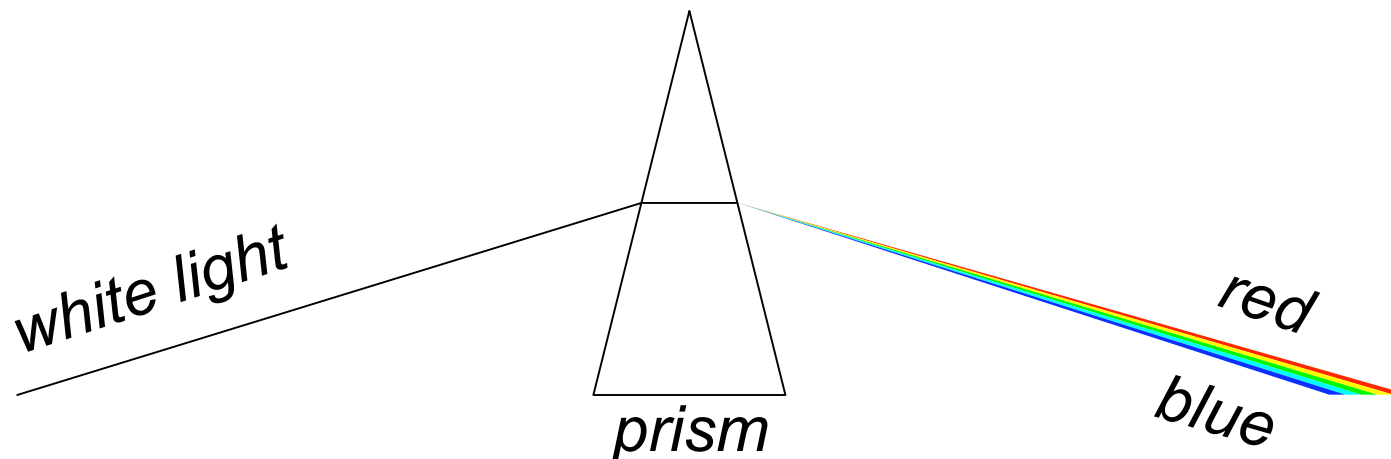


# TOPICS

- Recap of PHYS110 - *1 lecture*
- Physical Optics - *4 lectures*
  - EM spectrum and colour
  - Light sources
  - Interference and diffraction
  - Polarization
- **Lens Aberrations** - *3 lectures*
  - Spherical aberrations
  - Coma, astigmatism, field curvature, distortion
  - Chromatic aberrations**
- Instrumental Optics - *4 lectures*
  - Telescope, microscope
  - Stops, eyepieces
  - Instruments for the anterior eye
  - Instruments for the posterior eye

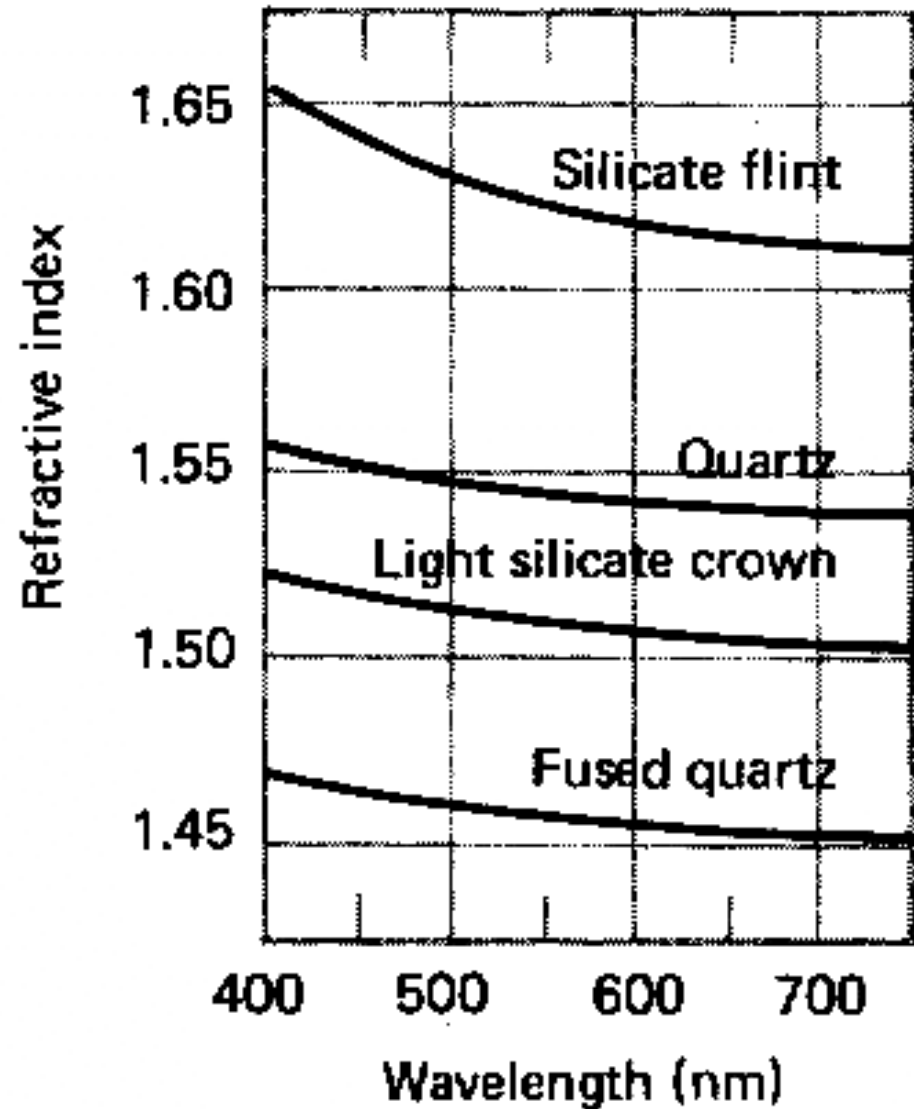
# Dispersion

- For most materials, the refractive index depends on the wavelength of the incident light
- This effect is called ***dispersion***
- Refracted light that is not monochromatic is split up into its components



# Dispersion

- Most materials have a higher refractive index for blue light (short wavelength) than for red light (long wavelength)
- Materials with a high refractive index usually have a stronger dispersion



# The dispersive index $V$

- The variation of refractive index with wavelength is characterised by the **dispersive index**  $V$ , defined as:

$$V = \frac{n_Y - 1}{n_B - n_R}$$

$n_Y$ : refractive index for yellow light ( $\lambda = 589\text{nm}$ )

$n_B$ : refractive index for blue light ( $\lambda = 486\text{nm}$ )

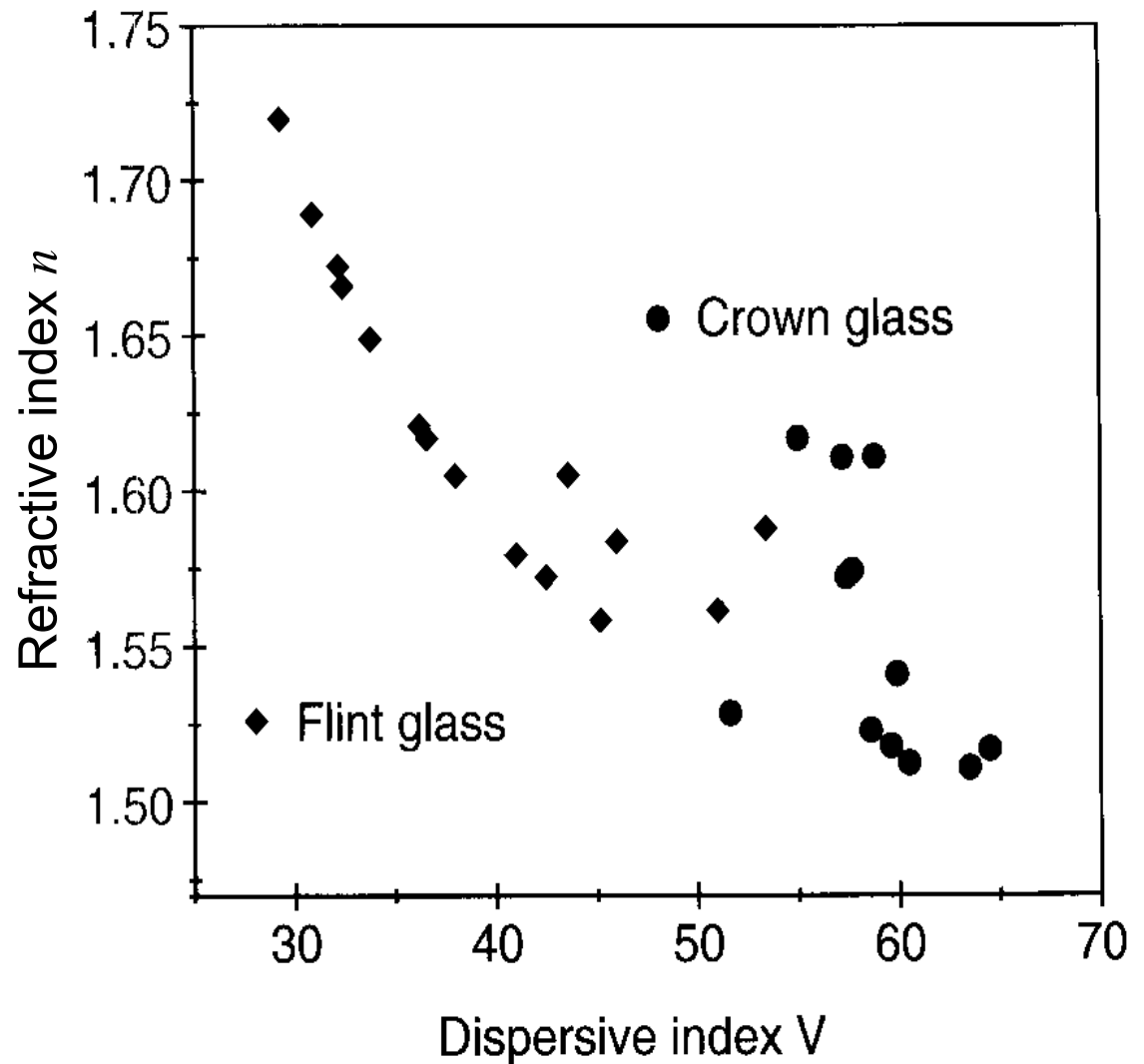
$n_R$ : refractive index for red light ( $\lambda = 656\text{nm}$ )

$\Rightarrow$  High values of  $V$  correspond to little dispersion!

$\Rightarrow$  Low values of  $V$  correspond to strong dispersion!

# The dispersive index $V$

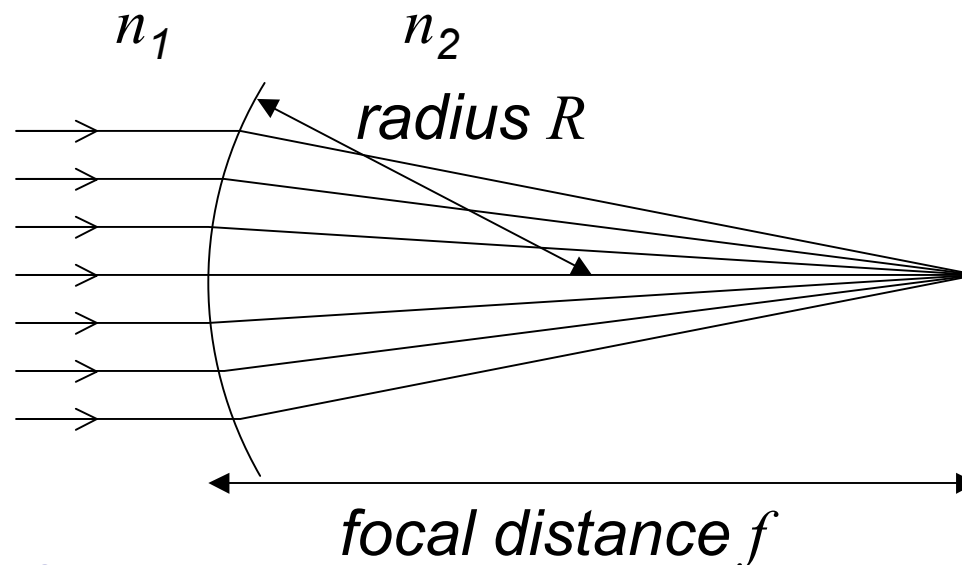
- Crown glass:
  - low refractive index  $n$
  - high value of  $V$
  - little dispersion
- Flint glass:  
(*lead glass*)
  - high refractive index  $n$
  - low value of  $V$
  - strong dispersion



# Effect of dispersion on lenses

- The vergence power  $F$  (in Dioptres) of a curved surface with radius  $R$  (in metres) going from a medium with refractive index  $n_1$  to  $n_2$  is

$$F = \frac{1}{f} = \frac{n_2 - n_1}{R}$$



# Effect of dispersion on lenses

- Example: a bi-convex lens with two surfaces with a radius of 30 cm and refractive index 1.60 for red light, has a vergence power of:

$$F = 2 \times (1.60 - 1.00) / 0.30 = 4.00 \text{ Dioptres}$$

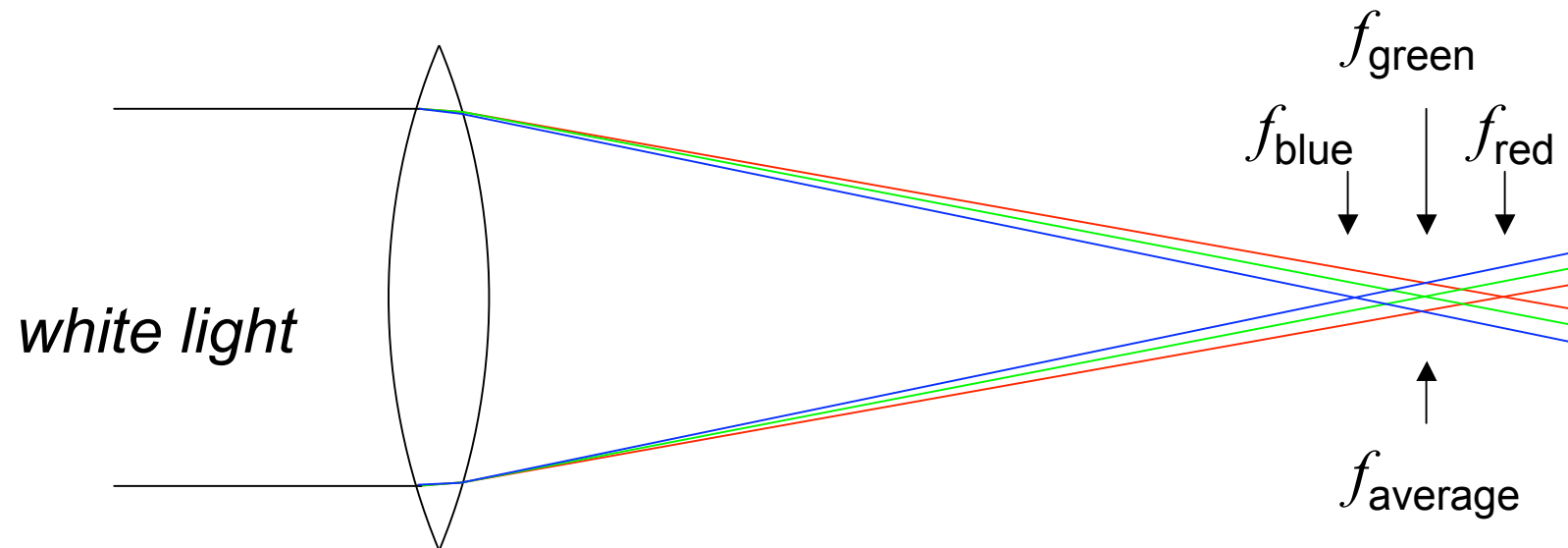
$$\text{Focal distance } f = 1/F = 1/4.00 \text{ m} = 0.250 \text{ m} = 25.0 \text{ cm}$$

- For blue light, the refractive index is 1.62.

$$F = 2 \times (1.62 - 1.00) / 0.30 = 4.13 \text{ Dioptres}$$

$$\text{Focal distance } f = 1/F = 1/4.13 \text{ m} = 0.25 \text{ m} = 24.2 \text{ cm}$$

# Longitudinal chromatic aberration



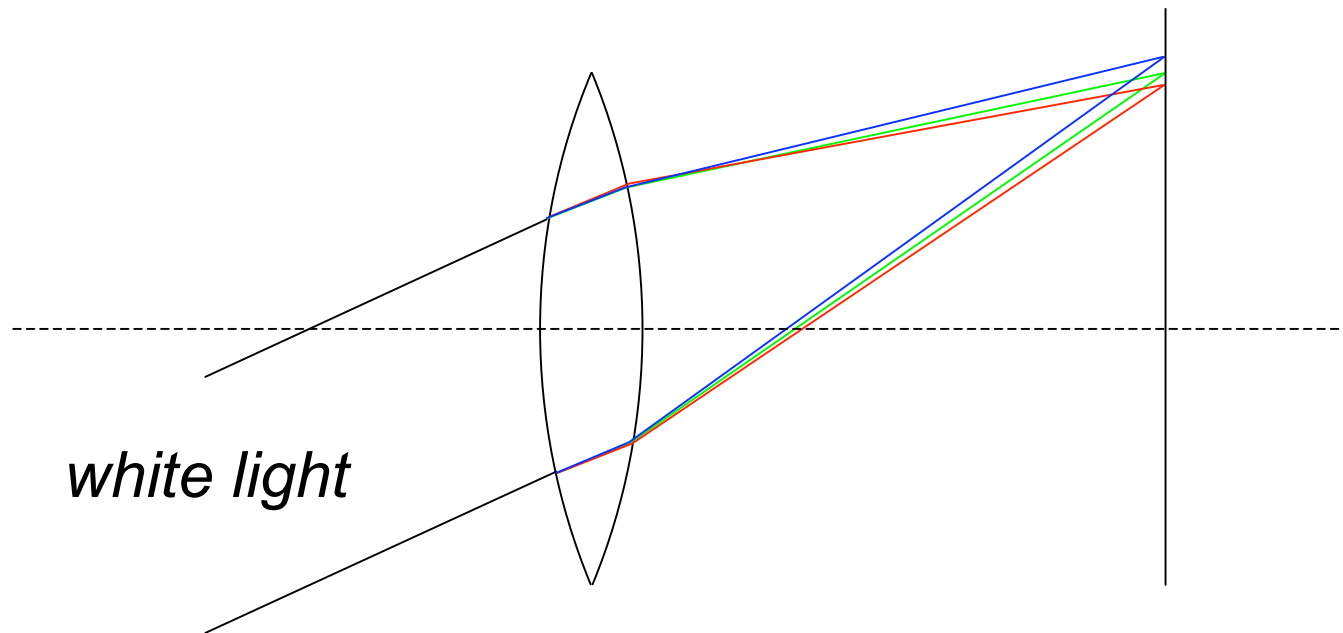
Consequence:

- blurred image
- sharpest image when using the average focal distance
- green will be sharp, but red and blue blurred



# Transverse chromatic aberrations

- In addition, off-axis objects suffer from transverse chromatic aberration as the magnification of an image varies with the wavelength.



# Transverse chromatic aberrations

- The image of an off-axis white object will have a blue rim on one side and a red rim on the other side:

*Object*



*Image*

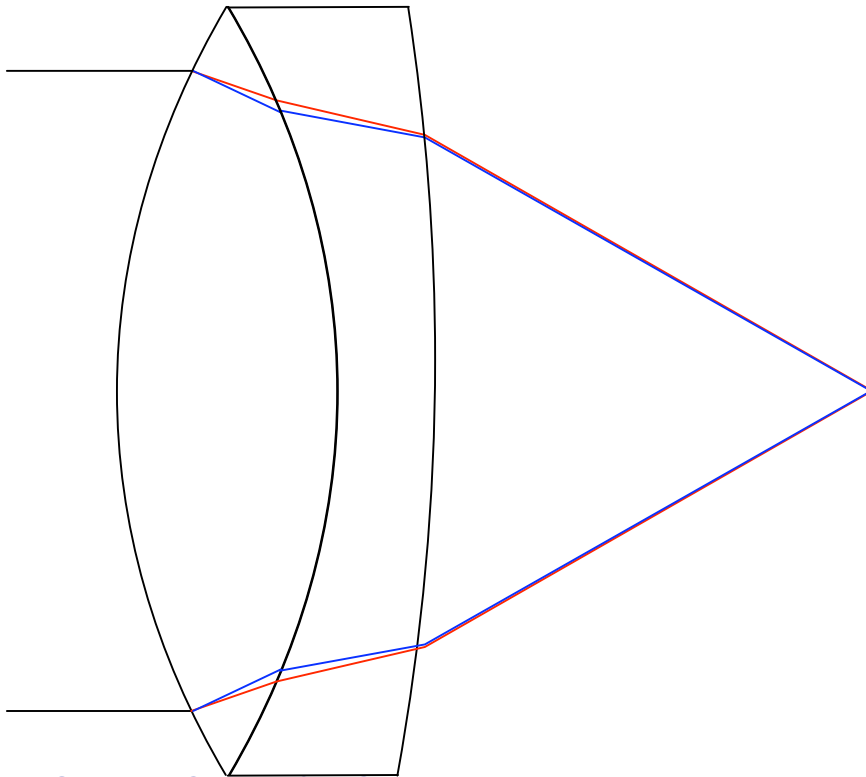


# Reducing chromatic aberrations

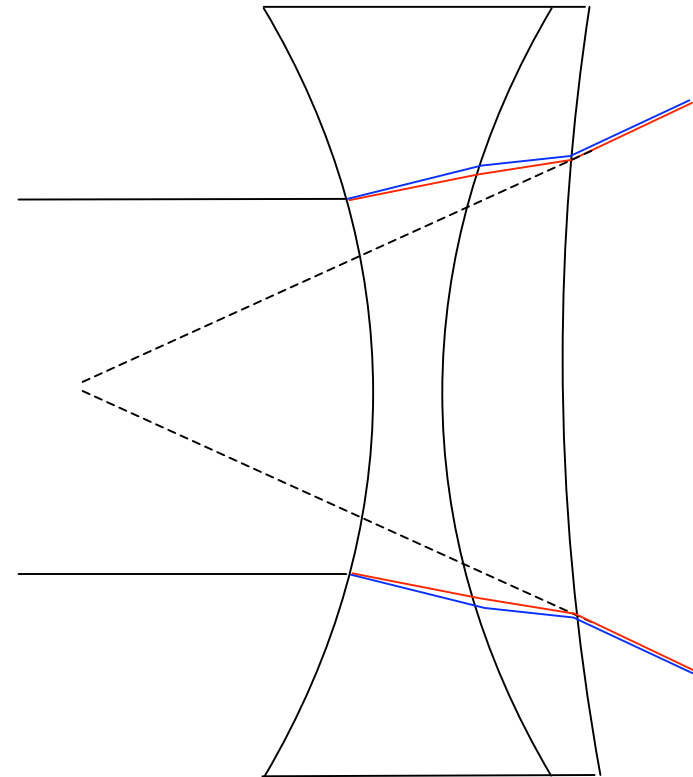
1. Using lens materials with little dispersion (high dispersion index  $V$ )
  - Relevant for single-lens systems such as spectacle glasses, magnifying glass
2. Using an achromatic doublet
  - Combine a strong lens with little dispersion and a weaker lens with strong dispersion, *of the opposite vergence power*
  - The second lens will neutralize the dispersion of the first lens while preserving most of the refractive power

# The achromatic doublet

- **Converging doublet:**
  - Strong converging lens with little dispersion
  - Weak diverging lens with strong dispersion



- **Diverging doublet:**
  - Strong diverging lens with little dispersion
  - Weak converging lens with strong dispersion



# More about achromatic doublets

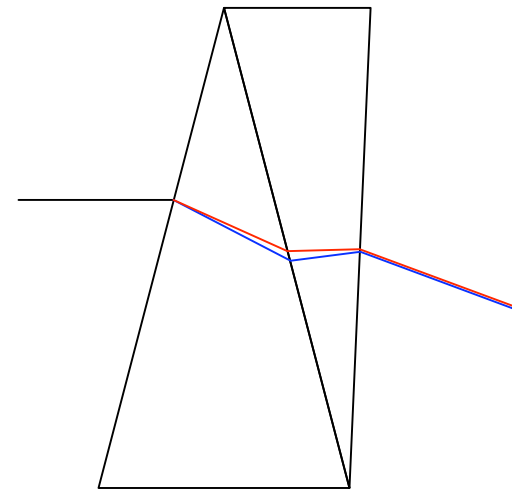
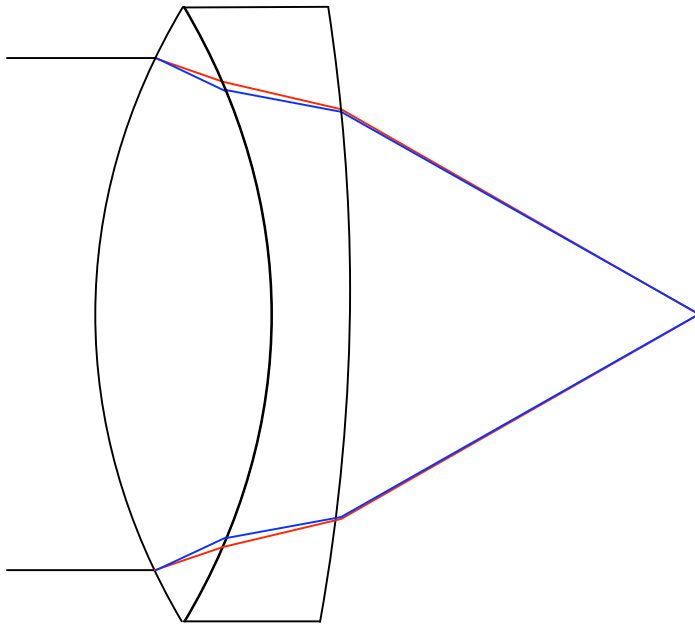
- The two lenses are usually glued (cemented) together to reduce reflections
  - The faces in common need to have the same radius of curvature
- Doublets can be designed to reduce both chromatic and spherical aberrations
- With a doublet the lens power can be made equal for two wavelengths, but small residual chromatic aberration remain for all other wavelengths
- Real optical systems often contain more than two elements to reduce all aberrations

# Achromatic prisms

- Dispersion causes chromatic effect in prisms
  - The prism power  $P$  is stronger for blue light than for red light
- For many applications of prisms, the chromatic effects are undesirable
- The methods used for achromatic lenses also apply to achromatic prisms:
- An achromatic doublet can be made by combining a strong prism with little dispersion and a weaker prism with high dispersion, *with the opposite orientation*

# The achromatic doublet

- Lens:
  - Strong converging lens with little dispersion
  - Weak diverging lens with strong dispersion
- Prism:
  - Strong prism with little dispersion
  - Weak prism with strong dispersion *with the opposite orientation*



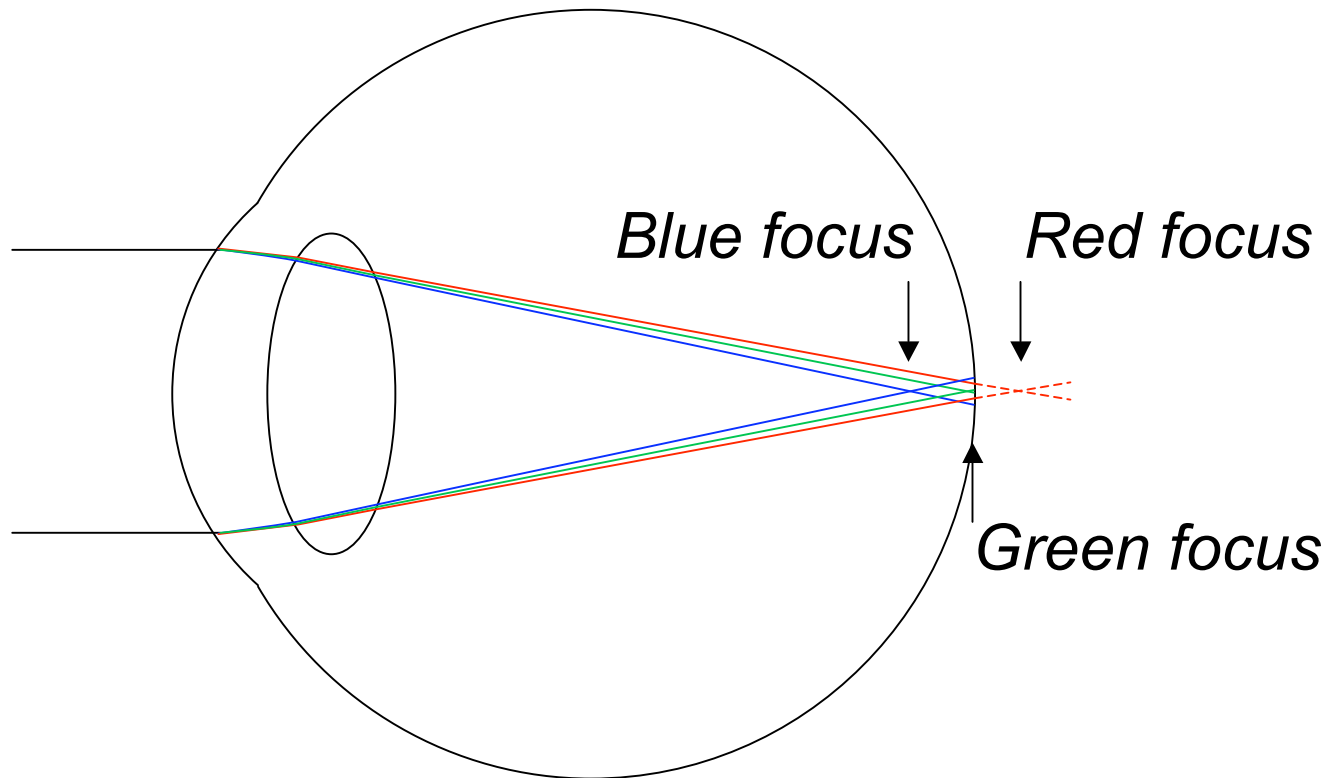
# Chromatic aberration in the Eye.

- In the eye, the focal length is shorter for blue than for red light.
- Spread in power from blue to red is approximately 2 Dioptres.
- For an emmetropic eye, the centre of spectrum (yellow-green) is focused on the retina.
- Blue light is focused in front of the retina, red light behind the retina.



# Chromatic aberration in the Eye.

## Emmetropic eye:

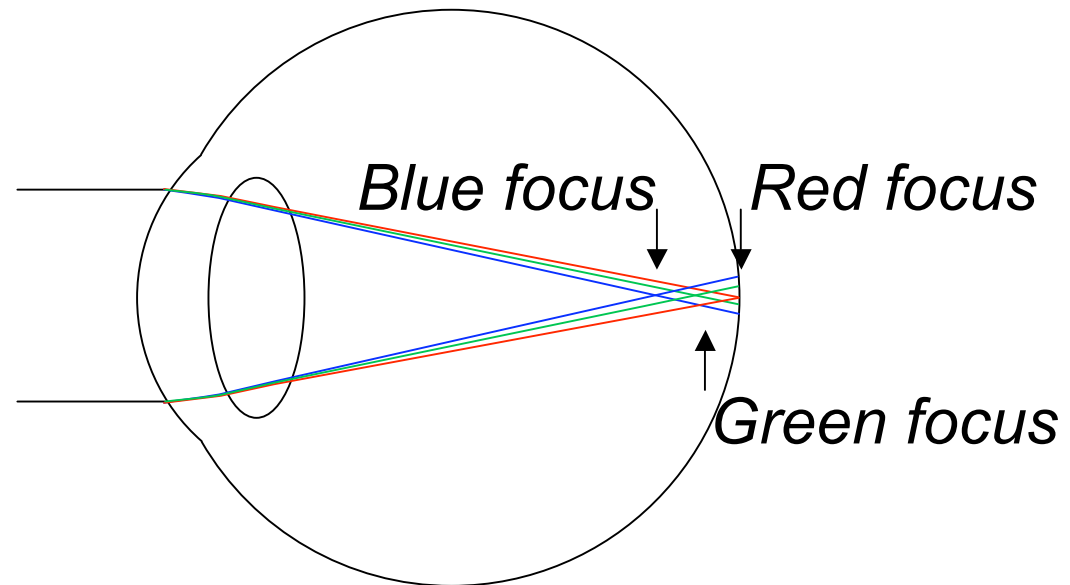


# Chromatic aberrations & ametropia

## Myopic eye:

*(near-sighted)*

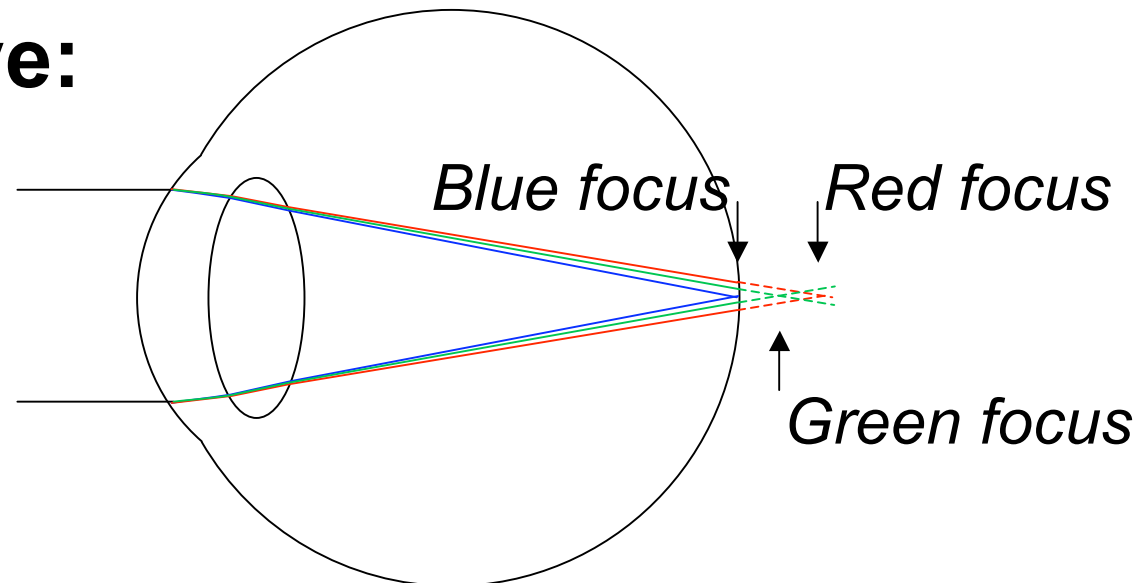
sees red sharper  
than blue



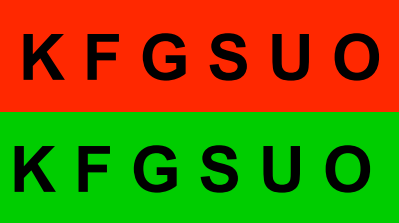
## Hypermetropic eye:

*(far-sighted)*

sees blue sharper  
than red



# The Duochrome test:

- Uses chromatic aberrations to detect myopia
  - Two sets of black letters:
    - one set with red background
    - one set with green background
- 
- The image shows two horizontal bars. The top bar has a red background and contains the black letters 'K F G S U O' in a sans-serif font. The bottom bar has a green background and contains the same black letters 'K F G S U O' in the same font.
- A myopic patient will see letters on the red background more clearly
  - A hypermetropic patient will see letters on the green background more clearly
  - A corrected eye should see both sets of letters with equally clarity
  - *NB1: Green is used instead of blue, which is a poorly perceived colour*
  - *NB2: Duochrome test is valid even for colour-blind patients*