



# A measurement and QCD analysis of the proton structure function $F_2(x, Q^2)$ at HERA

H1 Collaboration

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## Abstract

A new measurement of the proton structure function  $F_2(x, Q^2)$  is reported for momentum transfers squared  $Q^2$  between 1.5 GeV<sup>2</sup> and 5000 GeV<sup>2</sup> and for Bjorken  $x$  between  $3 \cdot 10^{-5}$  and 0.32 using data collected by the HERA experiment H1 in 1994. The data represent an increase in statistics by a factor of ten with respect to the analysis of the 1993 data. Substantial extension of the kinematic range towards low  $Q^2$  and  $x$  has been achieved using dedicated data samples and events with initial state photon radiation. The structure function is found to increase significantly with decreasing  $x$ , even in the lowest accessible  $Q^2$  region. The data are well described by a Next to Leading Order QCD fit and the gluon density is extracted.

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## 1. Introduction

A prime task of the electron-proton collider HERA is the investigation of the structure of the proton. Measurements of the inclusive lepton-proton scattering cross section have been crucial for the understanding of proton substructure [1]. Early electron-proton scattering experiments have discovered pointlike proton constituents by observing a scale invariant dependence of the proton structure function  $F_2(x, Q^2)$  on the four-momentum transfer squared  $Q^2$  at Bjorken  $x \geq 0.1$  and  $Q^2$  values of about  $5 \text{ GeV}^2$ . Subsequent neutrino scattering experiments have established the Quark Parton Model (QPM) as a valid picture of the valence and sea quarks as constituents of the proton. The interaction of these partons as mediated by gluons is successfully described by Quantum Chromodynamics (QCD) which has been tested with high precision in muon-nucleon deep-inelastic scattering (DIS) experiments. Experiments at HERA extend the previously accessible kinematic range up to very large squared momentum transfers,  $Q^2 > 10^3 \text{ GeV}^2$ , and down to very small values of Bjorken  $x < 10^{-4}$ .

The first measurements of the structure function  $F_2(x, Q^2)$  reported at HERA, based on data collected in 1992, revealed its strong rise at low  $x < 10^{-2}$  with decreasing  $x$  [2,3]. This rise was confirmed with the more precise data of 1993 [4,5], based on an order of magnitude increase in statistics. Such a behaviour is qualitatively expected in the asymptotic limit of Quantum Chromodynamics [6]. It is, however, not clear whether the rise of  $F_2$  is fully described by the linear QCD evolution equations, such as the conventional DGLAP evolution [7] in  $\log Q^2$  or by the BFKL evolution [8] in  $\log(1/x)$ , or whether there is a significant effect due to non-linear parton recombination [9]. Furthermore, it is also unclear whether this rise will persist at low values of  $Q^2$  of the order of one  $\text{GeV}^2$ . For example, Regge inspired models expect  $F_2$  to be rather flat as function of  $x$  at small  $Q^2$ . The quantitative investigation of the quark-gluon interaction dynamics at low  $x$  is one of the major challenges at HERA. It requires high precision for the  $F_2$  measurement and complementary investigations of the characteristics of the hadronic final state [10].

In this paper an analysis is presented of inclusive deep-inelastic scattering data taken by the H1 Collaboration in 1994 with an integrated luminosity of  $2.7 \text{ pb}^{-1}$ , which is an order of magnitude larger than in 1993. The incident electron<sup>13</sup> energy  $E_e$  was  $27.5 \text{ GeV}$  and the proton energy  $E_p$  was  $820 \text{ GeV}$ . The accessible kinematic range has been extended to the very high  $Q^2$  region and the structure function  $F_2$  has been investigated at a new level of precision. To reach lower  $Q^2$  values and correspondingly lower  $x$  values, special samples were analysed of events with shifted interaction vertex, and of events with tagged initial state photon radiation.

This paper is organized as follows. After a short introduction to the kinematics of inclusive  $ep$  scattering (Section 2), the H1 apparatus is briefly sketched (Section 3). The different 1994 data samples, the luminosity determination and the Monte Carlo

<sup>13</sup> HERA operated with  $e^-p$  collisions in 1992, 1993 and the start of 1994, and  $e^+p$  collisions for the major part of 1994. In this paper the incident and scattered lepton will always be referred to as an "electron".

simulation are described in Section 4. Next the event selection including the background rejection (Section 5) is discussed for the different data samples used. Section 6 describes the  $F_2$  analyses. In Section 7 the results are discussed. A phenomenological analysis of  $F_2$  is performed and the data are compared to recent model calculations at low  $Q^2$ . The data are also studied in the framework of perturbative QCD and the gluon distribution is extracted. The paper is summarized in Section 8.

## 2. Kinematics

The structure function  $F_2(x, Q^2)$  is derived from the inclusive electron-proton scattering cross section. It depends on the squared four-momentum transfer  $Q^2$  and the scaling variable  $x$ . These variables are related to the inelasticity parameter  $y$  and to the total squared centre of mass energy of the collision  $s$  since  $Q^2 = xys$  with  $s = 4E_e E_p$ . A salient feature of the HERA collider experiments is the possibility of measuring not only the scattered electron but also the complete hadronic final state, apart from losses near the beam pipe. This means that the kinematic variables  $x$ ,  $y$  and  $Q^2$  can be determined with complementary methods which are sensitive to different systematic effects. These methods were exploited and detailed already in [4] which describes the analysis of the 1993 data. An appropriate combination of the results ensures maximum coverage of the available kinematic range.

The methods used in the analysis of the 1994 data are the so-called “E” (electron) method using only the information of the scattered electron and the so-called “ $\Sigma$ ” method calculating the kinematics based on both the scattered electron and the hadronic final state measurements [11]. The E method, which is independent of the hadronic final state, apart from the requirement that the interaction vertex is reconstructed using the final state hadrons, has at large  $y$  the best resolution in  $x$  and  $Q^2$  but needs sizeable radiative corrections. At low  $y$  the E method is not applied due to the degradation of the  $y_e$  resolution as  $1/y$ . The  $\Sigma$  method, which has small radiative corrections, relies mostly on the hadronic measurement which has still an acceptable resolution at low  $y$  values and can be used from very low to large  $y$  values. The E and  $\Sigma$  results were compared in order to control the calculation of the systematic errors. The basic formulae for  $Q^2$  and  $y$  for the E method are

$$y_e = 1 - \frac{E'_e}{E_e} \sin^2 \frac{\theta_e}{2}, \quad Q_e^2 = 4E'_e E_e \cos^2 \frac{\theta_e}{2} = \frac{E_e'^2 \sin^2 \theta_e}{1 - y_e}, \quad (1)$$

where  $E'_e$  and  $\theta_e$  are the energy and polar angle of the scattered electron. The polar angle  $\theta_e$  is defined with respect to the proton beam or  $z$  direction, termed “forward” region. The formulae for the  $\Sigma$  method are

$$y_\Sigma = \frac{\Sigma}{\Sigma + E'_e(1 - \cos \theta_e)}, \quad Q_\Sigma^2 = \frac{E_e'^2 \sin^2 \theta_e}{1 - y_\Sigma} \quad (2)$$

with

$$\Sigma = \sum_h (E_h - p_{z,h}). \quad (3)$$

Here  $E_h$  and  $p_{z,h}$  are the energy and longitudinal momentum component of a particle  $h$ , the summation is over all hadronic final state particles and the masses are neglected. The denominator of  $y_\Sigma$  is equal to  $2E_e$  but measured with all secondary particles. Thus

$$y_\Sigma = \frac{y_h}{1 + y_h - y_e} \quad (4)$$

with the standard definition

$$y_h = \frac{\Sigma}{2E_e}. \quad (5)$$

The variable  $x$  is calculated as  $x = Q^2/ys$ .

### 3. The H1 detector

The H1 detector [12] is a nearly hermetic multi-purpose apparatus built to investigate the inelastic high-energy interactions of electrons and protons at HERA. The structure function measurement relies essentially on the inner tracking chamber system and on the backward electromagnetic and the liquid argon calorimeters which will be described here briefly.

The tracking system includes the central tracking chambers, the forward tracker modules and a backward proportional chamber. These chambers are placed around the beam pipe at  $z$  positions between  $-1.5$  and  $2.5$  m. A superconducting solenoid surrounding both the tracking system and the liquid argon calorimeter provides a uniform magnetic field of 1.15 T.

The central jet chamber (CJC) consists of two concentric drift chambers covering a polar angle range from  $15^\circ$  to  $165^\circ$ . Tracks crossing the CJC are measured with a transverse momentum resolution of  $\delta p_T/p_T < 0.01 \cdot p_T/\text{GeV}$ . The CJC is supplemented by two cylindrical drift chambers at radii of 18 and 47 cm, respectively, to improve the determination of the  $z$  coordinate of the tracks. A proportional chamber is attached to each of the  $z$  drift chambers for triggering.

A tracking chamber system made of three identical modules measures hadrons emitted in the forward direction ( $7^\circ$  to  $20^\circ$ ). The forward tracker (FT) is used to determine the vertex for the events which leave no track in the CJC. This allows an extension of the analysis to larger  $x$  values.

In the backward region, attached to the backward electromagnetic calorimeter (BEMC), a four plane multiwire proportional chamber (BPC) was located with a polar angle acceptance of  $151^\circ$  to  $174.5^\circ$ . The BPC provides a space point for charged particles entering the BEMC which is used for low  $Q^2 \leq 120 \text{ GeV}^2$  events to identify electrons and to measure  $\theta_e$ . The spatial resolution for reconstructed BPC hits is about 1.5 mm in the plane perpendicular to the beam axis.

The backward electromagnetic calorimeter [13] which detects the scattered electron at low  $Q^2$  is made of 88 lead/scintillator stacks with a size of  $16 \times 16 \text{ cm}^2$  and a depth of 22 radiation lengths corresponding to about one interaction length. Around the beampipe the stacks are of triangular shape. The angular coverage of the BEMC is  $155^\circ < \theta_e < 176^\circ$ . A 1.5 cm spatial resolution of the lateral shower position is achieved using four photodiodes which detect the wavelength shifted light from each of the scintillator stacks. A scintillator hodoscope (TOF) situated behind the BEMC is used to veto proton-induced background events based on their early time of arrival compared with nominal  $ep$  collisions.

Hadronic final state energies and the scattered electron at high  $Q^2$  ( $Q^2 \geq 120 \text{ GeV}^2$ ) are measured in the liquid argon (LAR) calorimeter [14] which covers an angular region between  $3^\circ$  and  $155^\circ$ . The calorimeter consists of an electromagnetic section with lead absorber plates and a hadronic section with stainless steel absorber plates. Both sections are highly segmented in the transverse and longitudinal directions with about 44000 cells in total. The electromagnetic part has a depth between 20 and 30 radiation lengths. The total depth of both calorimeters varies between 4.5 and 8 interaction lengths.

The luminosity was determined from the measured cross section of the Bethe-Heitler (BH) reaction  $ep \rightarrow epy$ . The final state electron and photon can be detected in calorimeters (electron and photon “taggers”) close to the beam pipe but at large distances from the main detector (at  $z = -33 \text{ m}$  and  $z = -103 \text{ m}$ ).

## 4. Data and Monte Carlo samples

### 4.1. Data samples

Several data samples have been analysed in order to cover maximally the kinematic plane. The distribution of the events is shown in Fig. 1. The majority of the events are produced with the interaction vertex centered around zero in  $z$ , called the “nominal vertex” sample (shown as regions C and D in Fig. 1). Throughout this paper, the low (high)  $Q^2$  sample refers to events in which the scattered electron has been detected in the BEMC (LAR calorimeter). To reduce the systematic errors of the  $F_2$  measurement, a strict data selection was performed based on the behaviour of the main detector components. This behaviour was required to be optimal for the low  $Q^2$  analysis of the nominal vertex sample which allows the highest precision to be reached. The remaining integrated luminosity for the low  $Q^2$  sample is  $2.2 \text{ pb}^{-1}$ , the one for the high  $Q^2$  sample is  $2.7 \text{ pb}^{-1}$ . The number of accepted events per unit luminosity was checked to be constant within statistical errors during the data taking period.

In order to study the behaviour of  $F_2$  at small  $Q^2$  several means were used to extend the acceptance to this kinematic region using special event samples. For DIS events at very low  $Q^2$  the electron is scattered through a large angle  $\theta_e$ . For  $\theta_e$  values greater than  $173^\circ$  and the interaction vertex at its nominal position at  $z = +3 \text{ cm}$  the electron hits the inner edge of the BEMC calorimeter or remains undetected near the beam pipe.



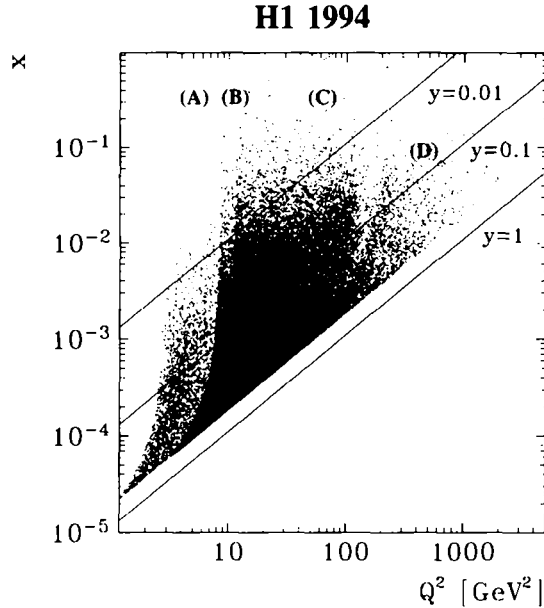


Fig. 1. Distribution of the event sample in the  $(x, Q^2)$  plane. The four visible regions (A, B, C, D) correspond to (A) events recorded during a period in which the interaction region was shifted with respect to the nominal position allowing access to larger  $\theta_e$ ; (B) events from the nominal vertex position taken in a period in which the innermost BEMC stacks of triangular shape were included in the trigger (“opened triangles”, see text) or (C) not included; (D) high  $Q^2$  events with the scattered electron detected in the LAr calorimeter.

The acceptance extension in the backward region was realized as follows:

- During good accelerator background conditions, the innermost parts of the backward electromagnetic calorimeter (BEMC) around the beampipe were included in the trigger for part of the time. Since these detector elements are of triangular shape, these data will be referred to as the “open triangle” data sample. An integrated luminosity of  $0.27 \text{ pb}^{-1}$  was accumulated. The kinematic region covered by this sample is shown as region (B) in Fig. 1.
- As in 1993 [4], the interaction point was shifted in the forward direction to an average position of  $z = +67 \text{ cm}$  which permits measurements up to  $\theta_e \simeq 176.5^\circ$ . This sample of  $58 \text{ nb}^{-1}$  of data is referred to as the “shifted vertex” data sample to distinguish it from the data with a nominal event vertex. It covers region (A) in Fig. 1.
- The low  $Q^2$  region was also accessed by analyzing events from the so-called early proton satellite bunch colliding with an electron bunch at  $z \simeq +68 \text{ cm}$ . The kinematic region covered by this sample is similar to that of the shifted vertex data sample. The “satellite” data sample amounts to  $\simeq 3\%$  of the total data corresponding to a total “luminosity” of  $68 \text{ nb}^{-1}$  selected over the whole run period.
- Finally, a sample of deep-inelastic radiative events was extracted with a hard photon emitted collinear with the incident electron. These events have a reduced incident electron beam energy which allows access to very low  $Q^2$  values with the present detector setup. Since only about 2% of the DIS events are tagged as radiative events,

the nominal vertex sample had to be used for this study. Subsequently the tagged radiative events are referred to as “the radiative event sample” and the bulk of the data are sometimes called “non-radiative” in contrast.

#### 4.2. Luminosity determination

The most precise method of determining the luminosity from the reaction  $ep \rightarrow ep\gamma$  is based on the measurement of the energy spectrum of hard photons ( $E_\gamma > 10$  GeV) as explained in [15] for the 1993 data. The main uncertainties of the measurement of the integrated luminosity for the 1994 nominal vertex data are: the photon tagger absolute energy scale (0.9%), the trigger efficiency of the luminosity system (0.3%), the precision of the electron gas background subtraction (0.4%), the photon-tagger acceptance (0.5%), multiple photon overlaps (0.4%), the precision of integration resulting from the 10 sec interval between consecutive luminosity measurements (0.5%) and the correction for satellite bunches (0.5%). Major improvements with respect to 1993 data include the trigger efficiency, the satellite bunch correction and the precision of the energy scale in the photon tagger. The precision of the luminosity measurement for the nominal vertex data sample is 1.5% which represents an improvement of a factor of 3 with respect to the 1993 data analysis. For the shifted vertex data sample the luminosity uncertainty is 3.9%.

The results of this measurement were checked for consistency with a sample of Bethe–Heitler events in which both the electron and photon are detected simultaneously, and with QED Compton events. Both these analyses are subject to different systematics, compared with the hard photon method, allowing a cross check of the luminosity with a precision of up to 6%.

The integrated luminosity of the satellite data sample was obtained from the measured integrated luminosity for the shifted vertex data multiplied by the efficiency corrected event ratio in a kinematic region common to both data sets. The precision of that luminosity determination was estimated to be 7.1%.

#### 4.3. Monte Carlo simulation

More than one million Monte Carlo DIS events were generated using the DJANGO [16] program. The Monte Carlo event statistics correspond to an integrated luminosity of approximately  $18 \text{ pb}^{-1}$ . The DJANGO program is based on HERACLES [17] for the electroweak interaction and on the LEPTO program [18] to simulate the hadronic final state. HERACLES includes first order radiative corrections, the simulation of real Bremsstrahlung photons and the longitudinal structure function. The acceptance corrections were performed using the GRV parametrization [19] which describes rather well the HERA  $F_2$  results based on the 1993 data. LEPTO uses the colour dipole model (CDM) as implemented in ARIADNE [20] which is in good agreement with data on the energy flow and other characteristics of the final state as measured by H1 [21] and

ZEUS [22]. For the determination of systematic errors connected with the topology of the hadronic final state, the HERWIG model [23] was used.

Photoproduction background was simulated based on the PHOJET [24], PYTHIA [25] and RAYVDM [26] generators for  $\gamma p$  interactions. With these models large samples of photoproduction events were generated which contained all classes of events (elastic, soft hadronic collisions, hard scattering processes and heavy flavour production).

It was found that about 10% of the DIS data at HERA consists of events with a large gap in pseudo-rapidity around the proton remnant direction [27]. These events were found to be compatible with diffractive exchange and are well described by the model RAPGAP [28] as deep-inelastic scattering on a colourless object – termed a pomeron – emitted from the proton. The hadronic final state of these events is also well described by RAPGAP which includes ARIADNE for QCD effects. The RAPGAP Monte Carlo simulation was used to check the effect of the large rapidity gap events on the vertex reconstruction efficiency which depends mostly on the final state topology of the events. Differences between rapidity gap and “standard” DIS events of up to 2% were found at large  $y > 0.4$  and smaller at low  $y$ , and were included in the systematic error of  $F_2$ .

For the events generated with the models described above the detector response was simulated in detail [12] using a program based on GEANT [29]. The simulated Monte Carlo events were subjected to the same reconstruction and analysis chain as the real data.

## 5. Event selection

The low  $Q^2$  DIS events in the backward region were triggered by an energy cluster in the BEMC ( $E'_e > 4$  GeV) which was not vetoed by the TOF. The high  $Q^2$  events were triggered by requiring an electromagnetic energy cluster in the LAr calorimeter ( $E'_e > 8$  GeV). A trigger of lower energy threshold ( $E'_e > 6$  GeV) also accepted the event if there was simultaneously a tracking trigger. In the region of the final  $F_2$  data presented below the trigger efficiency, which has been determined from the data, is about 80% for  $E'_e \sim 8$  GeV, and becomes larger than 99% for  $E'_e > 10$  GeV.

### 5.1. Selection of deep-inelastic scattering events

Deep-inelastic scattering events in H1 are identified by the detection of the scattered electron in the BEMC or LAr calorimeter and the presence of a reconstructed interaction vertex. The electron identification cuts, fiducial volume and vertex requirement are detailed in Table 1.

These selection criteria follow closely those of the 1993 data analysis [4]. For the low  $Q^2$  nominal vertex sample ( $Q^2 \leq 120$  GeV<sup>2</sup>) an additional cut  $r_{\text{BPC}} < 64$  cm is applied, where  $r_{\text{BPC}}$  is the radial distance of the electron hit in the BPC to the beam axis. This cut prevents the electron from entering the transition region between the BEMC and the LAr

Table 1

Summary of event selection criteria for the shifted and the nominal vertex (vtx) data at low and high  $Q^2$ . The approximate event numbers are 10000, 220000 and 9000 events respectively. For the open triangle data sample the  $\theta_e$  cut is  $174^\circ$ . For the electron identification several estimators were used:  $\epsilon_1$ : electron cluster radius;  $\epsilon_2$ : smallest distance from the closest hit in the BPC to the centroid of the electron cluster;  $\epsilon_3$ : fraction of the electron energy deposited in the four most energetic cells of the cluster;  $\epsilon_4$ : fraction of the electron energy deposited in the first three radiation lengths of the calorimeter;  $\epsilon_5$ : angle between the line connecting the vertex to the centroid of the electron cluster and the associated track.

	Low $Q^2$ (shifted vtx)	Low $Q^2$ (nominal vtx)	high $Q^2$	
	E, $\Sigma$ method	E, $\Sigma$ method	E method	$\Sigma$ method
$\theta_e / ^\circ$	$\leq 176$	$< 173$	$< 150$	$\leq 153$
$E'_e / \text{GeV}$	$> 11$	$> 11$	$> 11$	$> 11$
$z_{\text{vertex}} / \text{cm}$	$67 \pm 30$	$5 \pm 30$	$5 \pm 30$	$5 \pm 30$
electron identif.	$\epsilon_1 < 5 \text{ cm}$	$\epsilon_1 < 5 \text{ cm}$	$\epsilon_3 > 50\%$	$\epsilon_3 > 65\%$
electron identif.	$\epsilon_2 < 5 \text{ cm}$	$\epsilon_2 < 5 \text{ cm}$	$\epsilon_4 > 3\%$	$\epsilon_5 < 30 \text{ mrad}$

calorimeter where the energy corrections are large and depend strongly on the impact point. For the same reason, the high  $Q^2$  events ( $Q^2 > 120 \text{ GeV}^2$ ) are accepted only if the electron cluster is fully contained in the LAr calorimeter. Despite these conditions, the measurement could also be performed for intermediate  $Q^2$  ( $Q^2 \sim 120 \text{ GeV}^2$ ) due to the  $\pm 30 \text{ cm}$  spread of the event vertex position around its nominal position.

The scattered electron is identified with the electromagnetic cluster of maximum energy which satisfies the estimator cuts of Table 1. The electron identification efficiency, determined from Monte Carlo simulation studies, is better than 97% except at  $Q^2 \leq 6.5 \text{ GeV}^2$  where it falls to 94% at the lowest  $x$  values.

At low  $Q^2$  the main sources of non- $ep$  background are due to proton beam interactions with residual gas and beam line elements upstream of the H1 detector. At high  $Q^2$  the main background is due to cosmic ray events and muons travelling off axis parallel to the proton beam. An efficient reduction of these background contributions is provided by the minimum energy and the vertex requirements discussed above. The number of residual beam-induced background events was estimated from non-colliding bunch studies, and the number of cosmic events from scanning. Both together represent less than 1% of the number of selected events in any  $(x, Q^2)$  bin.

The only significant background to DIS from  $ep$  interactions is due to photoproduction events where the scattered electron escapes the detector along the beam pipe but in which an energy cluster from the hadronic final state fakes a scattered electron. About 10% of these events are identified as photoproduction background if the scattered electron is found in the electron tagger. Photoproduction events were simulated to estimate this background. The photoproduction background was subtracted statistically bin by bin. Only 12 bins, out of a total of 193  $(x, Q^2)$  bins, have a contamination larger than 3%. This contamination never exceeds 15% in any bin.

Fig. 2a shows the distribution of the angle of the scattered electron for the shifted vertex data compared to the Monte Carlo simulation weighted with the measured structure function (see Section 6). The Monte Carlo simulation is normalized to the luminosity

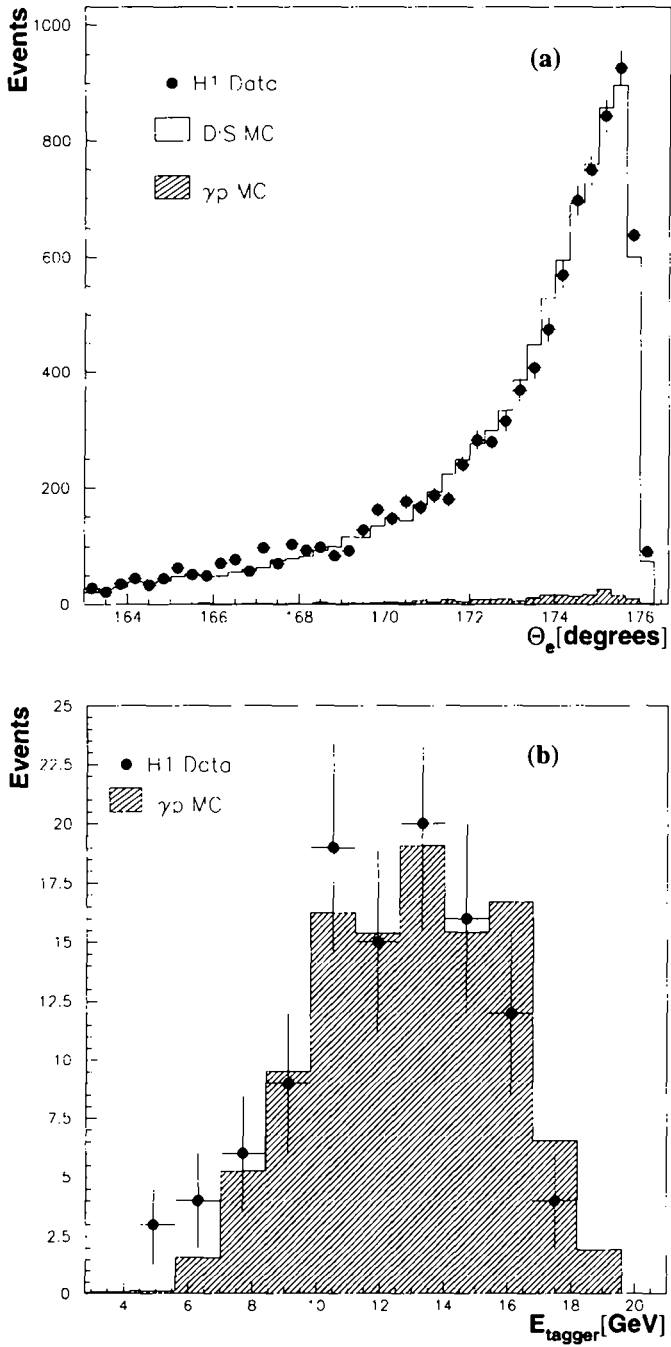


Fig. 2. Shifted vertex data: experimental and Monte Carlo distributions of (a) the polar angle of the scattered electron and (b) the energy of the scattered electron in photoproduction background events detected in the electron tagger.

and agrees well with the data illustrating the level of residual background in the low  $Q^2$  sample. In Fig. 2b the normalized energy spectrum in the electron tagger is shown which is reasonably reproduced by the background photoproduction event simulation.

Fig. 3a shows the distribution of the energy of the scattered electron for the high statistics nominal vertex data. The simulation gives an excellent description of the data from the low energy up to the so-called kinematic peak region, i.e. the region around the value of the incident electron beam energy. This agreement was achieved after a spatially dependent calibration of the data and Monte Carlo response [30] using the double-angle method [31]. The small remaining contribution of the photoproduction background is also shown. In Fig. 3b the fractions of  $y_h$  originating from tracks, BEMC and LAr calorimeter are given as a function of  $\log_{10} y_h$ . In this analysis the  $y_h$  variable is determined by using a combination of central tracks and calorimeter cells [32]. An isolation criterion is used to avoid counting the energy of the LAr cells originating from a track already used in  $y_h$ . For  $y < 0.15$ , i.e. in the region where the  $\Sigma$  method will be used for the  $F_2$  result, the measurement is dominated by the track reconstruction and the LAr measurement (Fig. 3b). At larger  $y$ , the BEMC contribution plays an increasing role due to the low energy particles which accumulate in the backward direction. The DIS Monte Carlo simulation describes well these fractions in the complete kinematic range.

Fig. 4a shows the distribution of the energy of the scattered electron detected in the LAr calorimeter. It is well described by the Monte Carlo simulation. A detailed calibration was carried out by comparing events from the kinematic peak at low  $y$  ( $< 0.1$ ) with simulation, including corrections for the energy lost due to the dead material between the wheels which make up the LAr calorimeter [33]. This procedure has been cross checked with the double-angle method.

Fig. 4b shows the ratio  $y_{\Sigma}/y_e$  in the high  $Q^2$  sample compared to the Monte Carlo expectation. The resolution of this ratio, which is calculated for  $y_e > 0.05$ , and thus of  $y_{\Sigma}$  is better than 13% in this kinematic region. The “tail” visible at values below 0.7 is due to radiative events, and is well described by the Monte Carlo simulation.

## 5.2. Selection of deep-inelastic radiative events

A sample of deep-inelastic events with an energetic photon ( $E_{\gamma} > 4$  GeV) emitted collinear with the incident electron was selected. These radiative events can be interpreted as deep-inelastic scattering events with a reduced (“true”) incident energy  $E_t = E_e - E_{\gamma}$  which can be reconstructed due to the additional detection of the radiated photon in the small angle photon tagger of the luminosity system. When using the E method, the kinematic variables  $y_t$  and  $Q_t^2$  are obtained by replacing in Eq. (1) the nominal beam energy by the reduced energy  $E_t$ . Note that  $Q_{\Sigma}^2$  and  $y_{\Sigma}$  are unchanged by the  $E_e \rightarrow E_t$  transformation while  $x_{\Sigma}$  is affected.

A first experimental study of this process at HERA has been published [15,34] by the H1 Collaboration using 1993 data, which were however too limited in statistics for a quantitative study of the proton structure. The larger integrated luminosity of the 1994

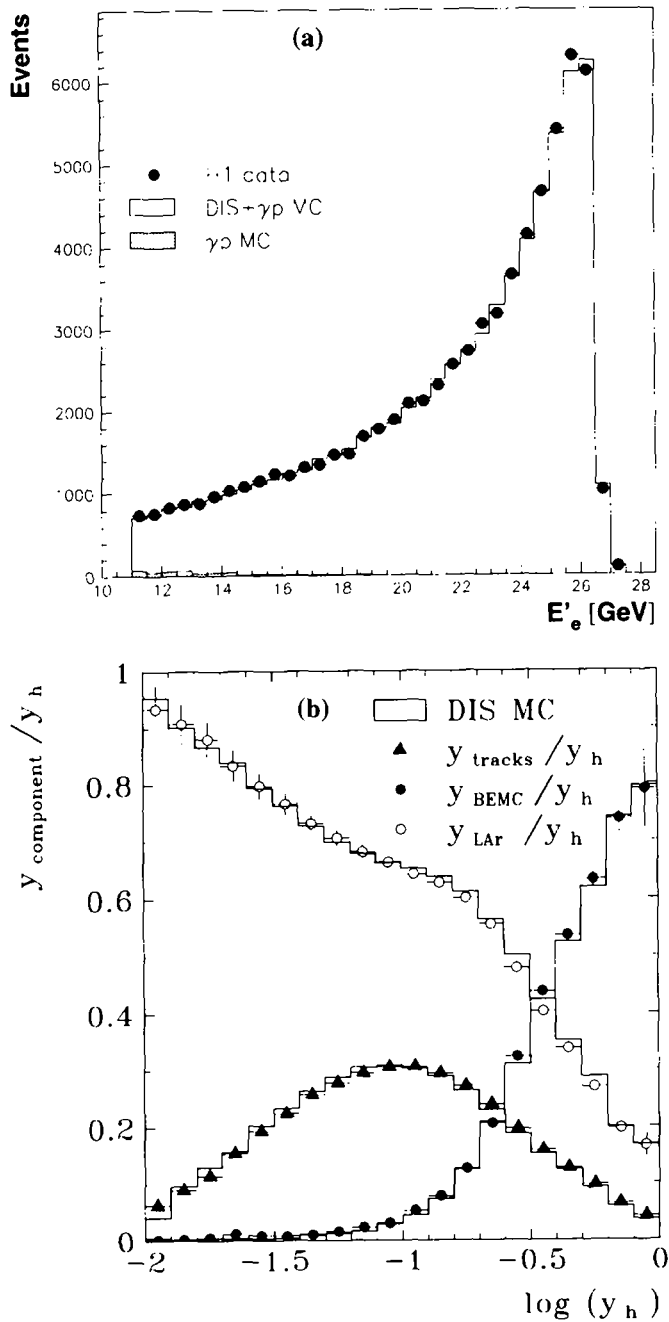


Fig. 3. Nominal vertex data with the scattered electron in the BEMC ( $Q^2 \leq 120 \text{ GeV}^2$ ): experimental and Monte Carlo distributions (a) of the scattered electron energy and (b) of the fraction of  $y_h$  contributed by the tracks, the LAr calorimeter and the BEMC.

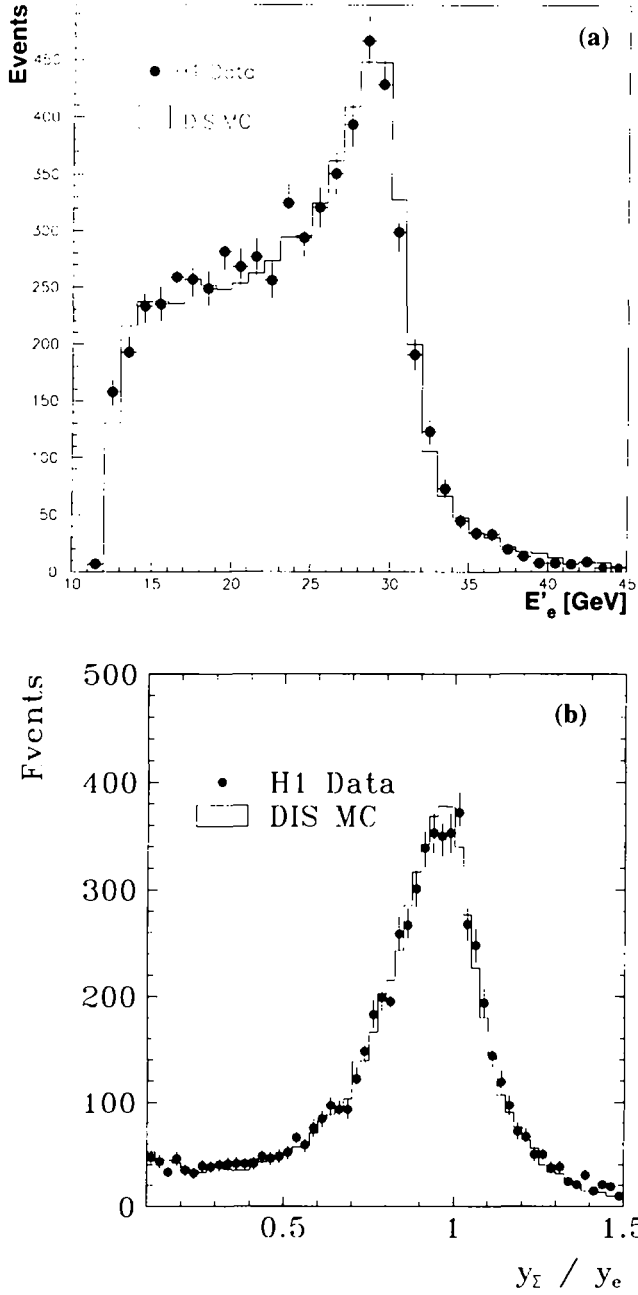


Fig. 4. High  $Q^2$  data: experimental and Monte Carlo distributions (a) of the energy of the scattered electron detected in the LAr calorimeter and (b) of the ratio  $y_L / y_e$ , for  $y_e \geq 0.05$ .



Table 2

Summary of event selection criteria for the radiative event sample. For the electron identification two estimators were used:  $\epsilon_1$ : electron cluster radius and  $\epsilon_2$ : smallest distance from the closest track to the centroid of the electron cluster. The variable  $\Delta$  is defined in Eq. (6).

Low $Q^2$ (radiative events)	
E, $\Sigma$ method	
$\theta_e/^\circ$	$\leq 174$
$E_e'/\text{GeV}$	$> 8$
$z_{\text{vertex}}/\text{cm}$	$5 \pm 35$
electron identif.	$\epsilon_1 < 5 \text{ cm}$
electron identif.	$\epsilon_2 < 4 \text{ cm}$
$E_\gamma/\text{GeV}$	$> 4$
$E_{\text{ctag}}/\text{GeV}$	$< 2$
$\Delta$	$< 0.5$

data permits a significant  $F_2$  measurement for  $Q^2$  values down to  $1.5 \text{ GeV}^2$ . The ZEUS Collaboration [36] recently published results on  $F_2$  using this method.

A summary of the selection criteria of the final sample of about 8200 events is given in Table 2 [35]. The event selection for radiative events is similar to the one for low  $Q^2$  non-radiative events, apart from the additional requirement of a detected photon with at least 4 GeV in the small angle photon tagger of the luminosity system. This requirement also reduces the photoproduction background. Therefore the minimum scattered electron energy can be lowered to 8 GeV.

The selected sample contains both radiative DIS events and pile-up events due to overlaps of DIS and  $\gamma p$  events with Bethe–Heitler events in a time window of  $\pm 5 \text{ ns}$ . The pile-up events are partly removed from the sample by requiring the energy in the electron tagger,  $E_{\text{ctag}}$ , to be less than 2 GeV, but the majority of them remains.

The background can be controlled through the redundancy of the true electron beam energy measurement  $E_t$ . For radiative DIS events we expect measurements of the quantity

$$\Delta \equiv [E_\gamma - E_e(y_e - y_h)]/E_\gamma \quad (6)$$

to be concentrated around zero while for pile-up DIS events a concentration around one is expected. Here  $y_e$  and  $y_h$  are calculated according to Eqs. (1) and (5). The distribution of  $\Delta$  is shown in Fig. 5 for a sample of events with (a)  $E_{\text{ctag}} > 2 \text{ GeV}$  (dominantly  $ep$  collisions with BH overlap events) and (b)  $E_{\text{ctag}} < 2 \text{ GeV}$ . The data are compared with Monte Carlo simulation. The pile-up sample in Fig. 5a shows a clear peak for  $\Delta = 1$ , and is well described by the sum of simulated DIS and  $\gamma p$  distributions with overlap of BH events. Fig. 5b shows a peak for  $\Delta = 1$  from residual pile-up events for which the electron from the BH event was not detected, and a peak around  $\Delta = 0$  from genuine radiative events. Radiative events are selected in this analysis by requiring  $\Delta < 0.5$ . The background of pile-up events as estimated by the Monte Carlo simulation studies is subtracted statistically. The remaining background from overlap  $\gamma p$  and DIS

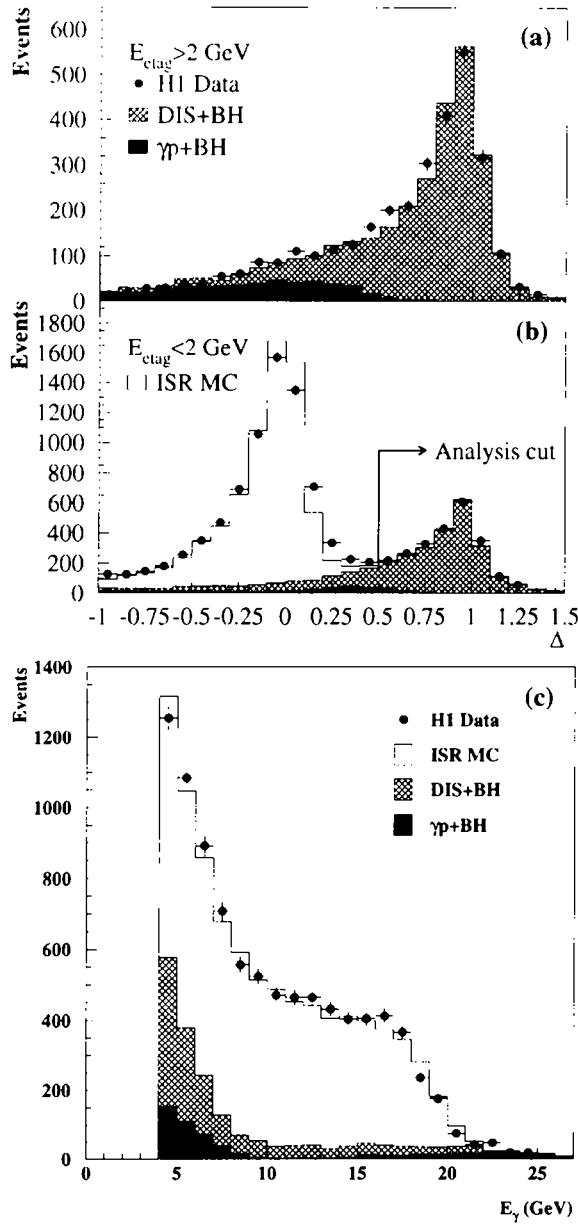


Fig. 5. Radiative events: experimental and Monte Carlo distributions of  $\Delta$  (Eq. (6)) with (a) the energy detected in the electron tagger ( $E_{\text{ctag}}$ ) bigger than 2 GeV; (b) with  $E_{\text{ctag}} < 2 \text{ GeV}$  and (c) distribution of the photon energy detected in the photon tagger. The analysis cut in (b) indicates the region of  $\Delta > 0.5$  excluded from the analysis. The full solid line in (b) and (c) represents the sum of all three contributions in the Monte Carlo: DIS initial state radiation events (ISR MC), DIS events with a BH overlap (DIS + BH) and photoproduction events with a BH overlap ( $\gamma\text{p} + \text{BH}$ ).

events estimated from Monte Carlo studies amounts to 8%, with at most 15% in an  $x, Q^2$  bin. In Fig. 5c the photon energy spectrum as measured in the photon tagger is shown for the selected sample and compared with simulated signal and background distributions. There is a good agreement between data and Monte Carlo simulation.

## 6. Structure function measurement

The structure function  $F_2(x, Q^2)$  was derived from the one-photon exchange cross section

$$\frac{d^2\sigma}{dx dQ^2} = \frac{2\pi\alpha^2}{Q^4 x} \left( 2 - 2y + \frac{y^2}{1+R} \right) F_2(x, Q^2). \quad (7)$$

The structure function ratio  $R = F_2/2xF_1 - 1$  has not yet been measured at HERA. It was calculated using the QCD relation [37] with the NLO strong coupling constant [38] and the GRV structure function parametrization. Note that a 20% error on  $R$  corresponds to about 2% uncertainty on  $F_2$  at  $y = 0.6$  for  $R$  of about 0.6. The  $R$  values are quoted in Tables 3-5; the uncertainty on  $R$  was not included in the systematic errors of the  $F_2$  measurements.

Compared to the previous H1 analysis [4] the  $F_2$  measurement has been extended to lower and higher  $Q^2$  (from  $4.5 - 1600 \text{ GeV}^2$  to  $1.5 - 5000 \text{ GeV}^2$ ), and to lower and higher  $x$  (from  $1.8 \cdot 10^{-4} \leq x \leq 0.13$  to  $3 \cdot 10^{-5} \leq x \leq 0.32$ ). The determination of the structure function requires the measured event numbers to be converted to the bin averaged cross section based on the Monte Carlo acceptance calculation. The binning in  $x$  was governed by the detector resolution and could be chosen to be rather fine since the E and  $\Sigma$  methods were used in the optimum range at low and high  $x$ , respectively. The  $x$  resolution is better than 20%. The  $Q^2$  resolution is about 5% and the number of bins in  $Q^2$  was adapted to statistics. All detector efficiencies were determined from the data utilizing the redundancy of the apparatus. Apart from very small extra corrections, all efficiencies were correctly reproduced by the Monte Carlo simulation. The bin averaged cross section was corrected for higher order QED radiative contributions using the program HECTOR [39]. Effects due to Z boson exchange at present values of  $Q^2$  and  $y$  are smaller than 3% and were treated as part of the radiative corrections.

Different data sets are available which, for a given  $(Q^2, x)$  interval, use different parts of the detectors. Thus many cross checks could be made in kinematic regions of overlap for the two kinematic reconstruction methods and these gave very satisfactory results. In this paper results are presented from the radiative  $F_2$  analysis ( $1.5 \leq Q^2 \leq 3.5 \text{ GeV}^2$ ), from the shifted vertex analysis ( $1.5 \leq Q^2 \leq 2.5 \text{ GeV}^2$ ), from a combination of the shifted vertex and the satellite bunch analysis ( $3.5 \leq Q^2 \leq 6.5 \text{ GeV}^2$ ), from the open triangle analysis ( $Q^2 = 8.5 \text{ GeV}^2$ ) and from the nominal high statistics sample when the scattered electron is detected in the BEMC ( $12 \leq Q^2 \leq 120 \text{ GeV}^2$ ) or in the LAR calorimeter ( $120 < Q^2 \leq 5000 \text{ GeV}^2$ ).

Table 3

Proton structure function  $F_2(x, Q^2)$  with statistical and systematic errors, part I. The normalization uncertainty, not included in the systematic error, is 1.5% for  $Q^2 \geq 8.5 \text{ GeV}^2$  and 3.9% for  $Q^2 < 8.5 \text{ GeV}^2$ .

$Q^2$	$x$	$F_2$	$\delta_{\text{stat}}$	$\delta_{\text{syst}}$	$R$	$Q^2$	$x$	$F_2$	$\delta_{\text{stat}}$	$\delta_{\text{syst}}$	$R$
1.5	.00003	0.969	0.176	0.187	0.71	8.5	.00130	0.811	0.030	0.047	0.42
1.5	.00025	0.540	0.055	0.104	0.75	8.5	.00200	0.770	0.034	0.049	0.40
1.5	.00063	0.458	0.050	0.101	0.74	8.5	.00320	0.562	0.028	0.043	0.38
1.5	.00158	0.365	0.045	0.095	0.70	8.5	.00500	0.648	0.033	0.051	0.36
1.5	.00398	0.381	0.070	0.087	0.63	8.5	.00800	0.564	0.032	0.049	0.33
2.0	.00005	1.037	0.077	0.110	0.65	12.	.00032	1.276	0.020	0.055	0.39
2.5	.00008	0.885	0.052	0.065	0.80	12.	.00050	1.168	0.016	0.056	0.39
2.5	.00013	0.874	0.079	0.127	0.80	12.	.00080	1.067	0.015	0.061	0.38
2.5	.00025	0.622	0.037	0.119	0.80	12.	.00130	0.942	0.015	0.039	0.37
2.5	.00063	0.621	0.039	0.093	0.79	12.	.00200	0.866	0.016	0.057	0.36
2.5	.00158	0.466	0.033	0.072	0.75	12.	.00320	0.749	0.016	0.055	0.34
2.5	.00398	0.402	0.039	0.062	0.65	12.	.00500	0.685	0.016	0.061	0.32
3.5	.00008	1.036	0.053	0.092	0.64	12.	.00800	0.618	0.016	0.057	0.30
3.5	.00013	1.026	0.045	0.067	0.64	12.	.01300	0.531	0.017	0.049	0.26
3.5	.00020	0.934	0.041	0.075	0.64	15.	.00032	1.426	0.030	0.064	0.37
3.5	.00032	0.854	0.046	0.093	0.64	15.	.00050	1.280	0.020	0.050	0.36
3.5	.00050	0.716	0.041	0.119	0.64	15.	.00080	1.110	0.018	0.057	0.35
3.5	.00080	0.712	0.049	0.126	0.63	15.	.00130	1.008	0.016	0.033	0.35
3.5	.00130	0.778	0.058	0.137	0.61	15.	.00200	0.895	0.015	0.046	0.34
3.5	.00250	0.621	0.043	0.157	0.59	15.	.00320	0.773	0.014	0.036	0.32
3.5	.00398	0.458	0.046	0.075	0.54	15.	.00500	0.677	0.014	0.035	0.30
5.0	.00013	1.106	0.049	0.074	0.54	15.	.00800	0.634	0.014	0.031	0.28
5.0	.00020	1.033	0.044	0.069	0.54	15.	.01300	0.547	0.013	0.027	0.24
5.0	.00032	0.907	0.039	0.066	0.54	20.	.0005	1.407	0.026	0.054	0.34
5.0	.00050	0.839	0.039	0.076	0.53	20.	.0008	1.210	0.022	0.050	0.33
5.0	.00080	0.769	0.037	0.063	0.53	20.	.0013	1.061	0.020	0.055	0.33
5.0	.00130	0.630	0.034	0.050	0.51	20.	.0020	0.945	0.018	0.042	0.32
5.0	.00200	0.540	0.033	0.043	0.50	20.	.0032	0.861	0.017	0.038	0.31
5.0	.00400	0.500	0.029	0.086	0.46	20.	.0050	0.761	0.017	0.028	0.30
6.5	.00013	1.292	0.085	0.127	0.49	20.	.0080	0.693	0.016	0.035	0.28
6.5	.00020	1.101	0.052	0.072	0.48	20.	.0130	0.567	0.015	0.024	0.26
6.5	.00032	0.963	0.045	0.068	0.48	20.	.0200	0.487	0.015	0.025	0.22
6.5	.00050	0.926	0.044	0.088	0.48	25.	.0005	1.546	0.047	0.058	0.40
6.5	.00080	0.848	0.038	0.076	0.47	25.	.0008	1.330	0.028	0.051	0.39
6.5	.00130	0.759	0.039	0.068	0.46	25.	.0013	1.151	0.024	0.047	0.38
6.5	.00250	0.667	0.029	0.054	0.43	25.	.0020	1.019	0.022	0.035	0.37
6.5	.00630	0.504	0.029	0.084	0.37	25.	.0032	0.872	0.020	0.034	0.35
8.5	.00020	1.215	0.050	0.062	0.44	25.	.0050	0.768	0.019	0.034	0.33
8.5	.00032	1.089	0.038	0.048	0.44	25.	.0080	0.683	0.018	0.031	0.30
8.5	.00050	1.033	0.034	0.062	0.43	25.	.0130	0.585	0.017	0.028	0.26
8.5	.00080	0.923	0.031	0.038	0.43	25.	.0200	0.548	0.017	0.037	0.22

Table 4

Proton structure function  $F_2(x, Q^2)$  with statistical and systematic errors, part II. The normalization uncertainty, not included in the systematic error, is 1.5%.

$Q^2$	$x$	$F_2$	$\delta_{\text{stat}}$	$\delta_{\text{syst}}$	$R$	$Q^2$	$x$	$F_2$	$\delta_{\text{stat}}$	$\delta_{\text{syst}}$	$R$
35.	.0008	1.442	0.038	0.051	0.36	150.	.0200	0.566	0.069	0.114	0.15
35.	.0013	1.308	0.032	0.052	0.35	150.	.0320	0.598	0.085	0.103	0.12
35.	.0020	1.116	0.027	0.052	0.33	150.	.0500	0.424	0.071	0.065	0.09
35.	.0032	0.928	0.024	0.038	0.32						
35.	.0050	0.832	0.023	0.040	0.30	200.	.005	1.065	0.059	0.053	0.21
35.	.0080	0.739	0.022	0.035	0.27	200.	.008	0.853	0.051	0.038	0.19
35.	.0130	0.600	0.019	0.025	0.24	200.	.013	0.787	0.052	0.071	0.17
35.	.0200	0.508	0.019	0.019	0.20	200.	.020	0.585	0.041	0.023	0.14
35.	.0320	0.452	0.019	0.026	0.16	200.	.032	0.490	0.038	0.026	0.11
						200.	.050	0.460	0.039	0.029	0.09
45.	.0013	1.305	0.038	0.048	0.32	200.	.080	0.372	0.032	0.039	0.06
45.	.0020	1.225	0.034	0.049	0.31	200.	.130	0.350	0.037	0.032	0.04
45.	.0032	1.105	0.032	0.058	0.30	200.	.200	0.301	0.045	0.036	0.03
45.	.0050	0.912	0.028	0.033	0.28						
45.	.0080	0.743	0.025	0.029	0.26	250.	.005	1.185	0.106	0.060	0.20
45.	.0130	0.686	0.024	0.031	0.22	250.	.008	1.000	0.062	0.054	0.18
45.	.0200	0.599	0.022	0.027	0.19	250.	.013	0.826	0.055	0.047	0.16
45.	.0320	0.505	0.021	0.023	0.15	250.	.020	0.730	0.051	0.072	0.14
45.	.0500	0.411	0.022	0.028	0.12	250.	.032	0.590	0.044	0.067	0.11
						250.	.050	0.584	0.043	0.060	0.09
60.	.0020	1.213	0.042	0.048	0.29	250.	.080	0.408	0.033	0.037	0.06
60.	.0032	1.079	0.037	0.045	0.28	250.	.130	0.312	0.029	0.051	0.04
60.	.0050	0.937	0.033	0.043	0.26	250.	.200	0.231	0.031	0.056	0.03
60.	.0080	0.830	0.031	0.046	0.24						
60.	.0130	0.701	0.028	0.029	0.21	350.	.008	0.997	0.082	0.049	0.17
60.	.0200	0.639	0.027	0.025	0.18	350.	.013	0.825	0.066	0.043	0.15
60.	.0320	0.586	0.026	0.028	0.14	350.	.020	0.581	0.052	0.042	0.13
60.	.0500	0.492	0.025	0.023	0.11	350.	.032	0.608	0.054	0.056	0.10
60.	.0800	0.432	0.027	0.023	0.08	350.	.050	0.570	0.052	0.061	0.08
						350.	.080	0.447	0.043	0.038	0.06
90.	.0032	1.103	0.052	0.048	0.26	350.	.130	0.356	0.036	0.057	0.04
90.	.0050	0.997	0.045	0.047	0.24	350.	.200	0.256	0.036	0.055	0.03
90.	.0080	0.908	0.041	0.056	0.22	350.	.320	0.280	0.051	0.061	0.02
90.	.0130	0.726	0.035	0.040	0.19						
90.	.0200	0.650	0.033	0.031	0.17	500.	.013	0.904	0.083	0.050	0.14
90.	.0320	0.587	0.030	0.034	0.13	500.	.020	0.725	0.065	0.046	0.12
90.	.0500	0.481	0.027	0.019	0.10	500.	.032	0.546	0.059	0.034	0.10
						500.	.050	0.433	0.051	0.035	0.08
120.	.0050	1.018	0.094	0.076	0.23	500.	.080	0.397	0.047	0.032	0.06
120.	.0080	0.914	0.068	0.056	0.21	500.	.130	0.276	0.036	0.030	0.04
120.	.0130	0.755	0.063	0.111	0.18	500.	.200	0.228	0.035	0.027	0.03
120.	.0200	0.570	0.049	0.057	0.16						
120.	.0320	0.582	0.048	0.060	0.13	650.	.013	0.881	0.120	0.076	0.14
120.	.0500	0.402	0.035	0.045	0.10	650.	.020	0.727	0.081	0.061	0.12
120.	.0800	0.330	0.032	0.034	0.07	650.	.032	0.545	0.068	0.047	0.09
						650.	.050	0.483	0.062	0.045	0.07
150.	.0032	1.292	0.069	0.067	0.23	650.	.080	0.422	0.059	0.031	0.05
150.	.0050	1.067	0.065	0.057	0.22	650.	.130	0.369	0.050	0.030	0.04
150.	.0080	0.928	0.061	0.060	0.20	650.	.200	0.262	0.044	0.042	0.03
150.	.0130	0.716	0.064	0.079	0.17	650.	.320	0.222	0.055	0.074	0.02

Table 5

Proton structure function  $F_2(x, Q^2)$  with statistical and systematic errors, part III. The normalization uncertainty, not included in the systematic error, is 1.5%.

$Q^2$	$x$	$F_2$	$\delta_{\text{stat}}$	$\delta_{\text{syst}}$	$R$	$Q^2$	$x$	$F_2$	$\delta_{\text{stat}}$	$\delta_{\text{syst}}$	$R$
800.	.020	0.686	0.098	0.083	0.11	1200.	.200	0.260	0.057	0.048	0.02
800.	.032	0.676	0.085	0.082	0.09	1200.	.320	0.201	0.056	0.064	0.01
800.	.050	0.533	0.075	0.067	0.07						
800.	.080	0.428	0.075	0.057	0.05	2000.	.05	0.634	0.087	0.046	0.06
800.	.130	0.490	0.075	0.066	0.04	2000.	.08	0.395	0.060	0.035	0.05
800.	.200	0.312	0.057	0.073	0.03	2000.	.13	0.237	0.048	0.026	0.03
800.	.320	0.258	0.065	0.090	0.02	2000.	.20	0.199	0.041	0.017	0.02
						2000.	.32	0.193	0.043	0.045	0.01
1200.	.032	0.668	0.109	0.091	0.09						
1200.	.050	0.412	0.078	0.064	0.07	5000.	.13	0.453	0.121	0.056	0.03
1200.	.080	0.502	0.089	0.069	0.05	5000.	.20	0.229	0.087	0.030	0.02
1200.	.130	0.436	0.084	0.066	0.03	5000.	.32	0.283	0.085	0.064	0.01

Compared with the analysis of the 1993 data, many uncertainties have been reduced. The systematic errors are due to the following sources:

- The uncertainty in the electron energy scale which is 1% in the BEMC, and 3% in the LAr calorimeter. Since the  $y_e$  resolution varies as  $1/y$  with the energy resolution even a 1% error on  $\delta E/E$  can lead to 10% errors on  $F_2$  at low  $y$  in the E method.
- The uncertainty in the hadronic energy scale: the detailed study of  $y_h/y_e$  and of  $p_{T,h}/p_{T,e}$  ( $p_T$  is the momentum transverse to the beam axis) allowed the assignment of a 4% error on the hadronic energy deposited in the LAr calorimeter, a 15% error on the same quantity in the BEMC, and a 3% error on the  $y_h$  fraction carried by the tracks. These errors take into account the intrinsic energy scale uncertainty of each detector and the uncertainty of the sharing of the total hadronic final state energy between these three subdetectors. These numbers also include uncertainties due to the treatment of the electronic noise in the LAr calorimeter and the BEMC.
- An uncertainty of up to 1 mrad for the electron polar angle which leads to an error on  $F_2$  of 8% at low  $Q^2$ .
- Apart from the electron identification, all efficiencies were determined from the data and compared with Monte Carlo simulation. The agreement between the experimental and the simulated values for the individual efficiencies was found to be better than 2%. An overall error of 2% was assigned due to the imperfect description of the various efficiencies. A larger error was added to account for the variation of the vertex reconstruction efficiency at large  $x$  (up to 8%) where jets get closer to the beam pipe in the forward direction, and at small  $x$  or large  $\theta$  (up to 4%) where H1 had no further tracking device besides the BPC to monitor the vertex efficiency.
- Uncertainties in the hadronic corrections, the cross section extrapolation towards  $Q^2 = 0$  and higher order corrections, which give an error of up to 2% in the radiative correction. The accuracy was cross checked by comparing the HECTOR calculation with the HERACLES Monte Carlo simulation results. The agreement to the few percent level between the structure function results obtained with the E and the  $\Sigma$

methods is an additional cross check for the control of the radiative corrections.

- The structure function dependence of the acceptance which was kept below 1% by performing a two step iterative analysis. The uncertainty in the simulation of the hadronic final state reflects most prominently in the efficiency for the requirement of an interaction vertex from tracks. A comparison of the different models (Section 4.3) for the hadronic final state was used to assign an additional 3% systematic error entering in all analyses at low  $x$  through the vertex efficiency.
- Based on the control data sample of electron tagged  $\gamma p$  events the uncertainty due to photoproduction background could be estimated to be smaller than 30% of the correction applied. This is equivalent to at most a 5% systematic error in the highest  $y$  bins at lower  $Q^2$  only.
- Statistical errors in the Monte Carlo acceptance and efficiency calculations were computed and added quadratically to the systematic error.
- For the analysis of radiative events an additional 1.5% uncertainty on the photon energy measurement in the photon tagger was considered and a 2% systematic error was added due to the uncertainty of the photon tagger geometrical acceptance. An uncertainty on the trigger efficiency of 6% to 9% was included for the lowest  $x$  points.

Some of the systematic uncertainties affect differently the  $F_2$  measurement in the different methods. The systematic errors are given in Tables 3–5 point by point. However, some are strongly correlated over a large kinematic range. These correlations have been considered in the fits reported below. The matrix with the many different error contributions is available upon request to the H1 Collaboration. In Fig. 6 the comparison of the measurements using the E and using the  $\Sigma$  method is shown. Both are in good agreement for all  $Q^2$  values. Some possible discrepancies between both methods, e.g. at  $Q^2 = 3.5 \text{ GeV}^2$ , were investigated carefully and taken into account when evaluating the systematic error of the final structure function values if they could not be resolved. Small deviations are possible though, due to the different population of the  $x, Q^2$  plane between the methods of calculating the kinematics. The two measurements are combined using the E method for  $y > 0.15$  and the  $\Sigma$  method for  $y < 0.15$ . The result is shown in Fig. 7 and given in Tables 3–5. The measurements obtained from the low  $Q^2$  nominal vertex sample have a typical systematic error of 5%. The large statistics allow the measurement of  $F_2$  to reach  $Q^2$  values of  $5000 \text{ GeV}^2$ , and to achieve a few percent statistical precision at  $Q^2$  below  $100 \text{ GeV}^2$ . The results are in good agreement with the previous H1 publication [4]. In particular, the distinct rise of  $F_2$  towards low  $x$ , observed with the 1992 and 1993 [2,4] data, is confirmed with higher precision and extends now to significantly lower  $Q^2$  values.

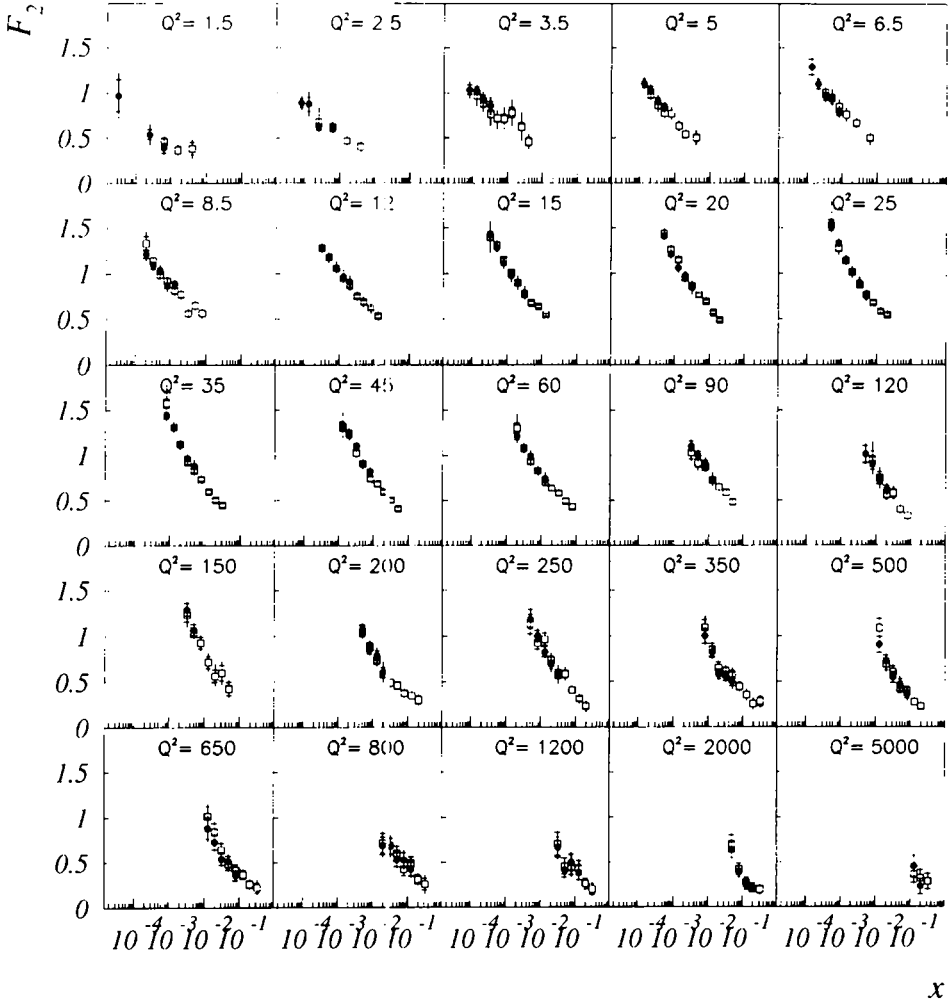


Fig. 6. Measurement of the structure function with the electron (closed circles) and the  $\Sigma$  method (open squares). The  $Q^2$  values are in  $\text{GeV}^2$ . The inner error bar is the statistical error. The full error bar represents the statistical and systematic errors added in quadrature disregarding the error from the luminosity measurement.

**7. Discussion of the results**

*7.1. Phenomenological fits to the data*

The  $x$  and  $Q^2$  behaviour of  $F_2$  can be described by a phenomenological ansatz of the type

$$F_2(x, Q^2) = [a \cdot x^b + c \cdot x^d \cdot (1 + e \cdot \sqrt{x}) \cdot (\log Q^2 + f \log^2 Q^2 + h/Q^2)] \cdot (1 - x)^g, \tag{8}$$



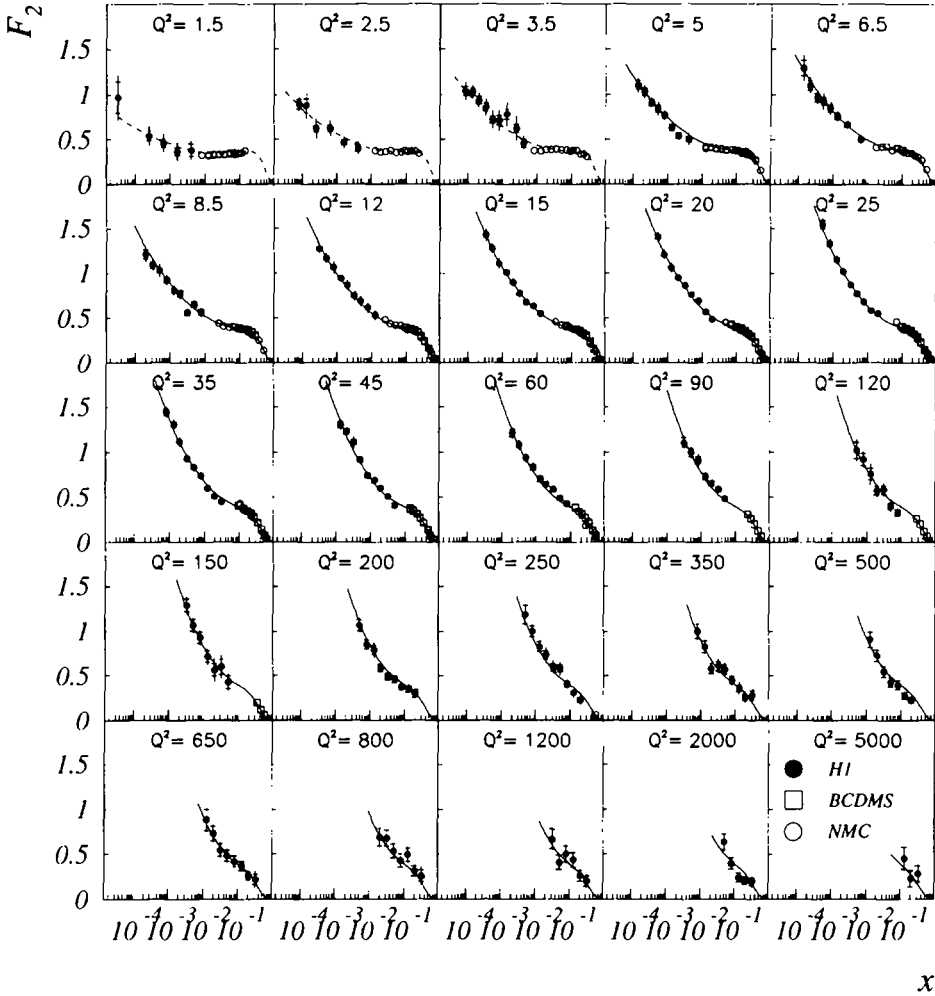


Fig. 7. Measurement of the structure function  $F_2(x, Q^2)$  as a function of  $x$ . The  $Q^2$  values are in  $\text{GeV}^2$ . The closed circles are the results of this analysis, the open circles are results taken from the recent publication of the NMC [40] and the open squares results from BCDMS [41]. The inner error bar is the statistical error. The full error bar represents the statistical and systematic errors added in quadrature and disregarding the luminosity error. Additionally a data point has also been measured at  $Q^2 = 2 \text{ GeV}^2$  (see Table 3, not shown in the Figure). The curves represent the NLO QCD fit described in Section 7.4, which includes the data for  $Q^2 \geq 5 \text{ GeV}^2$ . The extension of the curves below  $5 \text{ GeV}^2$  represents only the backward evolution of the fit.

where  $Q^2$  is given in  $\text{GeV}^2$ . This functional form was introduced in detail previously [4]. An extra  $1/Q^2$  term has been added in order to get a good description at  $Q^2$  below  $5 \text{ GeV}^2$ . Note that this term is not a measure of higher twist contributions. For the fit, results from H1, NMC [40] and BCDMS [41] are used and statistical and systematic errors were added in quadrature. The parameter values quoted in Table 6 are close to those obtained with 1993 data. The fit provides a good description of all data from the experiments with a  $\chi^2/\text{dof}$  of 1.65 using full errors. For the H1 data alone the

Table 6

Parameters of a phenomenological fit to the proton structure function results from this experiment combined with  $F_2$  measurements from the NMC and the BCDMS experiments. The parametrization is valid for  $1.5 \text{ GeV}^2 < Q^2 < 5000 \text{ GeV}^2$ ,  $3 \cdot 10^{-5} < x < 1$  and  $Q^2 < x \cdot 10^5 \text{ GeV}^2$ . The parameter  $h$  is given in  $\text{GeV}^2$ .

a	b	c	d	e	f	g	h
3.10	0.76	0.124	-0.188	-2.91	-0.043	3.69	1.40

Table 7

The values of the exponent  $\lambda$  as a function of  $Q^2$ .

$Q^2/\text{GeV}^2$	$\lambda$	$\delta\lambda_{\text{stat}}$	$\delta\lambda_{\text{syst}}$	$Q^2/\text{GeV}^2$	$\lambda$	$\delta\lambda_{\text{stat}}$	$\delta\lambda_{\text{syst}}$
1.5	0.211	0.051	0.068	45	0.330	0.012	0.023
2.5	0.189	0.031	0.045	60	0.278	0.015	0.015
3.5	0.191	0.020	0.058	90	0.314	0.025	0.043
5.0	0.255	0.020	0.049	120	0.433	0.044	0.045
6.5	0.212	0.017	0.021	150	0.398	0.055	0.027
8.5	0.228	0.015	0.014	200	0.372	0.039	0.032
12	0.238	0.007	0.031	250	0.360	0.036	0.060
15	0.261	0.006	0.022	350	0.270	0.063	0.060
20	0.268	0.007	0.020	500	0.460	0.108	0.047
25	0.286	0.009	0.024	650	0.391	0.128	0.059
35	0.331	0.010	0.022	800	0.503	0.235	0.129

parametrization gives a  $\chi^2/\text{dof}$  of 1.00.

In perturbative QCD the rate of growth of  $F_2$  towards low  $x$  is expected to increase with increasing  $Q^2$  [6]. The wide range of momentum transfer covered in this experiment enables a study of the  $Q^2$  dependence of the power  $\lambda$  characterizing the rise of  $F_2 \propto x^{-\lambda}$  at low  $x$ . For each  $Q^2$  bin and  $x < 0.1$  the exponent  $\lambda$  was determined taking into account the point-to-point systematic error correlations. The result is given in Table 7 and displayed in Fig. 8. A rise of  $\lambda$  with  $\log Q^2$  is observed in the covered range from about 0.2 to 0.4 between 1.5 and 800  $\text{GeV}^2$ .

The structure function  $F_2$  is related to the total cross-section of the virtual photon-proton interaction,  $\sigma_{\text{tot}}(\gamma^*p)$ , via

$$\sigma_{\text{tot}}(\gamma^*p) \simeq \frac{4 \pi^2 \alpha}{Q^2} F_2(W, Q^2). \tag{9}$$

At low  $x$ ,  $W$  is equal to  $\sqrt{Q^2/x}$ . The  $\lambda$  parameter thus also determines the dependence of  $F_2$  on the invariant mass squared  $W^2$  of the virtual photon-proton ( $\gamma^*p$ ) system. For hadronic and real photoproduction total cross sections the value of  $\lambda$  has been measured to be around 0.08 [42], which is interpreted as the intercept of the so-called soft pomeron. For virtual photon-proton interactions  $\lambda$  is found to be substantially larger, and increases with  $Q^2$ . Future analyses of HERA data, which will lead to  $F_2$  measurements at  $Q^2$  below 1  $\text{GeV}^2$ , should allow the transition between deep-inelastic scattering and real photoproduction to be studied.

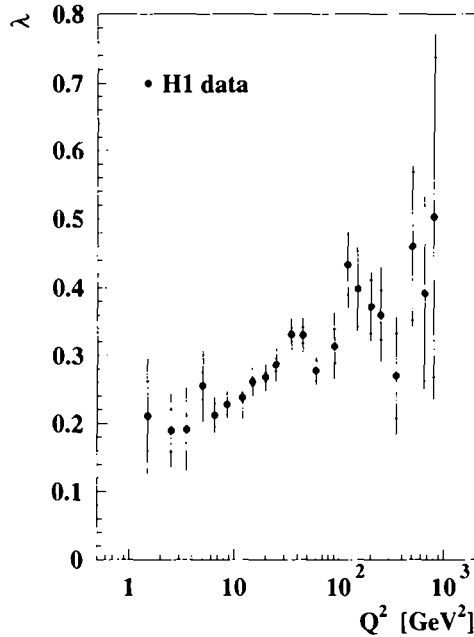


Fig. 8. Variation of the exponent  $\lambda$  from fits of the form  $F_2 \sim x^{-\lambda}$  at fixed  $Q^2$  values and  $x < 0.1$ .

### 7.2. Comparison with models at low $Q^2$

Figs. 7 and 9 clearly demonstrate the rise of  $F_2$  with decreasing  $x$ . In Fig. 9 the data from the eight lowest  $Q^2$  bins are shown<sup>14</sup> and compared with recent data and  $F_2$  parametrizations. The rise of  $F_2$  towards low  $x$  is also present in the low  $Q^2$  region. The measurement is in good agreement with the data from the ZEUS experiment [36] and matches well with the data from fixed target experiments [43,40] at higher  $x$  values.

The curves denoted as MRSA', MRSG [44], CTEQ3M [45] and GRV [19] are parametrizations based on the conventional QCD evolution equations. These calculations assume a certain shape of the  $x$  behaviour at a starting  $Q_0^2$  value and use the DGLAP [7] equations to get predictions at different  $Q^2$  values. The MRS and CTEQ distributions assume an  $x^{-\lambda}$  behaviour for  $x \rightarrow 0$  at starting  $Q_0^2$  of a few GeV $^2$ . Their parameters were determined using also the 1993 HERA structure function data.

The GRV calculation assumes that all parton distributions at very low  $Q_0^2 = 0.34$  GeV $^2$  have a valence like shape, i.e. vanish for  $x \rightarrow 0$ . Assuming that the DGLAP equations can be used to evolve the parton distributions from this low  $Q_0^2$  scale to larger  $Q^2$  values, they predicted that the structure function  $F_2$  should rise towards low  $x$  even for low values of  $Q^2 \sim 1$  GeV $^2$  [19]. The determination of the shape parameters of the

<sup>14</sup> For the radiative data points (triangles in Fig. 9) the  $y$  variable cannot be calculated using  $Q^2/sx$  with the nominal  $x$  since each bin has a different mean incoming electron energy. The average  $y$  values are 0.143, 0.063, 0.026, 0.010 for  $Q^2 = 1.5$  GeV $^2$  and 0.199, 0.086, 0.036, 0.015 for  $Q^2 = 2.5$  GeV $^2$ , starting at the smallest given  $x$  value. For the single point at  $Q^2 = 3.5$  GeV $^2$   $y = 0.018$ .

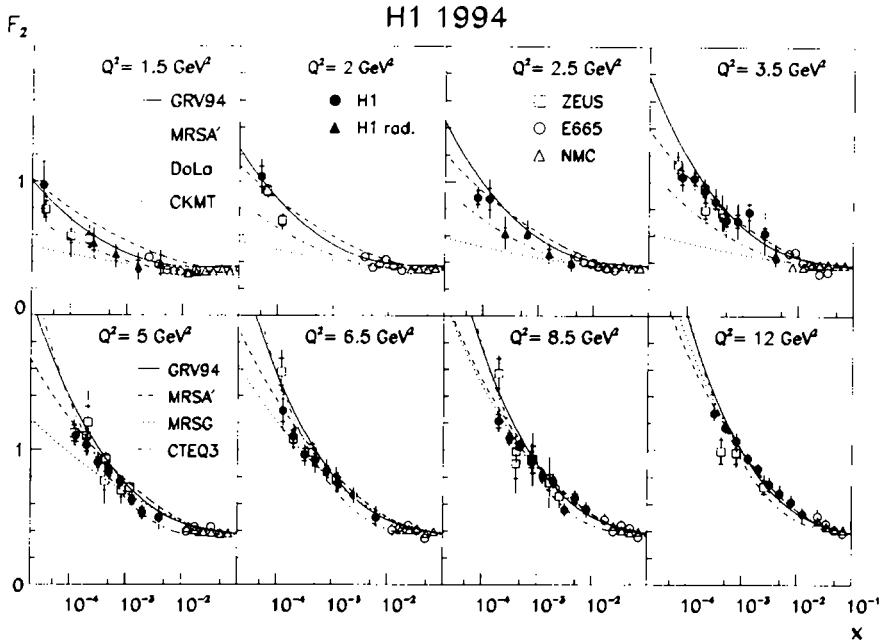


Fig. 9. Measurement of the proton structure function  $F_2(x, Q^2)$  in the low  $Q^2$  region by H1 (closed circles: non-radiative events; closed triangles: radiative events), together with results from the ZEUS [36] (open squares), E665 [43] (open circles) and NMC [40] (open triangles) experiments. The  $Q^2$  values of the ZEUS data shown for the bins  $Q^2 = 3.5, 5$  and  $6.5 \text{ GeV}^2$  are measurements at  $3.0, 4.5$  and  $6 \text{ GeV}$  respectively. Different parametrizations for  $F_2$  are compared to the data. The DOLA and CKMT curves are only shown for the upper row of  $Q^2$  bins; CTEQ3M and MRSG are shown for the lower row; GRV and MRSA' are shown for the full  $Q^2$  range.

distributions at the starting scale uses only data from fixed target experiments and not much freedom is left for further adjustments in the kinematic range of the HERA data. Small variations are connected with changes still possible in the starting  $Q_0^2$  and the value of the QCD parameter  $\Lambda$ . Fig. 9 shows that the GRV distributions describe the data well, indicating that in this kinematic regime the sea quark distributions can be produced by QCD dynamics.

Parametrizations motivated by Regge theory relate the structure function to Reggeon exchange phenomena which successfully describe the slow rise of the total cross section with the centre of mass system energy in hadron-hadron and  $\gamma p$  interactions. Using the “bare” instead of the “effective” pomeron intercept, the CKMT [46] parametrization rises faster with  $x$  compared to former DOLA [47] calculations. The CKMT curves were calculated using the parameters as given in [46], without QCD evolution in the whole range.

The predictions for the Regge inspired models DOLA and CKMT lie below the data for  $Q^2 \geq 2 \text{ GeV}^2$  at low  $x$ . The latter were already shown to be significantly below the H1 data of 1993 [48]. The GRV and MRSA' parametrizations give a good description of the data in the range shown, with the possible exception of the first  $Q^2$  bin for the

latter. The MRSG and CTEQ3 distributions, which are not available for the lowest  $Q^2$  values, describe the higher  $Q^2$  data well.

### 7.3. Double asymptotic scaling

The success of the GRV approach suggests that the observed rise of the structure function  $F_2$  towards low  $x$  is generated by QCD dynamics. This was already observed in 1974 [6] from a study of the behaviour of  $F_2$  in the limit of large  $Q^2$  and low  $x$ . In this asymptotic region the QCD evolution determines the shape of  $F_2$ . Recently Ball and Forte [49] developed a convenient way to test the asymptotic behaviour of  $F_2$  using two variables

$$\begin{aligned}\sigma &\equiv \sqrt{\log(x_0/x) \cdot \log(\alpha_s(Q_0)/\alpha_s(Q))}, \\ \rho &\equiv \sqrt{\frac{\log(x_0/x)}{\log(\alpha_s(Q_0)/\alpha_s(Q))}},\end{aligned}\quad (10)$$

where  $\alpha_s(Q)$  is evaluated at the two-loop level [50].

The parameters  $x_0$  and  $Q_0^2$  have to be determined experimentally. The parameter  $Q_0^2$  is optimized by minimizing the  $\chi^2$  of a linear fit of  $\log(R'_F F_2)$  versus  $\sigma$  (see below) using data with  $Q^2 \geq 5 \text{ GeV}^2$ . This leads to a value of  $Q_0^2 = 2.5 \text{ GeV}^2$ . The same procedure was followed for  $x_0$ , which showed less sensitivity. The value  $x_0 = 0.1$ , as suggested in [49,51], was found to be a good choice. To visualize the double scaling, it was proposed to rescale  $F_2$  with factors  $R'_F$  and  $R_F$  defined as

$$R_F(\sigma, \rho) = 8.1 \exp\left(-2\gamma\sigma + \omega \frac{\sigma}{\rho} + \frac{1}{2} \log(\gamma\sigma) + \log\left(\frac{\rho}{\gamma}\right)\right) / \xi_F \quad (11)$$

with

$$\xi_F = 1 + ((\xi_1 + \xi_2) * \alpha_s(Q) - \xi_1 * \alpha_s(Q_0)) * (\rho / (2\pi * \gamma)) \quad (12)$$

and

$$R'_F(\sigma, \rho) = R_F \exp(2\gamma\sigma). \quad (13)$$

Here  $\xi_1 = (206n_f/27 + 6b_1/b_0)/b_0$ ,  $\xi_2 = 13$ ,  $b_0 = 11 - 2n_f/3$ ,  $\omega = (11 + 2n_f/27)/b_0$  and  $b_1 = 102 - 38n_f/3$ . The number of flavours is  $n_f$  and  $\gamma = \sqrt{(12/b_0)}$ . The function  $\log(R'_F F_2)$  is then predicted to rise linearly with  $\sigma$ .  $R_F F_2$  is expected to be independent of  $\rho$  and  $\sigma$ . Note that these expectations are valid only if the gluon distribution, which drives  $F_2$  at low  $x$  via the sea quarks, does not have a too singular behaviour for  $Q^2 = Q_0^2$ .

Fig. 10a shows  $R_F F_2$  versus  $\rho$  for the data with  $Q^2 \geq 3.5 \text{ GeV}^2$ . The value of  $A$  for four flavours was chosen to be 263 MeV [52]. The continuity of  $\alpha_s(Q)$  at the bottom quark mass threshold is imposed using the prescription in [38]. Approximate scaling is observed for  $Q^2 \geq 5 \text{ GeV}^2$  and  $\rho \geq 2$ . At high  $\rho$  the low  $Q^2$  data tend to violate the scaling behaviour which is seen clearly for the data at  $3.5 \text{ GeV}^2$ . In Fig. 10b, the results

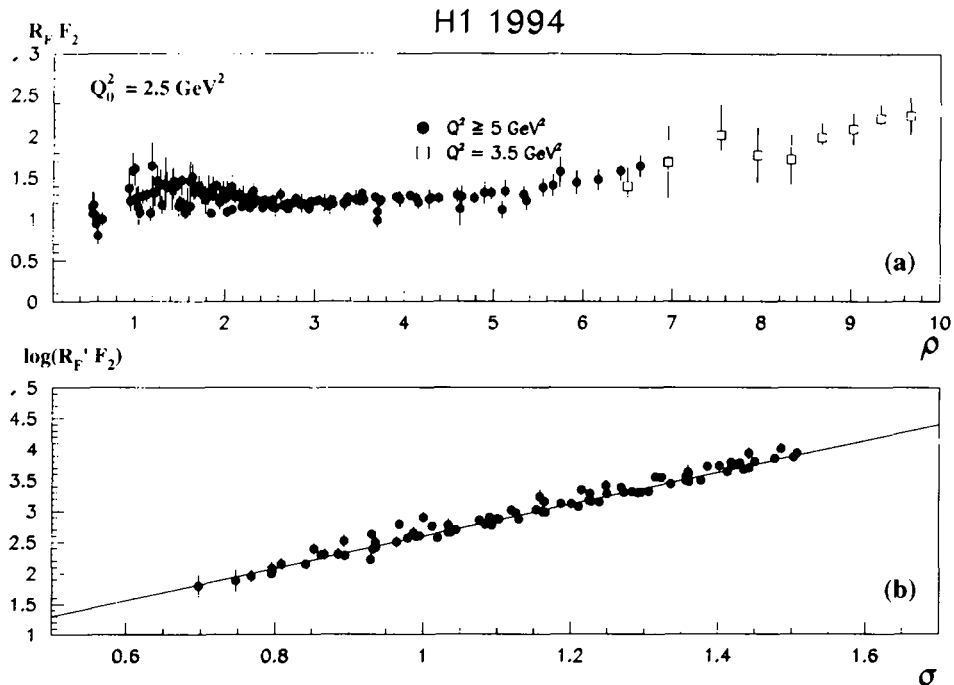


Fig. 10. The rescaled structure functions (a)  $R_F F_2$  versus  $\rho$  and (b)  $\log(R'_F F_2)$  versus  $\sigma$  (see text). Only data with  $Q^2 \geq 5 \text{ GeV}^2$  and  $\rho > 2$  are shown in (b).

are shown for  $\rho \geq 2$  and  $Q^2 \geq 5 \text{ GeV}^2$  as a function of  $\sigma$ . The data exhibit the expected linear rise of  $\log(R'_F F_2)$  with  $\sigma$ . A linear fit to the data gives a value for the slope of:  $2.50 \pm 0.02 \pm 0.06$  ( $2.57 \pm 0.05 \pm 0.06$ ) for  $Q^2 < 15 \text{ GeV}^2$  ( $Q^2 > 35 \text{ GeV}^2$ ) and 4 (5) flavours. The first error is the statistical error and the second error is the systematic error taking into account the point-to-point correlations. The value expected from QCD is 2.4 (2.5) for 4 (5) flavours. The results are in agreement with these predictions. Compared to the result presented in [51], the extraction based on the two-loop formalism used here is in better agreement with QCD expectation. Not included in this error is the influence of the uncertainty in the choice of  $\Lambda$ . Varying  $\Lambda$  by  $\pm 65 \text{ MeV}$  changes the result on the slope by  $\mp 0.03$ .

One can conclude that the low  $x$ , low  $Q^2$  measurements for  $Q^2 \geq 5 \text{ GeV}^2$  show scaling in  $\rho$  and  $\sigma$ . Thus double asymptotic scaling is a dominant feature of  $F_2$  in this region.

#### 7.4. Extraction of the gluon density

In a QCD analysis the evolution equations were solved numerically in the NLO order approximation following the procedure described in [53]. The splitting functions and the strong coupling constant  $\alpha_s(Q^2)$  are defined in the  $\overline{\text{MS}}$  factorization and renormalization schemes. In the DGLAP evolution equations only three light quark flavours are taken

into account. Heavy quark contributions are dynamically generated using the photon-gluon fusion (PGF) prescription given in [54,55], extended to NLO according to [56]. The scale of the PGF process has been taken as  $\sqrt{Q^2 + 4m_c^2}$  with a charm quark mass of  $m_c = 1.5$  GeV. An uncertainty of the charm quark mass of 0.5 GeV was considered which leads to a few percent variation of the gluon density. The small contribution of beauty quarks has been neglected.

The gluon  $g$ , the valence quark  $u_v$  and  $d_v$  and the non-strange sea  $S$  ( $S \equiv \bar{u} + \bar{d}$ ) distributions are parametrized at  $Q_0^2 = 5$  GeV<sup>2</sup> in the following way:

$$\begin{aligned} xg(x) &= A_g x^{B_g} (1-x)^{C_g}, \\ xu_v(x) &= A_u x^{B_u} (1-x)^{C_u} (1 + D_u x + E_u \sqrt{x}), \\ xd_v(x) &= A_d x^{B_d} (1-x)^{C_d} (1 + D_d x + E_d \sqrt{x}), \\ xS(x) &= A_S x^{B_S} (1-x)^{C_S} (1 + D_S x + E_S \sqrt{x}). \end{aligned} \quad (14)$$

The quark and antiquark components of the sea are assumed to be equal, and  $\bar{u}$  is set equal to  $\bar{d}$ . As determined in [57], the strange quark density is taken to be  $S/4$ . With these definitions the proton structure function  $F_2$ , for  $n_f = 3$  and to leading order, is given as

$$F_2(x, Q^2) = \frac{11}{18} xS + \frac{4}{9} xu_v + \frac{1}{9} xd_v. \quad (15)$$

The normalizations of the valence quark densities are fixed using the counting rules  $\int_0^1 u_v(x) dx = 2$  and  $\int_0^1 d_v(x) dx = 1$ . The normalization  $A_g$  of the gluon density is obtained via the momentum sum rule. Since no isoscalar data are available yet in the small  $x$  domain,  $B_u = B_d$  is assumed. The parameters  $B_S$  and  $B_g$  which govern the small  $x$  behaviour of  $F_2$  and of the gluon are allowed to be different. For  $A$  the value of 263 MeV is taken, as determined in [52].

In order to constrain the valence quark densities at high  $x$ , proton and deuteron results from the BCDMS and NMC experiments are also used. To avoid possible higher twist effects, data in the ranges  $Q^2 < 5$  GeV<sup>2</sup>, and  $Q^2 < 15$  GeV<sup>2</sup> for  $x > 0.5$  are not included in the fit. The small contribution of large rapidity gap events in the HERA data is considered to be part of the structure function, as there is no evidence that the QCD evolution of the diffractive part of  $F_2$  is significantly different from that of the total inclusive  $F_2$ .

The parton densities are derived from a fit of the evolution equations to the data using the program MINUIT. For the calculation of the  $\chi^2$  which was minimized, the statistical errors were combined in quadrature with those systematic errors which are uncorrelated. For BCDMS only statistical errors were included. In addition a term was added to the  $\chi^2$  to permit variation of the relative normalization of the different data sets. The following normalization errors were taken into account: H1 (nominal vertex sample): 1.5%, H1 (shifted vertex sample): 3.9%, BCDMS: 3%, and NMC: 2.5%. The  $\chi^2$  obtained in this procedure and the  $\chi^2$  computed when considering the full error of each point are given in Table 8.

Table 8

For each experiment are given: the number of data points used in the QCD fit, the  $\chi^2$  obtained as described in the text using only the uncorrelated errors, the  $\chi^2$  computed from the same fit using the full error on each point and the normalization factors as determined from the fit. The H1 nominal vertex and shifted vertex data samples are denoted as nvtx and svtx respectively.

Experiment	H1 nvtx	H1 svtx	NMC-p	NMC-D	BCDMS-p	BCDMS-D	total
data points	157	16	96	96	174	159	698
$\chi^2$ (unco. err.)	174	13	157	153	222	208	931
$\chi^2$ (full error)	85	6	120	114	122	140	591
normalization	1.00	1.04	1.00	1.00	0.97	0.97	

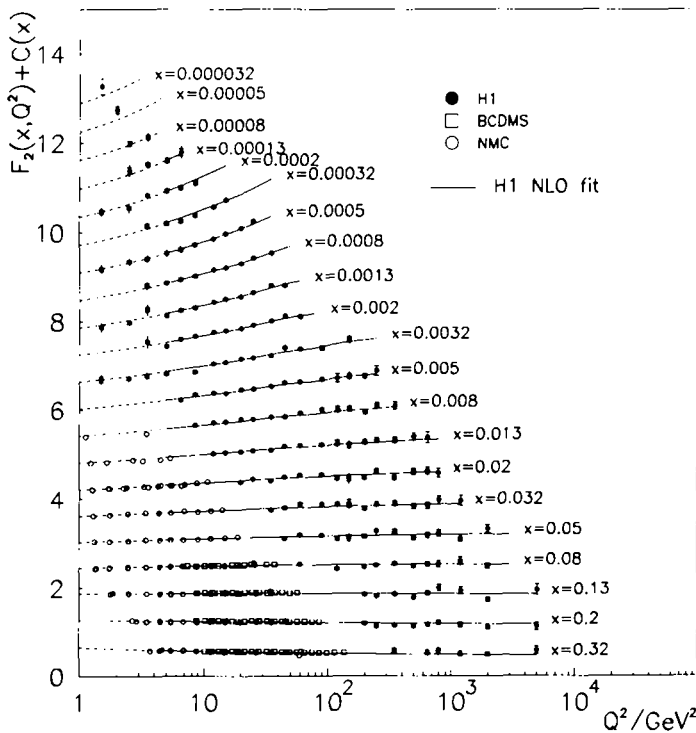


Fig. 11.  $F_2(x, Q^2)$  measured by H1 together with BCDMS [41] and NMC [40] fixed target results. The full line corresponds to the NLO QCD fit, see Section 7.4, which includes the data for  $Q^2 \geq 5 \text{ GeV}^2$ . The extension of the curves below  $5 \text{ GeV}^2$  represents only the backward evolution of the fit. The  $F_2$  values are plotted in a linear scale adding a constant  $c(x) = 0.6(i - 0.4)$  where  $i$  is the  $x$  bin number starting at  $i = 1$  from  $x = 0.32$ . The inner error bar is the statistical error, the outer corresponds to the full error resulting from adding the statistical and systematic error in quadrature. Some H1 data points at lower  $Q^2$  were shifted to nearby  $x$  values for graphical representation of the data.

The result of the fit is shown in Fig. 7 versus  $x$  and Fig. 11 versus  $Q^2$ . The fit gives a good description of all data used. Only small adjustments of the relative normalizations (given in Table 8) are required demonstrating remarkable agreement between these different experiments. In Fig. 7 the steep  $x$  behaviour of  $F_2$  is seen to be described very



Table 9

The values of the parameters at  $Q^2 = 5 \text{ GeV}^2$  of the gluon, the sea quark and valence quark densities, as determined from the QCD fit.

$A_g$	$B_g$	$C_g$			$A_u$	$B_u$	$C_u$	$D_u$	$E_u$
2.24	-0.20	8.52			2.84	0.55	4.19	4.42	-1.40
$A_S$	$B_S$	$C_S$	$D_S$	$E_S$	$A_d$	$B_d$	$C_d$	$D_d$	$E_d$
0.27	-0.19	1.66	0.16	-1.00	1.05	0.55	6.44	-1.16	3.87

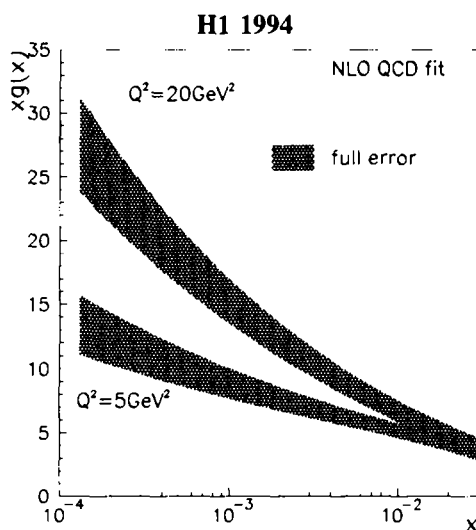


Fig. 12. The gluon density  $xg(x)$  at  $Q^2 = 5 \text{ GeV}^2$  and  $Q^2 = 20 \text{ GeV}^2$  extracted from a NLO QCD fit. The procedure to derive the error bands is explained in the text.

well by the fit. Note that the data for  $Q^2 < 5 \text{ GeV}^2$ , which were excluded from the fit, are still well reproduced by the fit evolved backwards in  $Q^2$ . However, a definite test of perturbative QCD in this region requires more accurate data and a study of possible higher twist effects, which is beyond the scope of this analysis. The  $Q^2$  dependence at fixed  $x$  is also described well over the nearly four orders of magnitude in  $Q^2$  covered by the H1 data, see Fig. 11. The parameters of the initial distributions are listed in Table 9. There are sizeable correlations between these parameters which were not studied in detail as the basic aim of this analysis was to extract the gluon density.

Fig. 12 shows the NLO gluon density  $xg(x, Q^2)$  at  $Q^2 = 5 \text{ GeV}^2$  and  $Q^2 = 20 \text{ GeV}^2$ . Note that there are no  $F_2$  measurements below  $5 \cdot 10^{-4}$  at  $Q^2 = 20 \text{ GeV}^2$ , but in that region the gluon is constrained by the data at lower  $Q^2$  via the QCD evolution equations. The experimental error band was determined in two steps: the initial error was obtained directly from the fit when considering only the uncorrelated errors of the

data points which are dominated by the statistical errors of the  $F_2$  measurement. Then the systematic errors introducing point-to-point correlations, as for instance a possible shift in the scattered electron energy, were treated in a procedure described in [51]. Their effect was added quadratically to the effect from the uncorrelated ones, determining the full experimental error band of the measurement of  $xg$ . A variation of  $A$  by 65 MeV [52] gives a change of 9% on the gluon density at  $20 \text{ GeV}^2$  which has not been added to the errors shown in Fig. 12.

The accuracy of this determination of  $xg$  is better by about a factor of two than the H1 result based on the 1993 data [51]. A rise of the gluon density towards low  $x$  is observed which is related to the behaviour of  $F_2 \propto x^{-\lambda}$ . Accordingly, the rise of  $xg$  towards low  $x$  increases with increasing  $Q^2$ .

## 8. Summary

A measurement has been presented of the proton structure function  $F_2(x, Q^2)$  in deep-inelastic electron-proton scattering at HERA with data taken in the running period of 1994. The integrated luminosity is  $2.7 \text{ pb}^{-1}$  which represents a tenfold increase in statistics compared to the  $F_2$  analysis based on the 1993 data of the H1 experiment. The structure function measurement includes data from different detector components and running configurations. Low  $Q^2$  values are reached using data with the  $ep$  interaction vertex shifted from the nominal position and with radiative events. The data cover a kinematic range for  $Q^2$  between 1.5 and  $5000 \text{ GeV}^2$  and  $x$  between  $3.0 \cdot 10^{-5}$  and 0.32.

The  $F_2$  values presented are obtained using different methods to reconstruct the inclusive scattering kinematics. At high values of the scaling variable  $y \geq 0.15$ , due to its superior resolution, the method used is based on the scattered electron energy and angle. Lower  $y$  values are covered with a method which combines electron and hadronic information to reduce radiative corrections and calibration errors. A smooth transition is observed from the fixed target high  $x$  data to the HERA low  $x$  data.

The rise of the structure function with decreasing  $x$  at fixed  $Q^2$  is confirmed. The rate of growth increases with increasing  $Q^2$  which has been one of the very first predictions of perturbative QCD. Approximate scaling in double logarithmic variables depending on  $x$  and  $Q^2$  is observed using a recent two-loop QCD calculation. The data are well described in the full  $x$  and  $Q^2$  range by a NLO fit based on the conventional DGLAP evolution equations. The fit results are used to measure the gluon distribution with improved precision down to  $x = 10^{-4}$ . The gluon density rises significantly for decreasing values of  $x$ .

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