## **The MUonE Experiment:** Understanding Muon g - 2 Puzzle via $\mu - e$ Scattering

Ce Zhang

INPAC/SJTU Seminar 15/09/2023



LEVERHULME TRUST \_\_\_\_\_

## **The MUonE Experiment:** Understanding Muon g - 2 Puzzle via $\mu - e$ Scattering

- Muon g 2 Puzzle
- MUonE Experiment
  - Principle
  - Apparatus (tracker, calo, muon beam...)
  - Simulation, Analysis & Systematics Effects
  - Test Runs
  - Current Status (the collaboration, schedule...)

# Muon g - 2

- The anomalous magnetic moment of the muon:
  - Magnetic moments **precess** in a magnetic field  $\vec{\mu} = g \frac{e}{2m} \vec{S}$
  - g factor quantifies interaction strength
  - Dirac predicted q = 2 for spin-1/2 fermions
- Interactions with virtual particles cause g to deviate from 2 (g > 2). Muon magnetic anomaly is defined as:

$$a_{\mu} = \frac{g-2}{2}$$



 $a_l = \frac{g_l - 2}{2} = \frac{\alpha}{2\pi} + O(\alpha^2)$ 

= 0.00116140



Muon g - 2

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$$a_{\mu} = \frac{g-2}{2}$$









#### • Latest result announced at Fermilab on Aug. 10, 2023



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FNAL (2021) + BNL average in tension with Theory Initiative White Paper (2020) at  $4.2 \sigma$ 

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#### **Discrepancy between Experiments & Theories**



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  - New e<sup>+</sup>e<sup>-</sup> → π<sup>+</sup>π<sup>-</sup> cross section from CMD-3 (2023)

> Disclaimer:

The CMD-3 point is a visual exercise. It is not a fully updated SM prediction!

- TI White Paper result has been substituted by CMD-3 only for 0.33 → 1.0 GeV.
- The NLO HVP has not been updated.
- It is purely for demonstration purposes → <u>should not be taken as final!</u>



#### **Discrepancy between Experiments & Theories**



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- Since then, two important developments on SM prediction:
  - Lattice QCD from the BMW (2020)
  - New e<sup>+</sup>e<sup>-</sup> → π<sup>+</sup>π<sup>-</sup> cross section from CMD-3 (2023)
- Future experimental progress:
  - Fermilab (final) Run 4/5/6 (~ 2 yrs)
  - New approach at J-PARC (2028 )



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  - 1) Lattice QCD Method: Ab-initio calculation on lattice





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Hadrons

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$$a_{\mu}^{\text{HVP}} = \left(\frac{\alpha m_{\mu}}{3\pi}\right)^2 \int_{m_{\pi^0}}^{\infty} ds \, \frac{R_{\text{had}}(s) \, K(s)}{s^2}, \quad R_{\text{had}}(s) = \sigma(e^+e^- \to \text{hadrons}) \left| \frac{4\pi \, \alpha(s)}{(3s)} \right|^2$$

**Muon** g - 2 **Puzzle** Dispersive Method Using Collider Data



•  $e^+e^- \rightarrow \pi^+\pi^-$  channel is the major source of uncertainty



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### **Muon** g - 2 **Puzzle** $e^+e^- \rightarrow \pi^+\pi^-$ Channel



• The discrepancy between BABAR and KLOE needs to be understood

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## **Muon** g - 2 **Puzzle** CMD-3 Result on $e^+e^- \rightarrow \pi^+\pi^-$ Channel



 A recent CMD-3 result is different from all the previous data → more chaotic!

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## **Muon** g - 2 **Puzzle** CMD-3 Result on $e^+e^- \rightarrow \pi^+\pi^-$ Channel



- A recent CMD-3 result is different from all the previous data → more chaotic!
- A quick summary on the puzzle:
  - $a_{\mu}^{\text{HVP}}$  represents a major uncertainty
  - $e^+e^-$  data-driven dispersive  $\Leftrightarrow$  Lattice (BMW)

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- Within the data-driven method:
  - Babar ⇔ KLOE (recently, some clues on MC generator...)
  - Latest CMD3  $\Leftrightarrow$  all the previous data



A New Approach towards  $a_{\mu}^{\text{HVP}}$  with running of  $\Delta \alpha_{\text{had}}$ 

• The dispersive approach to compute  $a_{\mu}^{\text{HVP,LO}}$  is via the time-like formula:

$$\int_{\mu}^{\gamma} \int_{\mu}^{\mu} a_{\mu}^{\text{Hurrow}} = \left(\frac{\alpha m_{\mu}}{3\pi}\right)^2 \int_{m_{\pi^0}}^{\infty} ds \, \frac{R_{\text{had}}(s)K(s)}{s^2}, \quad K(s) = \int_{0}^{1} dx \, \frac{x^2(1-x)}{x^2 + (1-x)(s/m_{\mu}^2)}$$

• Alternatively, exchanging the x and s integrations  $\rightarrow$  space-like formula:

$$t=q^{2}<0 \qquad Hadrons \qquad a_{\mu}^{\text{HVP}} = \frac{\alpha}{\pi} \int_{0}^{1} dx (1-x) \Delta \alpha_{\text{had}}[t(x)], \quad t(x) = \frac{x^{2}m_{\mu}^{2}}{x-1} < 0$$

$$\Delta \alpha_{\text{had}} \text{ is the hadronic contribution to the running } \alpha \text{ (electromagnetic coupling constant)}$$



Running of  $\Delta \alpha_{had}$ : Time-like vs Space-like





#### $\Delta \alpha_{had}$ via Muon-electron Scattering





#### $\Delta \alpha_{had}$ via Muon-electron Scattering





#### $\Delta \alpha_{had}$ via Muon-electron Scattering





#### $\Delta \alpha_{had}$ via Muon-electron Scattering





#### Setup Overview





Setup Overview



- Correlation between muon and electron angles allows to select elastic events and reject background ( $\mu N \rightarrow \mu N e^+e^-$ ).
- Boosted kinematics:
  - Single detector to cover full acceptance
  - $\theta_{\mu} < 5 \text{ mrad}, \theta_{e} < 32 \text{ mrad}.$



#### **Apparatus** The Tracker (CMS 2S Module)

- Silicon strip sensors currently in production for the CMS-Phase 2 upgrade (HL-LHC).
- Each module is divided in two independent halves.

#### A single half:

- 1016 strips
- 5 cm long
- Divided in 8 sectors
- Each sector has independent read-out







# **Apparatus**

#### The Tracking Station





- Two (x, y) layers and (u, v) layer
  - (x, y) layers tilted by 233 mrad
  - (u, v) layer to solve reconstruction ambiguities.
- Relative position within a station must be stable at 10  $\mu$ m.
  - Low-CTE material (INVAR, carbon)
  - Cooling system + controlled temperature environment
  - Laser holographic system to monitor stability

#### **Apparatus** Calorimeter for PID



- A forward EM calorimeter (ECAL) covering part of the total acceptance for the elastic scattering.
- Useful for PID & systematic study (an independent kinematic measurement)

Transverse dim: ~ 1x1 m<sup>2</sup>

5x5 PbWO4 crystals:

- Area: 2.85x2.85 cm<sup>2</sup>
- Length: 22 cm (~25 X0).
- Total area: ~14x14 cm<sup>2</sup>.
- Readout: APD sensors.



#### T10 target ECN3 -EHN2 CERN LHC **EHN1 Neutrino Platform** EHN1 -H2, H4, H6 T2, T4, T6 targets. MUonE Prevessin site Lake (CERN's north area) SPS TT20 transfer line of Geneva BEND T6 target AL ICE Hadron Scraper (172 ± 17) GeV/c (160 ± 6) GeV/C μ 600 m 400 m **Muon Cleaning Section** Hadron Decay Section

#### Apparatus Muon (M2 beam-line) from CERN SPS Ring



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#### **Apparatus** Muon (M2 beam-line) from CERN SPS Ring



- CERN North Area M2: upstream of the COMPASS detector
  - Maximum 50 MHz (2-3×10<sup>8</sup>  $\mu$ +/spill) for 10<sup>12</sup> 400 GeV/c incident protons



# **Simulation Framework**

- NLO MonteCarlo generator: <u>MESMER</u>
  - Allows to change the muon beam energy and simulate the energy spread
- <u>'MuE'</u> fast simulation (Geant4 based)
  - Effects applied to  $(\theta_e,\,\theta_\mu)$  from the NLO generator
  - Part of detector effects (Multiple scattering) included
- <u>'FairMUonE'</u> dedicated for this project
  - Full detector effects and track reconstruction
- <u>'Combine'</u> tool for analyzing systematic effects





## Elastic Scattering Analysis 'FairMUonE' Package



- The package developed dedicated to MUonE
- Both simulation and track reconstruction in the same package
- Digitization of tracker & calo are implemented







# **Elastic Scattering Analysis**

#### **Event Selection**

- Basic criteria
  - Track candidate quality  $(\chi^2)$
  - Vertex position in the target
  - Acoplanarity
- Kinematic considerations
  - $E_{\mu(\text{beam})}$ ,  $\theta_{\mu}$ ,  $\theta_{e}$ :
    - $\theta_{\mu}$  : tune background of e<sup>+</sup>e<sup>-</sup> pairs
    - $\dot{\theta_e}$  : tune acceptance
    - $E_{\mu(\text{beam})}$  is in principle described by two angles
  - PID: muons can be distinguished from electrons using solely the angular information (a limited ambiguity region)





## Elastic Scattering Analysis Template Fit



- Extracting  $\Delta \alpha_{had}(t)$  through **a template fit** to the ( $\theta_e$ ,  $\theta_\mu$ ) distribution
- $\Delta \alpha_{\text{had}} \text{ parameterization (K, M): } \Delta \alpha_{\text{had}}(t) = KM \left\{ -\frac{5}{9} \frac{4}{3}\frac{M}{t} + \left(\frac{4}{3}\frac{M^2}{t^2} + \frac{M}{3t} \frac{1}{6}\right)\frac{2}{\sqrt{1 \frac{4M}{t}}} \ln \left| \frac{1 \sqrt{1 \frac{4M}{t}}}{1 + \sqrt{1 \frac{4M}{t}}} \right| \right\}$ 
  - 'Lepton-like' parameterization
  - K: related to  $\alpha_0$  and the electric charge of the lepton in the loop (had: quarks colour charge)
  - M: related to the squared mass of the particle in the loop  $(m_l^2, m_{\mu}^2, m_{\tau}^2)$
  - In the hadronic parameterization, K & M don't have real physical meaning

## Elastic Scattering Analysis Template Fit



- Extracting  $\Delta \alpha_{had}(t)$  through a template fit to the ( $\theta_e$ ,  $\theta_\mu$ ) distribution
- $\Delta \alpha_{had}$  parameterization (K, M):  $\Delta \alpha_{had}(t) = KM \left\{ -\frac{5}{9} \frac{4}{3}\frac{M}{t} + \left(\frac{4}{3}\frac{M^2}{t^2} + \frac{M}{3t} \frac{1}{6}\right)\frac{2}{\sqrt{1 \frac{4M}{t}}} \ln \left| \frac{1 \sqrt{1 \frac{4M}{t}}}{1 + \sqrt{1 \frac{4M}{t}}} \right| \right\}$



Preliminary template fit:

- Luminosity: 1.5x10<sup>4</sup> pb<sup>-1</sup>
- $4 \times 10^{12}$  elastic events with  $E_e > 1$ GeV ( $\theta_e < 32$  mrad)
- Input  $a_{\mu}^{HLO}$ : **688.6 × 10<sup>-10</sup>**
- Fitted  $a_{\mu}^{\text{HLO}}$ : (688.8 ± 2.4) × 10<sup>-10</sup>
- 0.35% statistical error

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# Systematic Effects

#### General Considerations

- The main challenge of the MUonE is the control of systematic effects at the same level of the stat precision
  - ~0.3% statistical accuracy on  $a_{\mu}^{\rm HVP,LO}$
  - Competitive with dispersive data-driven method
  - 3 years data-taking with full stations  $\rightarrow$  4E12 events
  - Estimated 10 ppm systematic uncertainty





#### **Systematic Effects** General Considerations

$$R_{\rm had} = \frac{d\sigma_{\rm data}(\Delta\alpha_{\rm had})}{d\sigma_{\rm MC}(\Delta\alpha_{\rm had}=0)} \sim 1 + 2\Delta\alpha_{\rm had}(t)$$

- Theory input: MC generator of radiative contributions at NNLO level
- Experimental requirements:
  - Uniform detection efficiency (modules, across all angular range)
  - Precise alignment (10  $\mu$ m longitudinally)
  - Main sources:
    - Multiple-scattering (accuracy of 1%)
    - Angular resolution (a few %)
    - Beam energy
    - ...

# Strategy



- Main systematics have large effects in the normalization region.
- Large statistics but not sensitivity to  $\Delta a_{had}$



# Systematic Effects Multiple Scattering



- Effect of  $\alpha \pm 1\%$  error on the multiple scattering core width
- Previously studied in a Beam Test in 2017 with 12–20 GeV electrons on the 8-20 mm Carbon targets: <u>G. Abbiendi et al JINST (2020) 15 P01017</u>



# Systematic Effects



- 2S modules resolution (from beam test): 8-11µm
- An effect of a ±10% error on the angular intrinsic resolution



# Systematic Effects



#### **2 Angular Intrinsic Resolution**

- 2S modules resolution (from beam test): 8-11µm
- An effect of a ±10% error on the angular intrinsic resolution
- $\theta_{\mu} > 0.4 \text{ mrad} (\theta_{e} < 20 \text{ mrad})$ gives better normalization region



## **Systematic Effects** 3 Muon Beam Energy

- Accelerator provides E<sub>beam</sub> with O(1%) precision (~ 1 GeV) → goal of **10 ppm** in the differential cross section
- The effect can also be seen in a quick data taking (~hours) for calibration





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# **Systematic Effects**

#### (4) Residual Systematics: the 'Combine' Tool

- Include residual systematics as nuisance parameters in a fit with signal.
- We can adjust the distortions in the shape of the differential cross section due to the residual systematics
  - <u>Combine tool</u> performs a likelihood fit to the nuisance parameters for each template
  - The profile likelihood as a function of K
  - Best fit value of K is determined by parabolic interpolation among the template points.
  - Nuisance parameters values for K = K<sub>best\_fit</sub>



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# **Systematic Effects**

#### (4) Residual Systematics: the 'Combine' Tool

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Selection cuts	Fit results
$\theta_e \leq 32 \mathrm{mrad}$ $\theta_\mu \geq 0.2 \mathrm{mrad}$	$K = 0.133 \pm 0.028$
	$\mu_{\rm MS} = (0.47 \pm 0.03)\%$
	$\mu_{\text{Intr}} = (5.02 \pm 0.02)\%$
	$\mu_{\rm E_{\rm Beam}} = (6.5 \pm 0.5) \mathrm{MeV}$
	$\nu = -0.001 \pm 0.003$
	(Input shifts identified correctly)
2000	





# **Test Runs** 2021 & 2022



• Intense Beam Test activities with detector in real beam conditions



2S module firstly tested on Nov 2021





1 full station (6 modules) + ECAL in the proposed MUonE location, Oct 2022

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# Test Run 2023

- 21 Aug 17 Sep (ongoing now!)
- 2 stations (pre-tracker + target + tracker) + ECAL
- Expected luminosity: ~ 1pb<sup>-1</sup>
  - ~10^{12}  $\mu$  accumulated on target with ~2.5  $\times\,10^8$  elastic events with  $E_{\rm e}\,{>}\,1$  GeV





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- 21 Aug 17 Sep (ongoing now!)
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- Expected luminosity: ~ 1pb<sup>-1</sup>
  - ~10^{12}  $\mu$  accumulated on target with ~2.5  $\times\,10^8$  elastic events  $E_{\rm e}$  > 1 GeV
- Goals:
  - Engineering stability & detectors performance
  - Background study
  - Reconstruction & prompt analysis
  - Demonstration measurement of  $\Delta \alpha^{\text{LEP}}$  with a few % precision!





# Test Run 2023



← Two stations

2S module  $\rightarrow$ 













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#### Preliminary result on scattering events!

• Runs with a 3-cm target installed

**Test Run 2023** 

- N single muons 2.9x108 in used sample (assuming no hit loss and overlap)
- One track in the 1<sup>st</sup> station + 2 tracked in the 2<sup>nd</sup> station
- Chi2/ndf track cut<5</li>
- Zvtx selection applied after selecting two outgoing tracks within the target position





#### Current Status Schedule



• TDR next year (2024)

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- The first physics run before LHC Long Shutdown (2026 2028)
  - 5 10 stations; 2- 4 months data-taking; a few % precision of  $a_{\mu}^{\text{HLO}}$
- Full run with 40 stations after LS3 with ~0.3% precision (both sys and stat)



# **Current Status**

#### The Collaboration



• 50+ people from over 9 countries. Collaboration is growing!



Liverpool (8+ people):

- 1) Data analysis
- 2) Simulation
- 3) Systematics
- 4) Mechanics
- 5) Beam Monitoring System (BMS)
- 6) Sensor dev after LS-3

# **Current Status**

#### Open to New Ideas!

- Tracker (2S module?), Calorimeter
  - Efficiency, pile-up, ...
- Mechanics

Alternative method to extract a<sup>HLO</sup>  $a_{\mu}^{HLO}$  can be written as the sum of 4 terms:  $a_{\mu}^{\text{HLO}} = a_{\mu}^{\text{HLO }(I)} + a_{\mu}^{\text{HLO }(II)} + a_{\mu}^{\text{HLO }(III)} + a_{\mu}^{\text{HLO }(IV)}$  $a_{\mu}^{\text{HLO }(I)} = -\frac{\alpha}{\pi} \sum_{n=1}^{3} \frac{c_{n}}{n!} \frac{d^{(n)}}{dt^{n}} \Delta \alpha_{had}(t) \Big|_{t}$ MUonE ~99% of a, HLO  $\overline{a_{\mu}^{\text{HLO }(II)}} = \frac{\alpha}{\pi} \frac{1}{2\pi i} \oint_{|s|=s_0} \frac{ds}{s} c_0 s \Pi_{had}(s) \Big|_{\text{pOCD}}$ Timelike  $a_{\mu}^{\text{HLO (III)}} = \frac{\alpha^2}{3\pi^2} \int_{s_{\mu}}^{s_0} \frac{ds}{s} [K(s) - K_1(s)] R(s)$ data ~1% of a<sup>HLO</sup> and pQCD  $a_{\mu}^{\text{HLO }(IV)} = \frac{\alpha^2}{3\pi^2} \int_{-\infty}^{\infty} \frac{ds}{s} [K(s) - \tilde{K}_1(s)] R(s)$ 11

Talk at Bern, 8th Sep by GV

- A new method to extract  $a_{\mu}^{\text{HLO}}$  using the same MUonE data
- Software developments (systematic effects, prompt data analysis, computing...)
- . . .
- Working towards **TDR next year**  $\rightarrow$  an important milestone
- New collaborators & ideas are welcome!

# Summary



- Muon g-2 puzzles:
  - SM predictions  $\Leftrightarrow$  Experiments
  - $e^+e^-$  data-driven method  $\Leftrightarrow$  Lattice method
  - Within data-driven method: 1) Babar  $\Leftrightarrow$  KLOE 2) CMD3  $\Leftrightarrow$  all the previous data
- MUonE: a new approach to firmer  $a_{\mu}^{\text{HVP,LO}}$  via muon-electron scattering
  - A independent determination of  $\Delta \alpha_{had}$  directly for the first time
  - Hardware & software developments with muon beam test runs ongoing
  - TDR next year (further info: <u>https://web.infn.it/MUonE/</u>)

# Backup

#### Improve the intrinsic resolution

Tilt a 2S module around an axis parallel to the strip direction.

•Charge sharing: energy deposition of particles in the Silicon is shared among adjacent strips.



•Effective staggering: tilting a 2S module by a small angle will provide two measurements which are not redundant. (i.e. 25 mrad tilt = ½pitch staggering)







#### Frontend control and readout via Serenity board (to be used in the CMS-Phase2 upgrade).

- Asynchronous beam: triggerless readout of the 2S modules @40MHz.
- Event aggregator on FPGA.
- Further data aggregation on the PC.
- Transmission to EOS into ~1GB files.



#### Laser holographic system





#### Initial state



•Compare holographic images of the same object at different times.

•Fringe pattern is related to deformations of the mechanical structure.

•Developed at INFN Trieste, tested in 2022 at CERN.

#### Thermal stability of the tracking station





Day/night variations can be reduced by installing the apparatus in a controlled environment.

# • **TB 2022: Residuals PRELIMINARY**





# **Tracker Reconstruction**



#### Production loop – reconstruction – algorithm

- 2D tracks reconstructed in X and Y projections
  - seeding with hit pairs
  - additional hits assigned based on distance from track
  - track refitted until no new hits can be added
  - clones with same sets of hits removed
  - trivial hit pairing with intended detector setup
- 3D tracks reconstructed from all pairs of X and Y tracks
  - stereo hits assigned based on distance
  - tracks with no stereo hits must have at least 3 X and Y hits
  - only tracks with stereo hits allowed with intended detector setup
  - tracks fitted and sorted based on  $\chi^2/{\rm ndf}$
  - shared hits removed from worse tracks
  - if adaptive fitter enabled, Kalman filter is ran on tracks
- linking based on deposited charge
  - $\bullet~$  full digitization  $\rightarrow$  no direct matching
  - 3 tracks with highest deposits assigned to each stub, sorted
  - reconstructed track linked to track with highest weighted sum

- for each target, all possible vertices are reconstructed
  - if enabled, also adaptive vertices
- signal vertices
  - single incoming and two outgoing tracks required (fixed number)
  - z position fixed in the middle of the target
  - kinematic fit with tracks restricted to an interaction point
  - modifies track parameters  $\rightarrow$  improved  $\theta$  angle resolution
- adaptive fitter
  - implemented for alignment using pions
  - only outgoing tracks required (at least 2, variable)
  - seeding based on distance in target, window size to be optimized
  - doesn't modify tracks, assigns Tukey weights instead
  - fits vertex position, including z

## The digitization algorithm

## 1) Primary ionization



.Start from the trajectory of a particle in a Si sens $\varphi_{dep}^{r}$  + energy deposit.

The trajectory is sampled into ionization points (10  $\mu$ m steps). An even fraction of the total energy deposit is associated to each point.

The fraction of energy deposit is converted into a charge  $(Q = E_{dep}/3.6 \text{ eV}).$ 



# The digitization algorithm



## 2) Drift

•The ionization points are drifted on the sensitive surface of the Si.

•A Gaussian charge diffusion model is applied to the ionization points.

## 3) Induce signal



 $\sigma_{drift} \propto \sqrt{\text{drift distance}}$ 

•The inonization point is expanded to a 2D cloud. The dimension depend on the drift distance.

•The total amount of charge in each strip is obtained by adding contribution from all the particles.

#### $\alpha$ running and the Vacuum Polarization

- $\blacktriangleright$  Due to Vacuum Polarization effects  $\alpha(q^2)$  is a running parameter depending on the 4momentum transfer q<sup>2</sup>
- > The "Vacuum Polarization" function  $\Pi(q^2)$  can be "absorbed" in a redefinition of an effective charge:

$$e^2 \rightarrow e^2(q^2) = \frac{e^2}{1 + (\Pi(q^2) - \Pi(0))}$$
  $\alpha(q^2) = \frac{\alpha(0)}{1 - \Delta\alpha}; \quad \Delta\alpha = -\Re e \Big( \Pi(q^2) - \Pi(0) \Big)$ 

 $\Delta \alpha = \Delta \alpha_{l} + \Delta \alpha^{(5)}_{had} + \Delta \alpha_{top}$ 

- $\succ \Delta a$  takes a contribution by non perturbative hadronic effects ( $\Delta a^{(5)}_{had}$ ) which exibits a different behaviour in time-like and space-like region
- $\geq \Delta \alpha^{(5)}_{had at}$  limits precision physics (EW fit) at M<sub>z</sub>! G. Venanzoni, Seminar at BINP, Novosibirsk 25 January 2018









#### **MUonE : signal/normalization region**





G. Venanzoni, PSI Colloquium, 28 March 2019