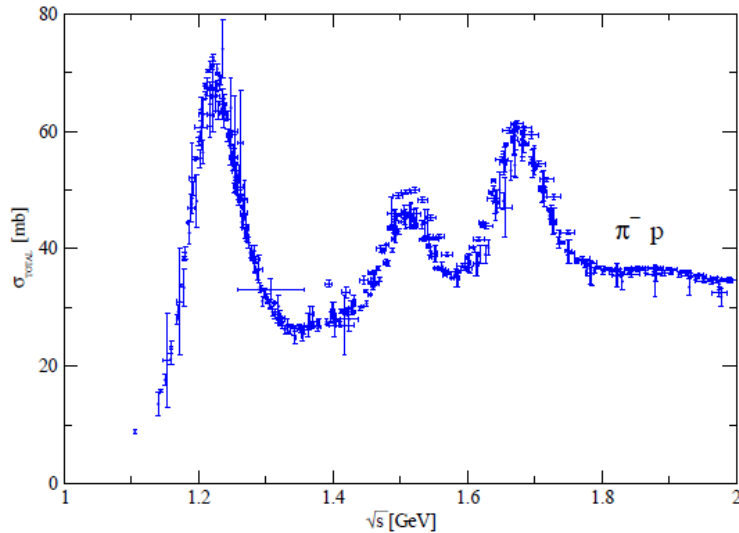


Outline

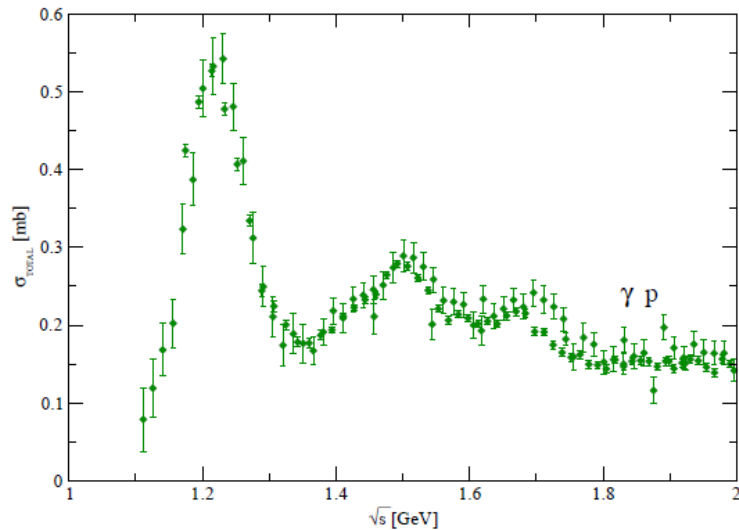
- Baryon resonance properties
- Partial Wave Analyses: MAID
- Weak resonance excitation
- The Rein-Sehgal model
- Non-resonant background

Baryon resonances

- Nucleons are extended objects \Rightarrow excitation spectrum



$$\pi N \rightarrow R \rightarrow \pi N, \pi\pi N, \eta N, \Lambda K \dots$$



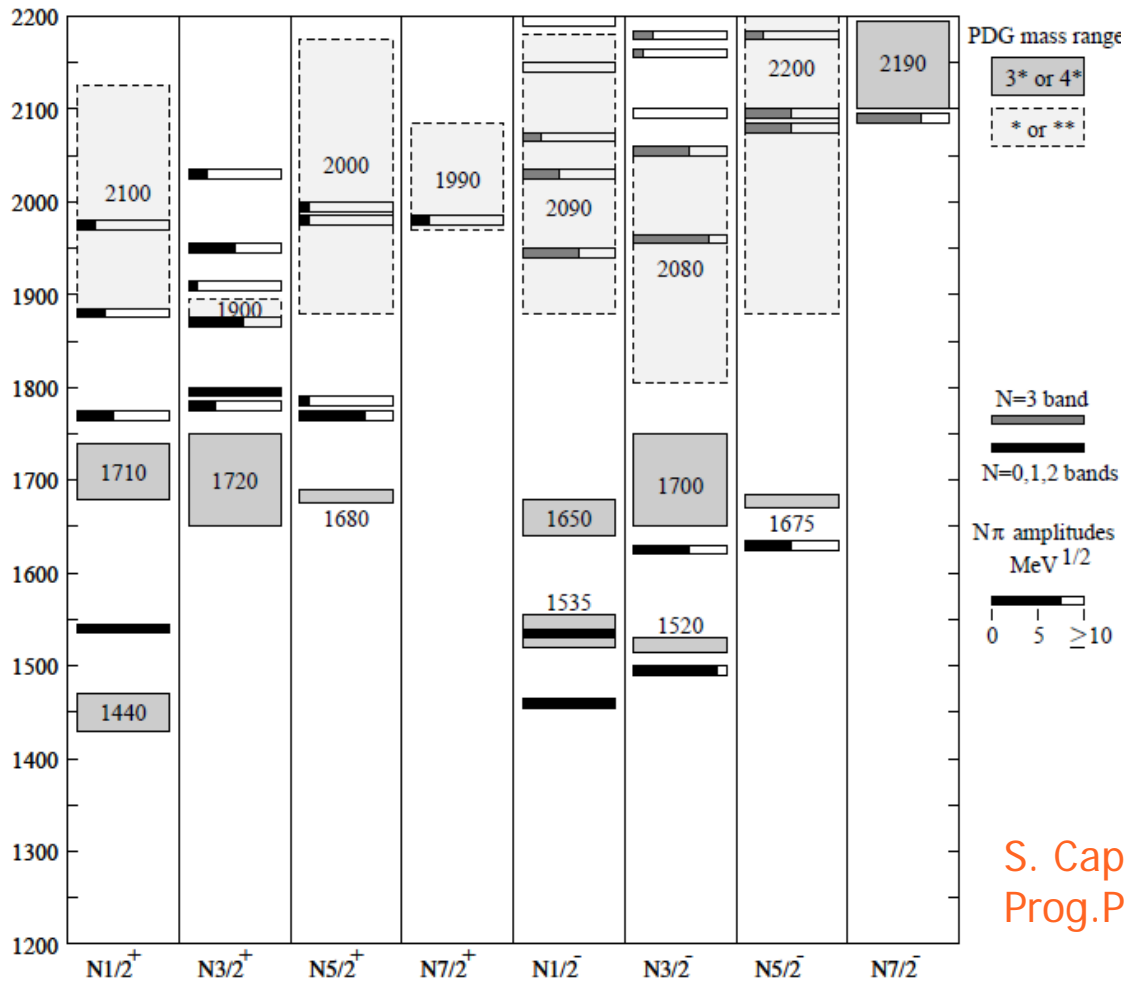
$$\gamma N \rightarrow R \rightarrow \pi N, \pi\pi N, \eta N, \Lambda K \dots$$

From PDG database

Baryon resonances

■ Nucleons are extended objects \Rightarrow excitation spectrum

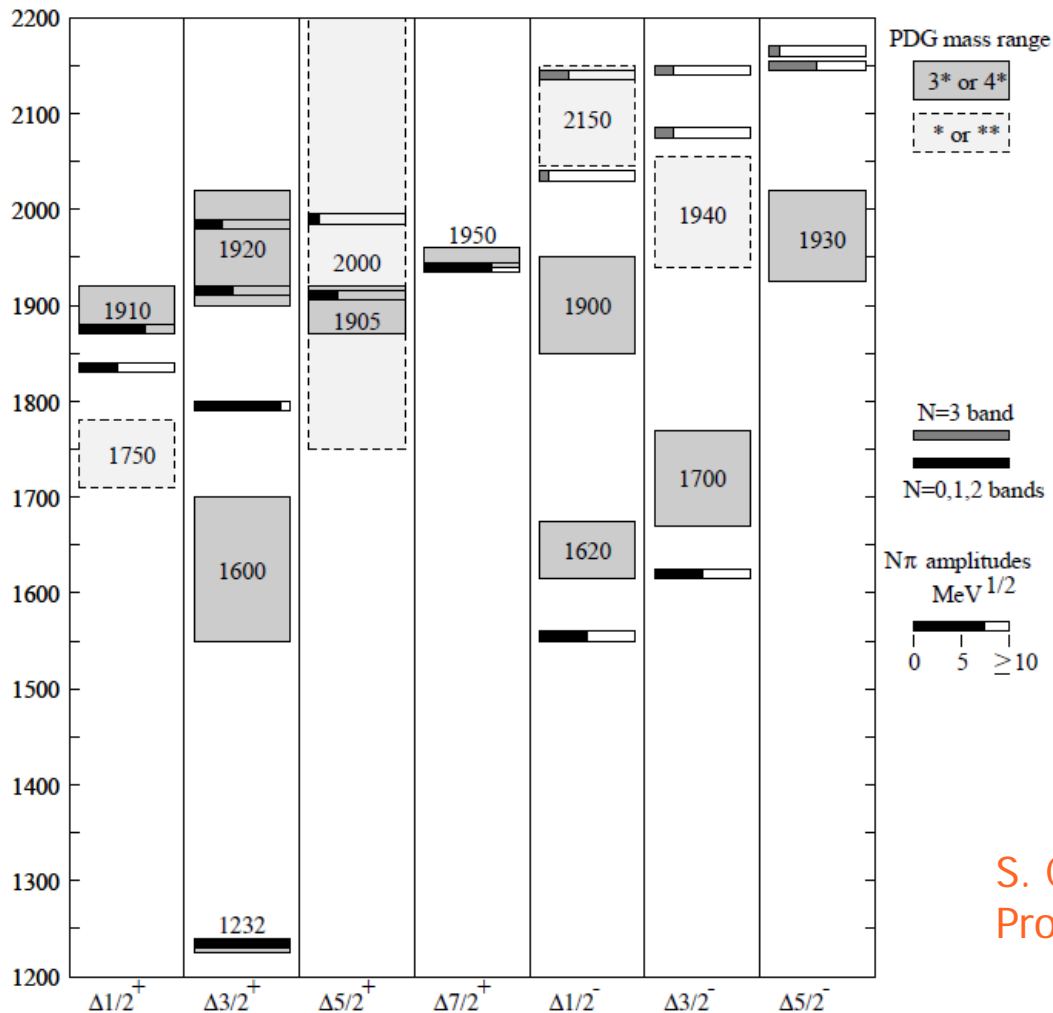
■ N ($I = 1/2$) states: $N(1440)P_{11}$, $N(1520)D_{13}$, $N(1535)S_{11}$, ...



S. Capstick, W. Roberts,
Prog.Part.Nucl.Phys.45(2000)241

Baryon resonances

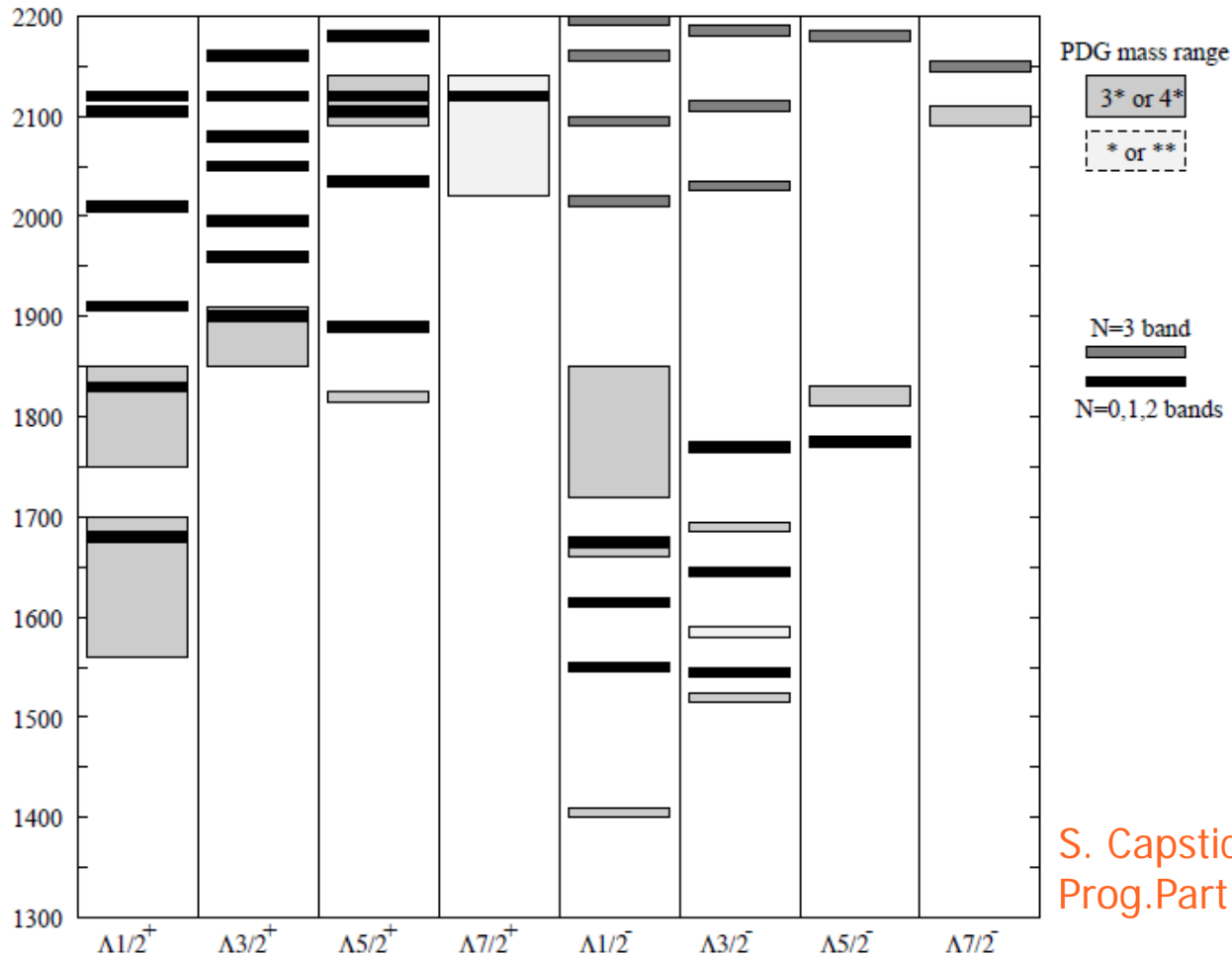
- Nucleons are extended objects \Rightarrow excitation spectrum
- Δ ($I = 3/2$) states: $\Delta(1232)P_{33}$, ...



S. Capstick, W. Roberts,
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Baryon resonances

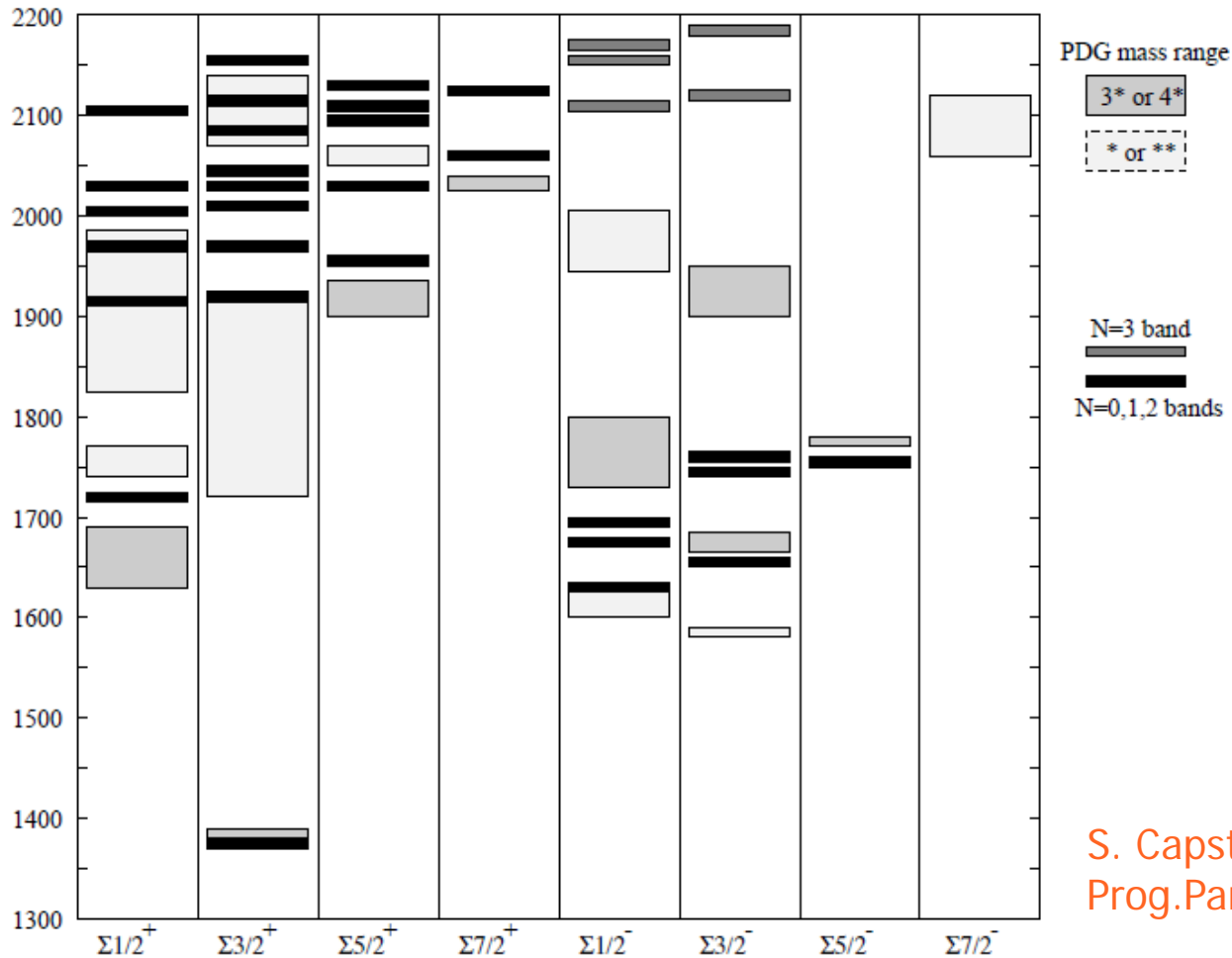
- Nucleons are extended objects \Rightarrow excitation spectrum
 - Λ ($S=-1, I=0$) states: $\Lambda(1405)$, ...



S. Capstick, W. Roberts,
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Baryon resonances

- Nucleons are extended objects \Rightarrow excitation spectrum
- Σ ($S=-1, I=1$) states: $\Sigma(1385)$, ...



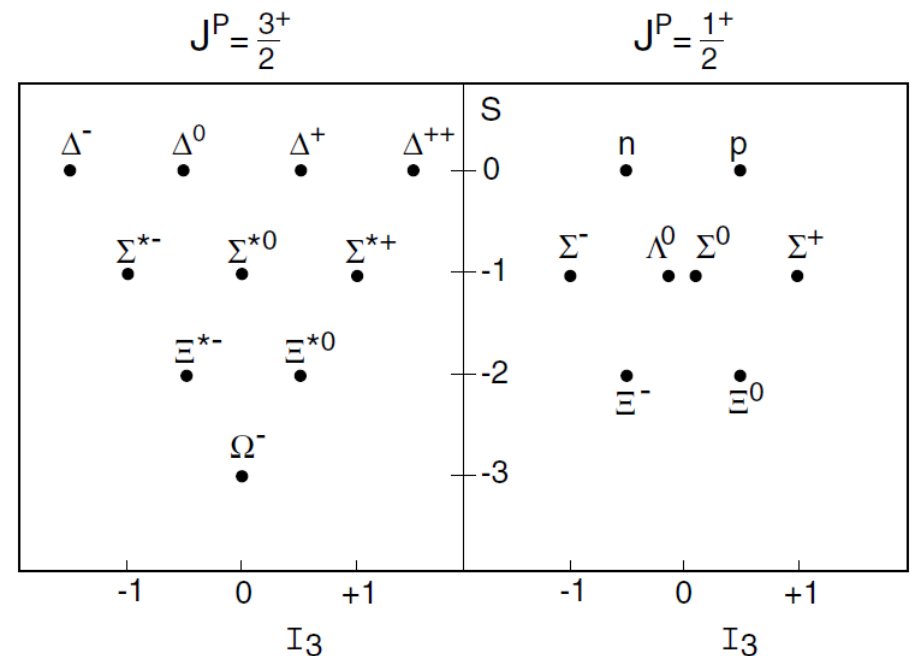
S. Capstick, W. Roberts,
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Baryon resonances

- **Nucleons** are extended objects \Rightarrow excitation spectrum
 - **N** ($I = 1/2$) states: $N(1440)P_{11}$, $N(1520)D_{13}$, $N(1535)S_{11}$, ...
 - Δ ($I = 3/2$) states: $\Delta(1232)P_{33}$, ...
 - Λ ($S=-1, I = 0$) states: $\Lambda(1405)$, ...
 - Σ ($S=-1, I = 1$) states: $\Sigma(1385)$, ...
 - Ξ ($S=-2, I=1/2$)
 - Ω ($S=-3, I=0$)
 - ...

- Constituent **quark** models:

- Color **singlet** (qqq)
- $3 \times 3 \times 3 = 10 + 8 + 8 + 1$



Baryon resonances

- **Nucleons** are extended objects \Rightarrow excitation spectrum
 - **N** ($I = 1/2$) states: $N(1440)P_{11}$, $N(1520)D_{13}$, $N(1535)S_{11}$, ...
 - Δ ($I = 3/2$) states: $\Delta(1232)P_{33}$, ...
 - Λ ($S=-1, I = 0$) states: $\Lambda(1405)$, ...
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 - ...
- Constituent **quark** models:
 - “Missing” resonances
 - $N(1440)$ is **lighter** than $N(1535)$
- There are **dynamically generated** states: $\Lambda(1405)$, $N(1535)$, ...

Baryon resonances

- Constituent **quark** models:
 - “Missing” resonances
 - N(1440) is **lighter** than N(1535)

In a **Quark Model** with an **oscillator** V :

$$E = \hbar\omega \left(n + \frac{3}{2} \right) \text{ with } n = 2n_r + l$$

$$n = 0 \quad l = 0 \quad \Rightarrow \quad N \quad (J^P = 1/2^+)$$

$$n = 1 \quad l = 1 \quad \Rightarrow \quad N^* \quad (J^P = 1/2^-)$$

$$n = 2 \quad l = 0 \quad \Rightarrow \quad N^* \quad (J^P = 1/2^+)$$

Baryon resonances

- **Nucleons** are extended objects \Rightarrow excitation spectrum
 - **N** ($I = 1/2$) states: $N(1440)P_{11}$, $N(1520)D_{13}$, $N(1535)S_{11}$, ...
 - Δ ($I = 3/2$) states: $\Delta(1232)P_{33}$, ...
 - Λ ($S=-1, I = 0$) states: $\Lambda(1405)$, ...
 - Σ ($S=-1, I = 1$) states: $\Sigma(1385)$, ...
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 - ...
- Constituent **quark** models:
 - “Missing” resonances
 - $N(1440)$ is **lighter** than $N(1535)$
- There are **dynamically generated** states: $\Lambda(1405)$, $N(1535)$, ...

Baryon resonances

- **Resonance** properties

- Quantum numbers

- Mass, width, branching ratios

- Originally from $\pi N \rightarrow \pi N$

- Electromagnetic properties $\leftrightarrow \gamma N \rightarrow \pi N, \gamma^* N \rightarrow \pi N$

$$\sigma(W) = \sigma_0 \frac{M^2 B_{in} B_{out} \Gamma^2}{(W^2 - M^2)^2 + M^2 \Gamma^2} \Rightarrow \begin{cases} W_R \approx M + i\frac{\Gamma}{2} \\ B_{in}, B_{out} \end{cases}$$

- But

- Resonances **overlap**: $N(1440)P_{11}$, $N(1520)D_{13}$, $N(1535)S_{11}$

- Resonances might not produce a peak in the (certain) cross section

- $N(1440)P_{11}$

- $\Sigma(1385)$: peak in the $\pi \Lambda$ **invariant mass** in $K^- p \rightarrow \pi^- \pi^+ \Lambda$

- $\Gamma = \Gamma(W) \sim q_{cm}^l$

- **Background/resonance** separation is **model dependent**

- Need for **Partial Wave Analyses**

MAID

- Unitary isobar model for $\gamma^* N \rightarrow N \pi$ Tiator et al., EPJ Special Topics 198 (2011)

$$T_{\gamma\pi}(W, Q^2) = T_{\gamma\pi}^B(W, Q^2) + T_{\gamma\pi}^R(W, Q^2)$$

- For each partial wave α :

$$T_{\gamma\pi}^{B,\alpha}(W, Q^2) = V_{\gamma\pi}^{B,\alpha}(W, Q^2) [1 + iT_{\pi N}^\alpha(W)]$$

$$V_{\gamma\pi}^{B,\alpha}(W, Q^2) \leftarrow \text{Born terms, phenomenological model}$$

$$T_{\pi N}^\alpha(W) \leftarrow \pi N \text{ elastic amplitude, from SAID}$$

$$T_{\gamma\pi}^{R,\alpha} = -\bar{\mathcal{A}}_\alpha^R(W, Q^2) \frac{f_{\gamma N}(W)\Gamma_{\text{tot}}(W)f_{\pi N}(W)}{W^2 - M_R^2 + iM_R\Gamma_{\text{tot}}(W)} e^{i\phi_R(W, Q^2)}$$

$$f_{\pi N}(W) \leftarrow \text{Breit-Wigner factor for resonance decay}$$

$$f_{\gamma N}(W) \leftarrow \gamma N R \text{ vertex}$$

$$\phi_R(W, Q^2) \leftarrow \text{adjusted to fulfill Watson theorem}$$

$$\bar{\mathcal{A}}_\alpha^R(W, Q^2) \leftarrow \text{Multipole amplitudes}$$

MAID

- Unitary isobar model for $\gamma^* N \rightarrow N \pi$ Tiator et al., EPJ Special Topics 198 (2011)

$$T_{\gamma\pi}(W, Q^2) = T_{\gamma\pi}^B(W, Q^2) + T_{\gamma\pi}^R(W, Q^2)$$

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$$\bar{\mathcal{A}}_{\alpha}^R(W, Q^2) \leftarrow \text{Multipole amplitudes}$$

- $j=l + 1/2$:

$$A_{1/2} = -\frac{1}{2} [(l+2)\bar{E}_{l+} + l\bar{M}_{l+}]$$

$$A_{3/2} = \frac{1}{2} \sqrt{l(l+2)} (\bar{E}_{l+} - \bar{M}_{l+})$$

$$S_{1/2} = -\frac{l+1}{\sqrt{2}} \bar{S}_{l+}$$

MAID

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$$T_{\gamma\pi}(W, Q^2) = T_{\gamma\pi}^B(W, Q^2) + T_{\gamma\pi}^R(W, Q^2)$$

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$$\bar{\mathcal{A}}_{\alpha}^R(W, Q^2) \leftarrow \text{Multipole amplitudes}$$

- $j=l - 1/2$:

$$A_{1/2} = \frac{1}{2} [(l+1)\bar{M}_{l-} - (l-1)\bar{E}_{l-}]$$

$$A_{3/2} = -\frac{1}{2} \sqrt{(l-1)(l+1)} (\bar{E}_{l-} + \bar{M}_{l-})$$

$$S_{1/2} = -\frac{l}{\sqrt{2}} \bar{S}_{l-}$$

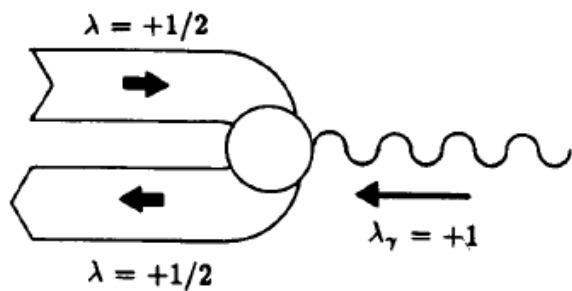
MAID

■ Helicity amplitudes

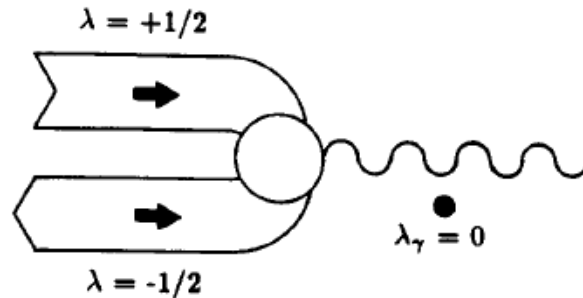
$$A_{1/2} = \sqrt{\frac{2\pi\alpha}{k_R}} \langle R, J_z = 1/2 | \epsilon_\mu^+ J_{\text{EM}}^\mu | N, J_z = -1/2 \rangle \zeta$$

$$A_{3/2} = \sqrt{\frac{2\pi\alpha}{k_R}} \langle R, J_z = 3/2 | \epsilon_\mu^+ J_{\text{EM}}^\mu | N, J_z = 1/2 \rangle \zeta$$

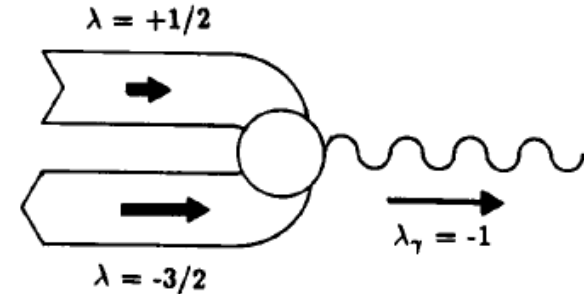
$$S_{1/2} = -\sqrt{\frac{2\pi\alpha}{k_R}} \frac{|\mathbf{q}|}{\sqrt{Q^2}} \langle R, J_z = 1/2 | \epsilon_\mu^0 J_{\text{EM}}^\mu | N, J_z = 1/2 \rangle \zeta$$



$A_{1/2}$



$S_{1/2}$

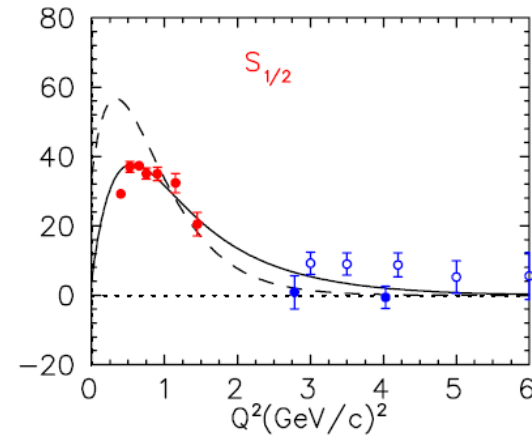
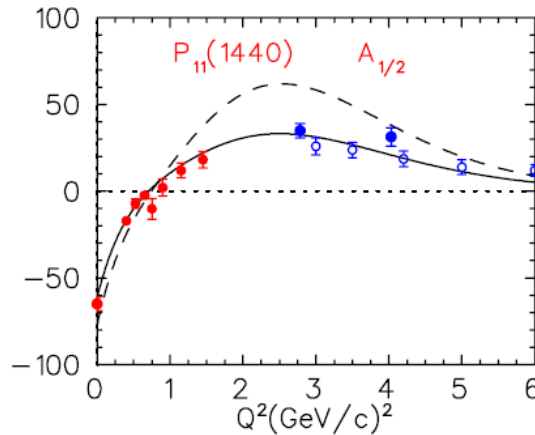
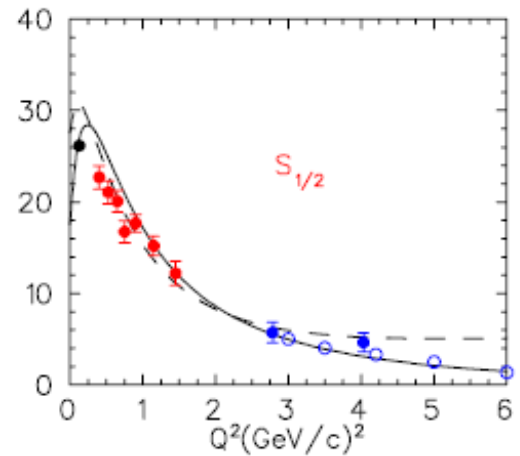
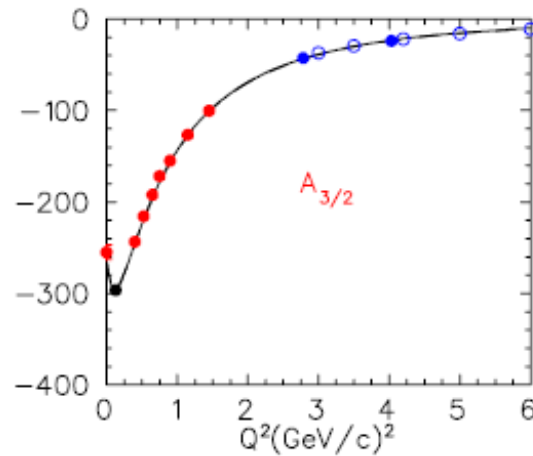
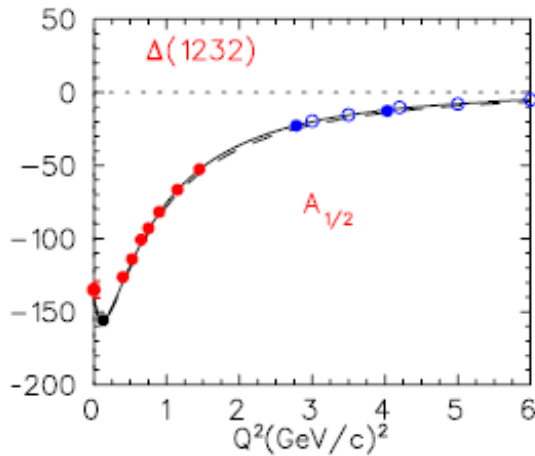


$A_{3/2}$

MAID

- **Transition N-R e.m. helicity amplitudes extracted** for all 4-star resonances with $W < 1.8$ GeV
- For example:

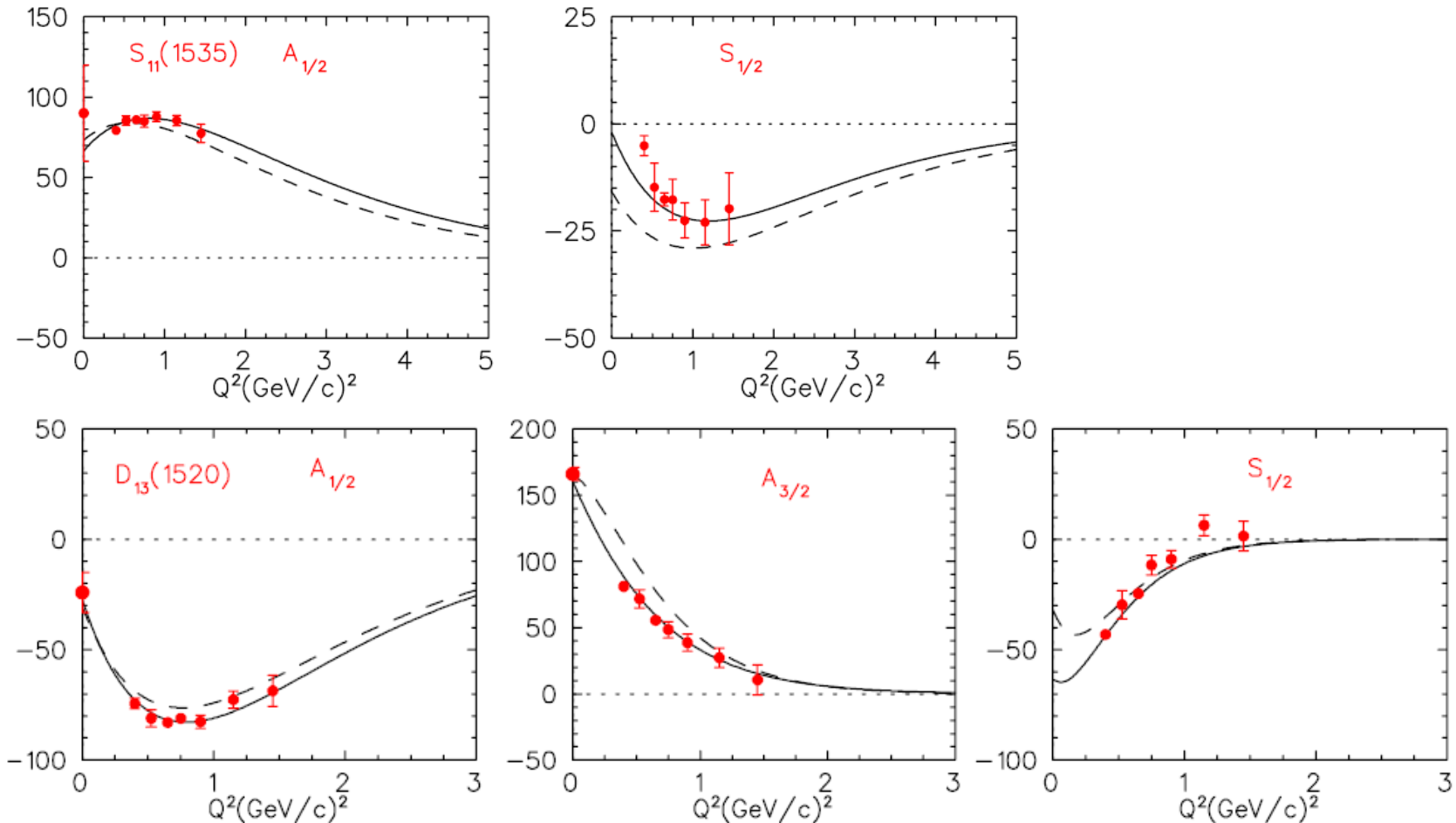
Tiator et al., EPJ Special Topics 198 (2011)



MAID

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- For example:

Tiator et al., EPJ Special Topics 198 (2011)



Weak Resonance excitation

- **Resonances** contribute to:

- the **inclusive** $\nu_l N \rightarrow l X$ cross section

- several **exclusive** channels: $\nu_l N \rightarrow l N' \pi$

$$\nu_l N \rightarrow l N' \gamma$$

$$\nu_l N \rightarrow l N' \eta$$

$$\nu_l N \rightarrow l \Lambda(\Sigma) \bar{K}$$

- At $E_\nu \sim 1$ GeV (MiniBooNE, SciBooNE, T2K,...) $\Delta(1232)$ is **dominant**

- At $E_\nu > 1$ GeV (MINER ν A) N^* become also **important**

Weak Resonance excitation

- CC R excitation: $\nu_l(k) N(p) \rightarrow l^-(k') R(p')$

$$\frac{d\sigma}{dk'_0 d\Omega'} = \frac{1}{32\pi^2} \frac{|\vec{k}'|}{k_0 M_N} \mathcal{A}(p') |\bar{\mathcal{M}}|^2 \quad \leftarrow \text{Inclusive cross section}$$

$$\mathcal{A}(p') = \frac{M^*}{\pi} \frac{\Gamma(p')}{(p'^2 - M^{*2})^2 + M^{*2} \Gamma^2(p')}$$

$\Gamma(p')$ \leftarrow total momentum dependent **width**

$$\mathcal{M} = \frac{G_F \cos \theta_C}{\sqrt{2}} l^\alpha J_\alpha$$

$$l^\alpha = \bar{u}(k') \gamma^\alpha (1 - \gamma_5) u(k) \quad \leftarrow \text{leptonic current}$$

$$J_\alpha = V_\alpha - A_\alpha \quad \leftarrow \text{hadronic current}$$

can be parametrized in terms of
N-R transition **form factors**

Weak Resonance excitation

- $\Delta(1232)$ $J^P=3/2^+$

$$J_\alpha = \bar{u}^\mu(p') \left[\left(\frac{C_3^V}{M_N} (g_{\alpha\mu} \not{q} - q_\alpha \gamma_\mu) + \frac{C_4^V}{M_N^2} (g_{\alpha\mu} q \cdot p' - q_\alpha p'_\mu) + \frac{C_5^V}{M_N^2} (g_{\alpha\mu} q \cdot p - q_\alpha p_\mu) \right) \gamma_5 \right. \\ \left. + \frac{C_3^A}{M_N} (g_{\alpha\mu} \not{q} - q_\alpha \gamma_\mu) + \frac{C_4^A}{M_N^2} (g_{\alpha\mu} q \cdot p' - q_\beta p'_\mu) + C_5^A g_{\alpha\mu} + \frac{C_6^A}{M_N^2} q_\alpha q_\mu \right] u(p)$$

$C_{3-5}^V, C_{3-6}^A \leftarrow$ N- Δ transition form factors

- Rarita-Schwinger fields: spin 3/2

$$u_\mu(p, s_\Delta) = \sum_{\lambda, s} \left(1\lambda \frac{1}{2}s \middle| \frac{3}{2}s_\Delta \right) \epsilon_\mu(p, \lambda) u(p, s)$$

- Eq. of motion: $(\not{p} - M_\Delta) u_\mu = 0$
- with constrains: $\gamma^\mu u_\mu = p^\mu u_\mu = 0$

Weak Resonance excitation

- Second resonance peak: $N^*(1440)$, $N^*(1520)$, $N^*(1535)$

- $N^*(1440)$ $J^P=1/2^+$

$$J_\alpha = \bar{u}(p') \left[\frac{F_1^V}{(2M_N)^2} (\not{q}q_\alpha - q^2\gamma_\alpha) + i \frac{F_2^V}{2M_N} \sigma_{\alpha\beta} q^\beta - F_A \gamma_\alpha \gamma_5 - \frac{F_P}{M_N} \gamma_5 q_\alpha \right] u(p)$$

- $N^*(1535)$ $J^P=1/2^-$

$$J_\alpha = \bar{u}(p') \left[\frac{F_1^V}{(2M_N)^2} (\not{q}q_\alpha - q^2\gamma_\alpha) \gamma_5 + i \frac{F_2^V}{2M_N} \sigma_{\alpha\beta} q^\beta \gamma_5 - F_A \gamma_\alpha - \frac{F_P}{M_N} q_\alpha \right] u(p)$$

- $N^*(1520)$ $J^P=3/2^-$

$$J_\alpha = \bar{u}^\mu(p') \left[\frac{C_3^V}{M_N} (g_{\alpha\mu} \not{q} - q_\alpha \gamma_\mu) + \frac{C_4^V}{M_N^2} (g_{\alpha\mu} q \cdot p' - q_\alpha p'_\mu) + \frac{C_5^V}{M_N^2} (g_{\alpha\mu} q \cdot p - q_\alpha p_\mu) \right. \\ \left. + \left(\frac{C_3^A}{M_N} (g_{\alpha\mu} \not{q} - q_\alpha \gamma_\mu) + \frac{C_4^A}{M_N^2} (g_{\alpha\mu} q \cdot p' - q_\beta p'_\mu) + C_5^A g_{\alpha\mu} + \frac{C_6^A}{M_N^2} q_\alpha q_\mu \right) \gamma_5 \right] u(p)$$

Weak Resonance excitation

- **Vector CC** and **NC** form factors can be expressed in terms of **EM** ones

- **CC**: $F_{1,2}^V = F_{1,2}^p - F_{1,2}^n$

- **NC**: $\tilde{F}_{1,2}^{p(n)} = \left(\frac{1}{2} - 2 \sin^2 \theta_W \right) F_{1,2}^{p(n)} - F_{1,2}^{n(p)}$

- The same applies for $C_{1,2,3}^V$

- **Helicity amplitudes** from π photo- and electro-production data

$$A_{1/2} = \sqrt{\frac{2\pi\alpha}{k_R}} \langle R, J_z = 1/2 | \epsilon_\mu^+ J_{\text{EM}}^\mu | N, J_z = -1/2 \rangle \zeta$$

$$A_{3/2} = \sqrt{\frac{2\pi\alpha}{k_R}} \langle R, J_z = 3/2 | \epsilon_\mu^+ J_{\text{EM}}^\mu | N, J_z = 1/2 \rangle \zeta$$

$$S_{1/2} = -\sqrt{\frac{2\pi\alpha}{k_R}} \frac{|\mathbf{q}|}{\sqrt{Q^2}} \langle R, J_z = 1/2 | \epsilon_\mu^0 J_{\text{EM}}^\mu | N, J_z = 1/2 \rangle \zeta$$

- **Helicity amplitudes** \Rightarrow **EM form factors**

Weak Resonance excitation

- Axial transition form factors

- Poorly known (if at all...)

- PCAC: $q^\alpha A_\alpha \approx 0$

- π -pole dominance of the pseudoscalar form factor: C_6^A

- $\Delta(1232)$ $J^P=3/2^+$

$$\text{PCAC} \Rightarrow C_6^A = -\frac{M_N^2}{q^2} C_5^A$$

$$\text{Using } \mathcal{L}_{\Delta N \pi} = -\frac{g_{\Delta N \pi}}{f_\pi} \bar{\Delta}_\mu (\partial^\mu \vec{\pi}) \vec{T}^\dagger N \quad g_{\Delta N \pi} \leftrightarrow \Gamma(N^* \rightarrow N \pi)$$

$$\pi\text{-pole dominance} \Rightarrow C_6^A = -\sqrt{\frac{2}{3}} g_{N^* N \pi} F(q^2) \frac{M_N^2}{q^2 - m_\pi^2} \quad F(0) = 1$$

$$\text{Therefore } C_5^A(0) = \sqrt{\frac{2}{3}} g_{\Delta N \pi} \leftarrow \text{Goldberger-Treiman relation}$$

$$C_4^A = -\frac{1}{4} C_5^A \quad C_3^A = 0 \leftarrow \text{Adler model}$$

Weak Resonance excitation

- Axial transition form factors

- $\Delta(1232)$ $J^P=3/2^+$

- Constraints from ANL and BNL data on $\nu_\mu d \rightarrow \mu^- \pi^+ p n$
 - with large normalization (flux) uncertainties

- Graczyk et al., PRD 80 (2009)

- Deuteron effects

- Non-resonant background **absent**

- $C_A^5(0) = 1.19 \pm 0.08$, $M_{A\Delta} = 0.94 \pm 0.03$ GeV

- Hernandez et al., PRD 81 (2010)

- Deuteron effects

- Non-resonant background fixed by chiral symmetry

- $C_A^5(0) = 1.00 \pm 0.11$ GeV, $M_{A\Delta} = 0.93 \pm 0.07$ GeV

- 20 % reduction of the GT relation: $C_A^5(0) \approx 1.2$

- But Watson's theorem is not fulfilled

- ANL and BNL data **do not** constrain $C_{A3,4}$

Weak Resonance excitation

- Axial transition form factors

- Poorly known (if at all...)

- PCAC: $q^\alpha A_\alpha \approx 0$

- π -pole dominance of the pseudoscalar form factor: F_P

- $N^*(1440)$ $J^P=1/2^+$

$$\text{PCAC} \Rightarrow F_P = -\frac{(M^* + M_N)M_N}{q^2} F_A$$

$$\text{Using } \mathcal{L}_{N^*N\pi} = -\frac{g_{N^*N\pi}}{f_\pi} \bar{N}^* \gamma_\mu \gamma_5 (\partial^\mu \vec{\pi}) \vec{\tau} N \quad g_{N^*N\pi} \Leftrightarrow \Gamma(N^* \rightarrow N\pi)$$

$$\pi\text{-pole dominance} \Rightarrow F_P = -2g_{N^*N\pi} F(q^2) \frac{(M^* + M_N)M_N}{q^2 - m_\pi^2} \quad F(0) = 1$$

Therefore $F_A(0) = 2g_{N^*N\pi} \leftarrow$ Goldberger-Treiman relation

$$\text{Educated guess: } F_A(q^2) = F_A(0) \left(1 - \frac{q^2}{M_A^2}\right)^{-2} \quad M_A = 1 \text{ GeV}$$

Weak Resonance excitation

- Axial transition form factors

- Poorly known (if at all...)

- PCAC: $q^\alpha A_\alpha \approx 0$

- π -pole dominance of the pseudoscalar form factor: F_P

- $N^*(1535)$ $J^P=1/2^-$

$$\text{PCAC} \Rightarrow F_P = -\frac{(M^* - M_N)M_N}{q^2} F_A$$

$$\text{Using } \mathcal{L}_{N^*N\pi} = -\frac{g_{N^*N\pi}}{f_\pi} \bar{N}^* \gamma_\mu (\partial^\mu \vec{\pi}) \vec{\tau} N \quad g_{N^*N\pi} \Leftrightarrow \Gamma(N^* \rightarrow N\pi)$$

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Weak Resonance excitation

- Axial transition form factors

- Poorly known (if at all...)

- PCAC: $q^\alpha A_\alpha \approx 0$

- π -pole dominance of the pseudoscalar form factor: C_6^A

- $N^*(1520)$ $J^P=3/2^-$

$$\text{PCAC} \Rightarrow C_6^A = -\frac{M_N^2}{q^2 - m_\pi^2} C_5^A$$

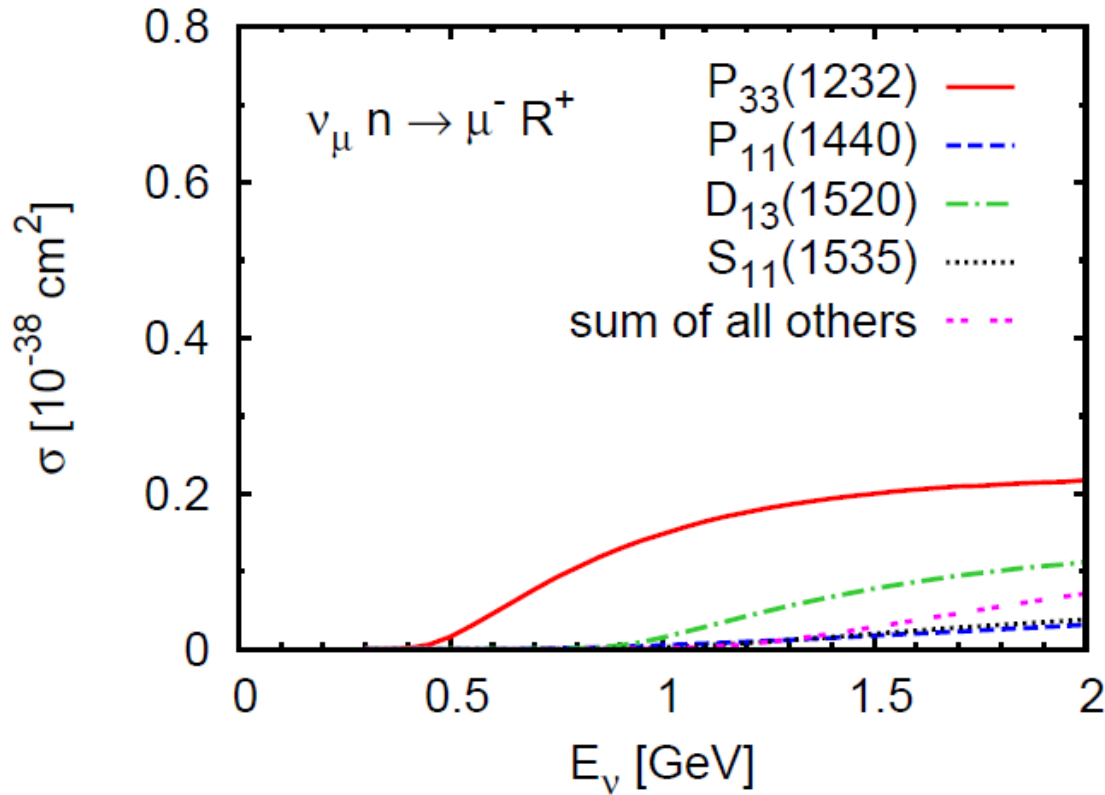
$$\text{Using } \mathcal{L}_{N^*N\pi} = -\frac{g_{N^*N\pi}}{f_\pi} \bar{N}_\mu^* \gamma_5 (\partial^\mu \vec{\pi}) \vec{\tau} N \quad g_{N^*N\pi} \Leftrightarrow \Gamma(N^* \rightarrow N\pi)$$

$$\pi\text{-pole dominance} \Rightarrow C_6^A = 2g_{N^*N\pi} F(q^2) \frac{M_N^2}{q^2 - m_\pi^2} \quad F(0) = 1$$

Therefore $C_5^A(0) = -2g_{N^*N\pi}$ ← Goldberger-Treiman relation

$$\text{Educated guess: } C_5^A(q^2) = C_5^A(0) \left(1 - \frac{q^2}{M_A^2}\right)^{-2} \quad M_A = 1 \text{ GeV} \quad C_3^A = C_4^A = 0$$

Inclusive resonance production



T. Leitner, O. Buss, LAR, U. Mosel, PRC 79 (2009)
 T. Leitner, PhD Thesis, 2009

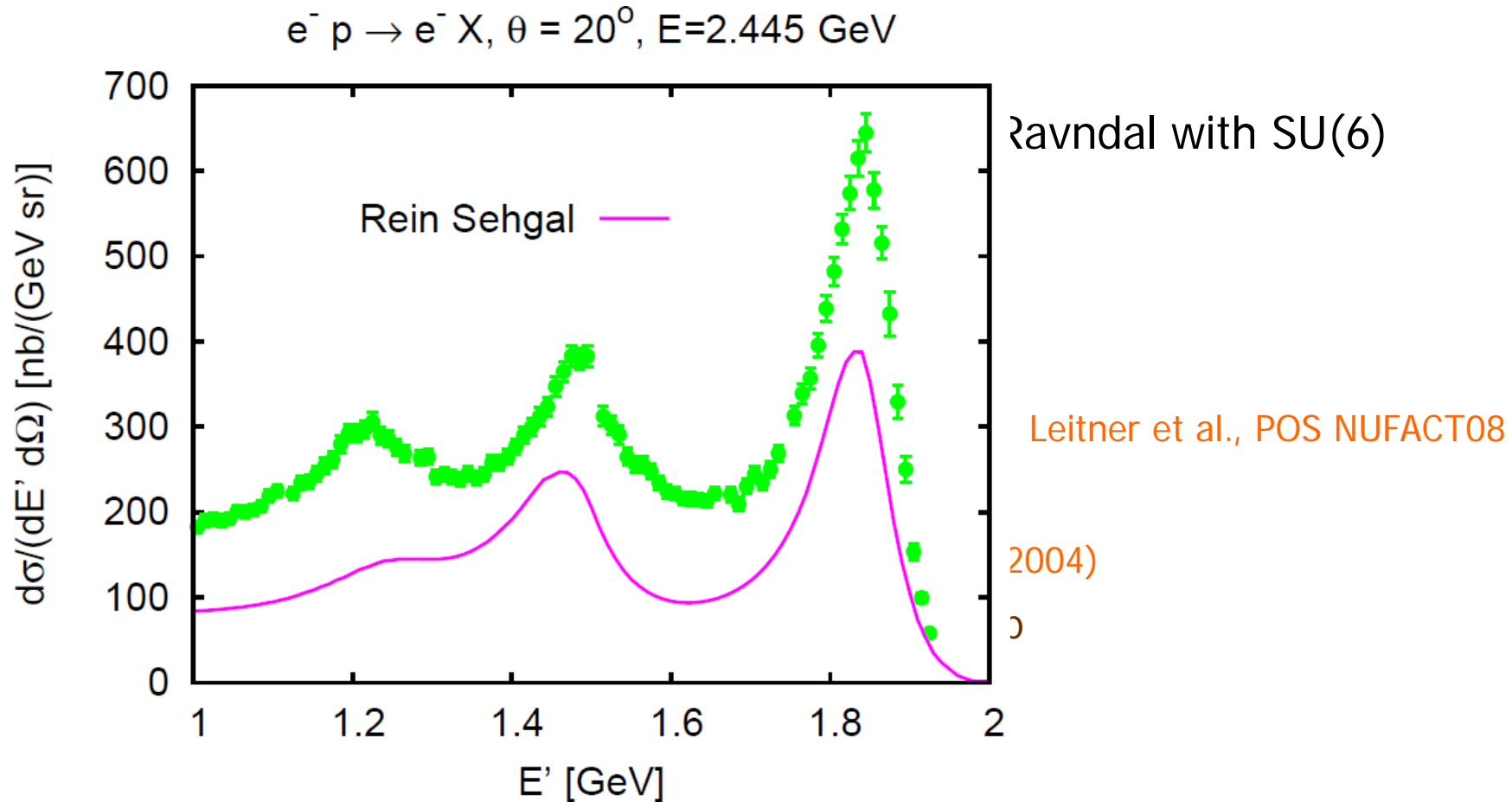
- At $E_\nu = 2$ GeV, $\text{CCN}^*(1520)/\text{CC}\Delta \sim 0.5$, $\text{CCN}^*(1440,1535)/\text{CC}\Delta \sim 0.22$
- $\text{N}^*(1520)$ is important for $\nu_l N \rightarrow l N' \pi$

Resonances in ν generators

- Rein-Sehgal model: Rein, Sehgal, Ann. Phys. 133 (1981) 79.
 - Used by almost all MC generators
 - Relativistic quark model of Feynman-Kislinger-Ravndal with SU(6) spin-flavor symmetry
 - Helicity amplitudes for 18 baryon resonances
 - Lepton mass = 0
 - Corrections: Kuzmin et al., Mod. Phys. Lett. A19 (2004)
Berger, Sehgal, PRD 76 (2007)
Graczyk, Sobczyk, PRD 77 (2008)
 - Poor description of π electroproduction data on p

Resonances in ν generators

- Rein-Sehgal model: Rein, Sehgal, Ann. Phys. 133 (1981) 79.

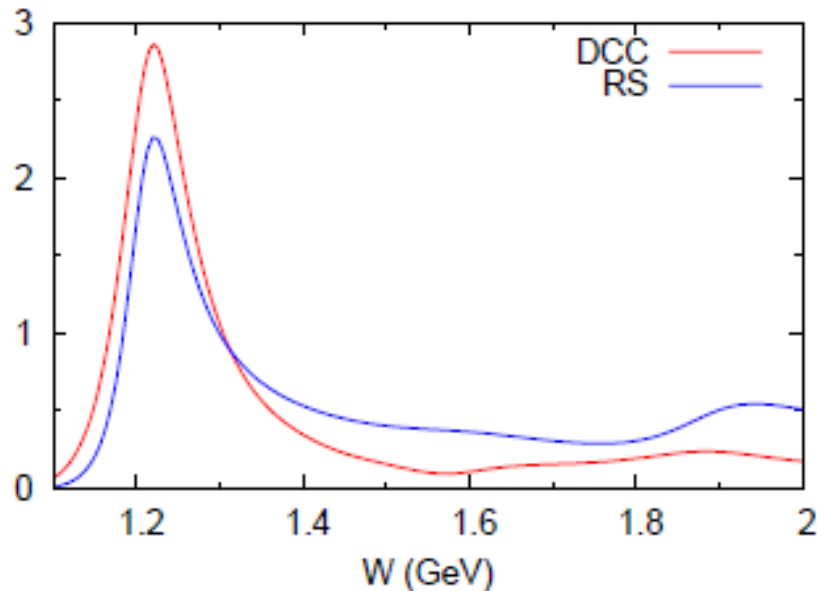


Resonances in ν generators

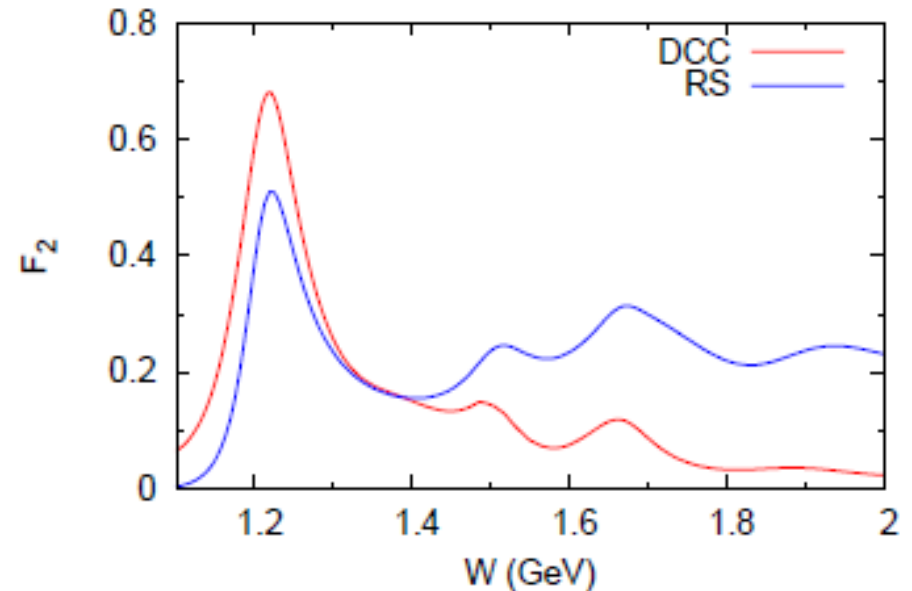
- Rein-Sehgal model: Rein, Sehgal, Ann. Phys. 133 (1981) 79.

- Used by almost all MC generators

$\nu_e + p \rightarrow e^- + p + \pi^+$



$\nu_e + n \rightarrow e^- + p + \pi^0$



- Also **unsatisfactory** in the axial sector: Kamano et al., PRD86 (2012)

PCAC (at $Q^2 \rightarrow 0$): $\pi N \rightarrow X \Leftrightarrow F_2$

Non-resonant background

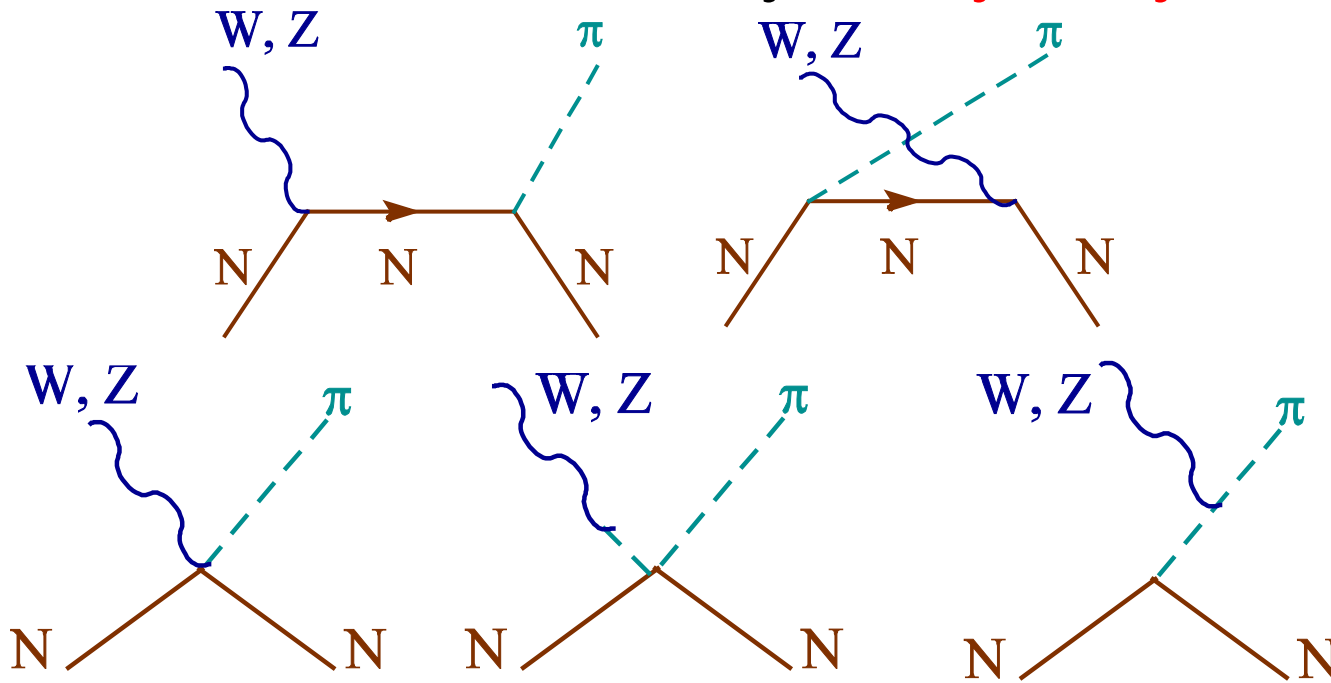
- **Specific** for each exclusive process
- Background terms **interfere** with the resonant contributions
- $\nu_l N \rightarrow l N' \pi$
- In Rein-Sehgal model: Rein, Sehgal, *Ann. Phys.* 133 (1981) 79.

“we have represented the background by a resonance amplitude of P11 character (like the nucleon), with the Breit-Wigner factor replaced by an adjustable constant. The corresponding cross section is added incoherently to the resonant cross section.”

- General principles:
 - **CVC**, **PCAC**
 - Threshold behavior dictated by **chiral symmetry** of QCD

Non-resonant background

- **Specific** for each exclusive process
- Background terms **interfere** with the resonant contributions
- $\nu_l N \rightarrow l N' \pi$
- General principles:
 - **CVC**, **PCAC**
 - Threshold behavior dictated by **chiral symmetry** of QCD



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